



*Supplement of*

## **Multi-Machine Learning Ensemble Regionalization of Hydrological Parameters for Enhancing Flood Prediction in Ungauged Mountainous Catchments**

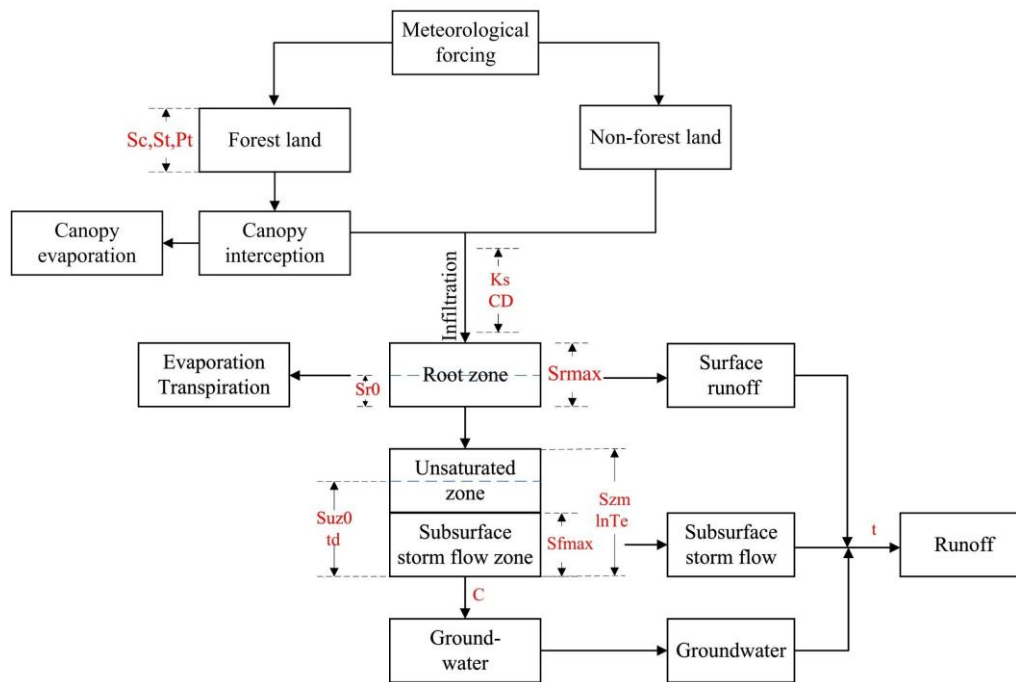
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## S1. The Topography-based Subsurface Storm Flow Hydrological Model (Top-SSF model)

The Topography-based Subsurface Storm Flow Hydrological Model (Top-SSF model) is a process-based model developed to simulate the hydrological response of mountainous catchments, with a particular emphasis on flash flood. The model structure (Fig. S1) and its key components are detailed in the subsequent sections.



**Fig S1.** Schematic diagram of the Top-SSF model structure

### S1.1 Canopy Interception

Canopy interception is calculated based on measured rainfall data and forest cover characteristics. The process is divided into three distinct phases: canopy wetting, canopy saturation, and canopy drying. In the Top-SSF model, the 1995 Gash model (Gash et al., 1995) was modified and used as the canopy interception module. The improved parts are as follows.

During the canopy humidification period, (1) the total interception equation for calculating the rainfall events was converted to the hourly canopy interception equation (Eq. 3), and (2) the total trunk runoff equation for calculating rainfall events was converted to the hourly trunk runoff equation (Eq. 4).

