



Deep learning of flood forecasting by considering interpretability and physical constraints

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Abstract. Deep learning models show promise for flood forecasting but often lack interpretability and physical realism. To bridge this gap, we enhance traditional Long Short-Term Memory (LSTM) networks by integrating: (1) a feature-time attention mechanism that emphasizes critical input features and historical moments by learning dynamic weights, and (2) physics-guided constraints that enforce fundamental hydrological principles by considering the monotonic relationships between inputs and outputs. Tested in China's Luan River Basin for 1–6 h flood predictions, the proposed physics-guided feature-time-based multi-head attention mechanism LSTM (PHY-FTMA-LSTM) outperforms standard LSTM and attention-only variants. It achieves exceptional accuracy with Nash-Sutcliffe efficiency (NSE) values of 0.988 at $t + 1$ and maintains strong performance at 0.908 at $t + 6$, offering valuable insights for enhancing interpretability and physical consistency in deep learning approaches.

1 Introduction

Floods are one of the most common and destructive natural hazards, posing a great threat to human life, infrastructure, and socio-economic conditions (Kellens et al., 2013; Mourato et al., 2021). Building reliable and accurate flood forecasting models is the foundation for sustainable flood risk management with a focus on prevention and protection, and is one of the most challenging tasks in hydrological forecasting (Birkholz et al., 2014; Zhang et al., 2016).

Traditional hydrological models simulate hydrological processes such as rainfall runoff with a clear physical

meaning, but their construction often demands rich hydro-meteorological data and subsurface information. Additionally, the large number of parameters involved poses challenges in determining their values, limiting their practical applicability (Chen et al., 2011). In contrast, data-driven machine learning (ML) models, which do not rely on explicit consideration of the physical mechanisms governing hydrological processes and only analyze the statistical relationships between inputs and outputs, have been widely used in hydrology in recent years (Lima et al., 2016; Yang et al., 2020; Yu et al., 2006; Zhu et al., 2005). Among them, deep learning (DL) models with multiple hidden layers have demonstrated significant advantages, including convolutional neural networks (CNNs), recurrent neural networks (RNNs), and their variants such as long short-term memory neural networks (LSTMs), and gated recurrent units (GRUs). LSTM, a type of RNN, is specifically designed for learning long-term dependencies, and its architectural enhancements effectively address issues such as gradient disappearance and explosion that are inherent to traditional RNNs. Consequently, LSTM has emerged as a highly favored model in flood forecasting (Cui et al., 2021; Kao et al., 2020; Lupichini et al., 2022; Lv et al., 2020).

The DL models, with their powerful characterization capabilities, excel in fitting observations and have high prediction accuracy for hydrological problems such as flood forecasting, but they still have limitations. First, the interpretability of DL models is poor (Nearing et al., 2021). The inherent black-box nature of DL models makes it difficult to understand the significance of model parameters and the decision-making process. The attention mechanism is an approach to enhance the interpretability of DL models (Vaswani et al., 2017). At-

tention allows for the interpretation of feature importance by selectively emphasizing critical information from a multitude of input variables through attention weights. Moreover, attention weights can be visualized to gain insights into the underlying reasoning behind the model's predictions. The attention mechanism has been successfully applied in various domains. Song et al. (2017) proposed an end-to-end spatio-temporal attention model for recognizing human actions from skeleton data, selectively attending to distinguishable joints within each frame of the input, and assigning different levels of attention to the output of different frames. Zhang et al. (2021) constructed an anomaly structure by incorporating spatial attention and channel attention modules, which facilitated the creation of feature spaces characterized by high compactness within the same class and separation between different classes, resulting in the accurate classification of floral images. As for hydrological forecasting, Wang et al. (2023) introduced an improved spatio-temporal attention mechanism model (STA-LSTM) for predicting river water levels. By visualizing attention weights, they discovered that the hydrological station closer to the outlet had greater influence, while the temporal weights decreased with increasing historical moments. However, it should be noted that the discussed model (STA-LSTM) considers only a single historical water level as input, neglecting the potential influence of other relevant input features on the final prediction. This limitation underscores the need for further research and development to explore the incorporation of multiple input features in attention mechanisms for more comprehensive and accurate models.