$$P'_g = -(\bar{R}/\bar{E})S_c \ln(1 - \bar{R}/\bar{E}) \quad (S1)$$

$$P''_g = \bar{R}/(\bar{R} - \bar{E})(S_t/P_t) + P'_g \quad (S2)$$

$$I(t) = \begin{cases} cP_g(t) & (P_g(t) < P'_g) \\ cP'_g + c\bar{E}(P_g(t) - P'_g)/\bar{R} + S_t & (P_g(t) \geq P'_g) \\ cP'_g + cP_t(1 - \bar{E}/\bar{R})(P_g(t) - P'_g) + c\bar{E}(P_g(t) - P'_g)/\bar{R} & (P_g(t) > P'_g, P_g(t) < P''_g) \end{cases} \quad (S3)$$

$$SF(t) = \begin{cases} 0 & (P_g(t) < P'_g) \\ cP_t(1 - \bar{E}/\bar{R})(P_g(t) - P'_g) - cS_t & (P_g(t) \geq P'_g) \\ 0 & (P_g(t) > P'_g, P_g(t) < P''_g) \end{cases} \quad (S4)$$

where:  $P'_g$  is the minimum rainfall required for the canopy to reach saturation (mm);  $\bar{R}$  is the average rainfall intensity (mm/h);  $\bar{E}$  is the average potential evaporation rate of the canopy (mm/h);  $S_c$  is the canopy storage capacity (mm);  $P''_g$  is the minimum rainfall needed in the trunk to reach saturation (mm);  $S_t$  is the trunk storage capacity (mm);  $P_t$  is the trunk runoff coefficient (%);  $I(t)$  is the canopy interception (mm);  $P_g(t)$  is the rainfall (mm);  $SF(t)$  is the trunk runoff (mm); and  $c$  is the forest canopy closure (%), which is equal to the forest cover.

During the canopy saturation period, canopy interception and trunk interception are equal to zero, and canopy evaporation can be estimated as potential evapotranspiration using the Penman–Monteith equation (Rutter et al., 1971).

During the canopy dry period, the original Gash model assumes that when the canopy is completely dry, the drying time exceeds 8 hours. In the Top-SSF model, Eq. S5 was used to calculate the hourly canopy evaporation:

$$E(t) = E_p(t) \left( \frac{C_h(t)}{S_c} \right) \quad (S5)$$

where  $E(t)$  for actual canopy evaporation (mm);  $C_h(t)$  is the depth of water held on canopy at time  $t$  (mm).

## S1.2 Soil Infiltration

In this study, infiltration is simulated using the Green-Ampt model. When surface ponding occurs, the infiltration rate is determined by solving the Green-Ampt equation iteratively, for which the Newton-Raphson method is employed. The infiltration rate

44 ( $f_{in}$ ) is given by:

$$45 \quad f_{in} = -\frac{Ks(CD+F_{satrt})}{Szm(1-\exp(F_{satrt}/Szm))} \quad (S6)$$

46 where,  $f_{in}$  is the infiltration rate (m/h);  $Ks$  is surface hydraulic conductivity (m/h);  
 47  $CD$  is capillary drive (m);  $F_{satrt}$  is the initial cumulative infiltration (m);  $Szm$  is the  
 48 maximum water storage capacity in the unsaturated zone (m).

### 49 **S1.3 Runoff Generation and Storage Dynamics**

#### 50 **S1.3.1 Soil Evaporation**

$$51 \quad E_a = E_{pt}\left(1 - \frac{Sr_z}{Sr_{max}}\right) \quad (S7)$$

52 where,  $E_a$  is the Actual soil evapotranspiration (m);  $E_{pt}$  is the potential  
 53 evapotranspiration (m);  $Sr_z$  is the root zone water deficit (m);  $Sr_{max}$  is the maximum  
 54 water storage capacity of the root zone (m).

#### 55 **S1.3.2 Overland Flow**

56 Overland flow in the Top-SSF model consists of saturation-excess and infiltration-  
 57 excess components.

58 Saturation-excess flow: Occurs when groundwater table depth  $S_i \geq 0$  at  
 59 computational cell  $i$ :

$$60 \quad r_{s,i} = \max\{S_{uz_i} - \max(S_i, 0), 0\} \quad (S8)$$

61 where  $r_{s,i}$  is the depth of saturation excess overland flow generated at cell  $i$  (m);  
 62  $S_{uz_i}$  is the soil water storage in the unsaturated zone, at cell  $i$  (m);  $S_i$  is the  
 63 groundwater table depth at cell  $i$  (m).

64 Infiltration-excess flow: Activated when rainfall intensity exceeds soil infiltration  
 65 capacity.

#### 66 **S1.3.3 Subsurface storm flow**

67 Water deficit in subsurface storm flow zone ( $S_{sf,i}$ ) is determined by topographic  
 68 controls:

$$69 \quad S_{sf,i} = S_{fmax} - \frac{\left(\frac{a}{\tan\beta}\right)A_i}{\int_A \left(\frac{a}{\tan\beta}\right)dA_i} (S_{fmax} - \bar{S}_{sf}) \quad (S9)$$

70 where,  $S_{sf,i}$  is the water deficit in the subsurface storm flow zone at cell  $i$  (m);  $S_{fmax}$

71 is the maximum subsurface storm flow zone deficit (m);  $\frac{a}{\tan \beta}$  is the subsurface  
 72 topographic index (-);  $\bar{S}_{sf}$  is the average water deficit in the subsurface storm flow  
 73 zone (m);  $A_i$  is the percentage of the catchment area occupied by cell  $i$  (%).

74 The unsaturated zone recharges the subsurface storm flow zone:

$$75 \quad r_{v,i} = \frac{S_{uz,i}}{S_{it_d}} \quad (S10)$$

76 where,  $r_{v,i}$  is the depth of unsaturated zone recharges the subsurface storm flow zone  
 77 at cell  $i$  (m);  $t_d$  is the unsaturated zone time delay per unit storage deficit (h/m).

78 The depth of storm subsurface flow generated at computational cell  $i$ ,  $r_{sf,i}$  is  
 79 given by:

$$80 \quad r_{sf,i} = q_{sf0}(1 - S_{sf,i}/S_{fmax}) \quad (S11)$$

81 where,  $r_{sf,i}$  is the depth of subsurface storm flow at cell  $i$  (m);  $q_{sf0}$  is initial  
 82 subsurface storm flow (m);  $S_{sf,i}$  is the water storage deficit in the subsurface storm  
 83 flow zone at cell  $i$  (m).

84 The subsurface storm flow recharges the groundwater:

$$85 \quad r_{g,i} = \min(C(S_{fmax} - S_{sf,i}), S_i) \quad (S12)$$

86 where,  $r_{g,i}$  is the subsurface storm flow recharge groundwater at  $i$  (m);  $C$  is the  
 87 transfer coefficient (m<sup>2</sup>/h).

88 The average water deficit of subsurface storm flow zone ( $\bar{S}_{sf}$ ) and the average  
 89 depth of groundwater ( $\bar{S}_g$ ) in the catchment are updated as follows:

$$90 \quad \Delta \bar{S}_{sf} / \Delta t = - \sum_{i=1}^M r_{v,i} A_i + \sum_{i=1}^M r_{sf,i} A_i + \sum_{i=1}^M r_{g,i} A_i \quad (S13)$$

$$91 \quad \Delta \bar{S}_g / \Delta t = - \sum_{i=1}^M r_{g,i} A_i + r_b \quad (S14)$$

92 where,  $\Delta \bar{S}_{sf}$  is the change in the average subsurface storm flow zone (m);  $M$  is the  
 93 total number of computational cells;  $\Delta \bar{S}_g$  is the change in the average groundwater  
 94 level (m);  $\Delta t$  is the time step (h);

### S1.3.4 Groundwater Flow

The depth of groundwater discharge is calculate as;

$$r_b = e^{\ln Te - \lambda - \bar{S}_g / Szm} \quad (S15)$$

where,  $r_b$  is depth of groundwater discharge (m);  $\ln Te$  is the log of the areal average of  $T0$  ( $m^2/h$ );  $\lambda$  is the catchment average topographic index;  $\bar{S}_g$  is the catchment average groundwater table depth (m).

### S1.4 Flow Routing

Catchment response time calculation:

$$T_{c,j} = t \sum_{k=1}^j \left( \frac{0.87 L_{ch,n}}{1000 S_{ch,n}} \right)^{0.385} \quad (S16)$$

where  $N$  is the number of river subsections within the catchment;  $L_{ch,n}$  is the length of the river channel (km);  $S_{ch,n}$  is the slope of the river segment ( $m \cdot m^{-1}$ ); and  $t$  is the time-correction coefficient (-).