Second, the DL models lack physical mechanisms. DL models primarily focus on establishing a mapping relationship between inputs and outputs, overlooking the underlying physical connections between them (Jiang et al., 2020). Consequently, the prediction results obtained from DL models may be physically inconsistent or unreliable due to extrapolation or observation bias (Reichstein et al., 2019). To address this limitation, researchers have proposed incorporating physical constraints into the loss function, which serves as the optimization objective of DL models. By adding physical theory as a priori knowledge, the models can be constrained to generate outputs that are consistent with the underlying physical principles, thereby enhancing their physical consistency. Several studies have explored this approach in different contexts. Read et al. (2019) chose the law of energy conservation as a physical constraint in temperature simulation to build a lake water temperature prediction model that conforms to physical theory. Wang et al. (2020) proposed a theory-guided neural network (TgNN) framework for groundwater flow that incorporates control equations, boundary conditions, initial conditions, and expert knowledge as additional terms in the loss function to guide the training process. Xie et al. (2021) considered extreme storm events, long-duration rainless events, and rainfall-runoff monotonic relationships in the rainfall-runoff process

at a daily scale and constrained LSTM with these three physical mechanisms to improve the physical interpretability.

Moreover, the current inputs for the DL models in flood forecasting are mainly historical runoff, rainfall, and evapotranspiration (Leedal et al., 2013; Rahimzad et al., 2021; Wan et al., 2019), but the initial soil moisture is also a crucial parameter, particularly for arid watersheds (Grillakis et al., 2016). The initial soil moisture directly affects the soil infiltration capacity, water input and output from the soil, and ultimately, the flooding process. Therefore, the paper also explores the effect of initial soil moisture on flood forecasting through the attention weight visualization matrix.

Based on the above research, this paper proposes a combined feature-time multi-head attention mechanism and physical constraints model for flood forecasting, named PHY-FTMA-LSTM. The main contributions of this work are outlined as follows: (1) The initial soil moisture in the watershed is introduced as an input, alongside historical runoff, rainfall, and evapotranspiration, these four input features are considered to investigate their influence on the flooding process. (2) The dual attention module of features and time and multiple attention heads are used. The resulting attention weight matrix is visualized to enhance the interpretability of the model, providing insights into the importance of different features and time dynamics. (3) The physical constraints of flood forecasting are combined with the DL models at hourly scales to enhance the physical consistency of the model. By optimizing the loss function, the model incorporates the monotonic relationship between rainfall, evapotranspiration, initial soil moisture, and runoff during the flooding process. This integration ensures that the output aligns with physical laws.

The novelty of this study is that, for the first time, the attention mechanism and physical constraints are simultaneously incorporated into the DL model based on the hourly scale, and the important parameter of soil moisture content is added as input to forecast flood with a lead time of 1–6 h in Luan River Basin in China as an example, which improves the prediction performance of flood forecasting models while enhancing interpretability and physical law consistency. The proposed PHY-FTMA-LSTM can effectively leverage key input information and produce prediction results that conform to the monotonicity constraints on the water balance.

2 Methods

To increase the interpretability and physical consistency of DL models in flood forecasting, this paper establishes a PHY-FTMA-LSTM model that combines the feature-time-based multi-head attention mechanism with physical constraints (Fig. 1a). The attention mechanism consists of a dual module: feature-based attention and time-based attention. In the feature-based attention module, the model generates a feature-based attention matrix that assigns different weights

to the input features based on their importance. Similarly, the time-based attention module generates a time-based attention matrix that assigns different weights to historical moments. By taking the element-wise product of these two matrices, the model generates the feature-time-based attention matrix (Fig. 1b). To enhance the modeling capability, the multi-head attention mechanism is utilized. Multiple attention heads are computed in parallel, and their outputs are averaged to balance the influence of each subhead. The attention weight matrix is then multiplied with the input matrix, resulting in the output of the feature-time-based multi-head attention layer (Fig. 1c). In addition, the physical constraints of the hydrological cycle process are added to the loss function to make the output conform to the physical laws. And the model is compared with the original LSTM, the feature-time-based attention LSTM (FTA-LSTM), and the feature-time-based multi-head attention LSTM (FTMA-LSTM).