For any simulation time step  $t$ , the proportion of the catchment area contributing to the flow at the outlet is determined. If the simulation time  $t$  is greater than or equal to the time of concentration for the catchment,  $T_{c,N}$  (i.e., the time of concentration from the most hydrologically distant point), then the entire catchment area is assumed to be contributing. Otherwise, if the simulation time  $t$  is less than  $T_{c,N}$ , the catchment is partially contributing. The proportion of the catchment area, contributing to the outlet flow at time  $t$  is calculated by linear interpolation between isochrones:

$$AR_t = ACH_{j-1} + \frac{t - T_{c,j-1}}{T_{c,j} - T_{c,j-1}} (ACH_j - ACH_{j-1}) \quad (S17)$$

where,  $AR_t$  is the proportion of the catchment area contributing to outlet flow at time  $t$  (%);  $T_{c,j}$  and  $T_{c,j-1}$  are the travel times defining the boundaries of the  $j$ -th and  $(j - 1)$ -th isochrones, respectively (h);  $ACH_j$  and  $ACH_{j-1}$  are the cumulative proportions of the total catchment area enclosed by the  $j$ -th and  $(j - 1)$ -th isochrones, respectively (%).

## S2. Hyperparameter configurations

**Table S1.** DT Hyperparameter configurations

	max_depth	min_samples_split	min_samples_leaf
<i>lnTe</i>	15	9	3
<i>Szm</i>	6	4	2
<i>td</i>	18	4	2
<i>Sfmax</i>	8	6	2
<i>C</i>	18	2	1
<i>qsfo</i>	14	2	1
<i>t</i>	18	6	2

**Table S2.** ERT Hyperparameter configurations

	n_estimators	min_samples_split	min_samples_leaf	max_features	max_depth
<i>lnTe</i>	500	2	1	0.9	15
<i>Szm</i>	200	5	1	0.5	10
<i>td</i>	500	2	1	0.9	15
<i>Sfmax</i>	500	2	1	0.1	15
<i>C</i>	500	2	1	0.9	15
<i>qsfo</i>	400	2	1	0.1	15
<i>t</i>	500	2	1	0.9	25

**Table S3.** GBM Hyperparameter configurations

	subsample	n_estimators	min_samples_split	min_samples_leaf	max_depth	learning_rate
<i>lnTe</i>	1.0	800	2	1	9	0.1
<i>Szm</i>	1.0	200	2	1	3	0.1
<i>td</i>	1.0	200	2	1	4	0.1
<i>Sfmax</i>	0.8	800	2	1	9	0.1
<i>C</i>	0.6	300	2	1	5	0.05
<i>qsfo</i>	0.8	800	2	1	9	0.1
<i>t</i>	0.8	800	2	1	9	0.1

125 **Table S4.** KNN Hyperparameter configurations

	p	n_neighbors
<i>lnTe</i>	1	20
<i>Szm</i>	3	6
<i>td</i>	1.0	4
<i>Sfmax</i>	1	7
<i>C</i>	1	4
<i>qsf0</i>	1	30
<i>t</i>	1	5

126 **Table S5.** RF Hyperparameter configurations

	n_estimators	max_depth	min_samples_split	min_samples_leaf
<i>lnTe</i>	1000	10	5	1
<i>Szm</i>	100	30	4	2
<i>td</i>	100	30	5	2
<i>Sfmax</i>	200	80	2	1
<i>C</i>	1000	90	10	2
<i>qsf0</i>	700	10	2	1
<i>t</i>	500	60	2	1

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128 **Table S6.** SVM Hyperparameter configurations

	tol	shrinking	kernel	gamma	C
<i>lnTe</i>	0.0001	True	rbf	10	50
<i>Szm</i>	0.0001	True	rbf	scale	0.1
<i>td</i>	0.0001	True	linear	10	1
<i>Sfmax</i>	0.0001	True	rbf	scale	0.1
<i>C</i>	0.001	True	poly	0.1	10
<i>qsf0</i>	0.0001	True	rbf	scale	0.1
<i>t</i>	0.0001	True	rbf	scale	0.1



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