2.1 LSTM

The LSTM model aims to alleviate the weaknesses of ordinary RNNs in handling long-time dynamics (Zhao et al., 2017). Different from the circular structure of the RNN hidden layer, the hidden layer of the LSTM introduces the memory cell, which consists of an input gate, forget gate, and output gate to selectively remember and forget the input data, and its structure is shown in Fig. 1d. The inputs at time t include the input information x_t at t , the hidden layer state h_{t-1} , and the cell state c_{t-1} at $t-1$. First, the forget gate determines the extent to which cell state c_{t-1} is discarded. Next, the input gate decides how much of the current external information x_t to retain and generates the candidate cell state $\bar{c}_t$. Then, c_t is updated based on the results of the forget and input gate. Finally, the output gate decides which state features of c_t are output and generates the hidden layer state variable h_t (Duan et al., 1992). The above process can be expressed as follows:

$$f_t = \sigma(W_f \cdot [h_{t-1}, x_t] + b_f) \quad (1)$$

$$i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i) \quad (2)$$

$$\bar{c}_t = \tanh(W_c \cdot [h_{t-1}, x_t] + b_c) \quad (3)$$

$$c_t = c_{t-1} \odot f_t + \bar{c}_t \odot i_t \quad (4)$$

$$o_t = \sigma(W_o \cdot [h_{t-1}, x_t] + b_o) \quad (5)$$

$$h_t = \sigma \odot \tanh(c_t) \quad (6)$$

where W_f , W_i , W_c , W_o are the weight vectors of the three gates and the gating unit, respectively. Similarly, b_f , b_i , b_c , b_o are the bias vectors. σ is the Sigmoid activation function. $\tanh$ is the hyperbolic tangent activation function. $\odot$ denotes the vector element product.

2.2 Attention mechanism

The attention mechanism is inspired by the concept of human visual selective attention, which helps neural networks

focus on important information while disregarding irrelevant details, thereby establishing connections between inputs and outputs (Brauwers and Frasinicar, 2023; Niu et al., 2021). By incorporating the attention mechanism, the model can allocate varying degrees of attention to different historical moments or feature vectors within the input sequence. This enables the model to automatically identify and prioritize the most relevant input information, leading to more accurate modeling of flood causes and trends. Ultimately, this improves the accuracy of flood prediction results and enhances the interpretability of the model.

In this study, a soft attention module is introduced before the original LSTM's input. This module calculates attention weight matrices separately for input features and historical moments and then combines them to produce a feature-time attention weight matrix.

The feature-based attention module can focus on the effects of different features on predicted floods and improve the model's attention to important features. In this paper, the input features are runoff, rainfall, evapotranspiration, and initial soil moisture. Let the input be a two-dimensional matrix $X \in R^{k \times n}$, where k and n denote the number of input features and the number of historical moments, respectively, then the input matrix at time t can be regarded as n k -dimensional vectors $X_t = [x_1^t, x_2^t, \dots, x_k^t]_{1 \times k}^T$. The input features at each time step are normalized using the softmax function (Eqs. 7 and 8). The attention weight matrix based on the input features is obtained by synthesizing the feature weights of all historical moments.

$$\alpha_i^t = \text{softmax}(x_i^t) = \frac{e^{-x_i^t}}{\sum_{i=1}^k e^{-x_i^t}} \quad (7)$$

$$\alpha_t = [\alpha_1^t, \alpha_2^t, \dots, \alpha_k^t]_{1 \times k}^T \quad (8)$$

where α_i^t is the weight of the i th feature, and $\sum_{i=1}^k \alpha_i^t = 1$.

The time-based attention module allows simulating the relationship between different time steps, focusing on the more important historical moments. The input matrix of features can be viewed as $X_k = [x_k^{t-n-1}, x_k^{t-n-2}, \dots, x_k^t]_{1 \times n}$, and the same softmax function (Eq. 9) is used to generate the time-based attention weights (Eq. 10), and the time weights of all features are synthesized to be the attention weight matrix based on historical moments.

$$\beta_k^i = \text{softmax}(x_k^i) = \frac{e^{-x_k^i}}{\sum_{i=1}^n e^{-x_k^i}} \quad (9)$$

$$\beta_k = [\beta_1, \beta_2, \dots, \beta_n]_{1 \times n} \quad (10)$$

where β_k^i is the weight of the i th time step, and $\sum_{i=1}^n \beta_k^i = 1$. Finally, the above two weight matrices are multiplied element by element to obtain the attention weight matrix that focuses on both the input features and historical moments

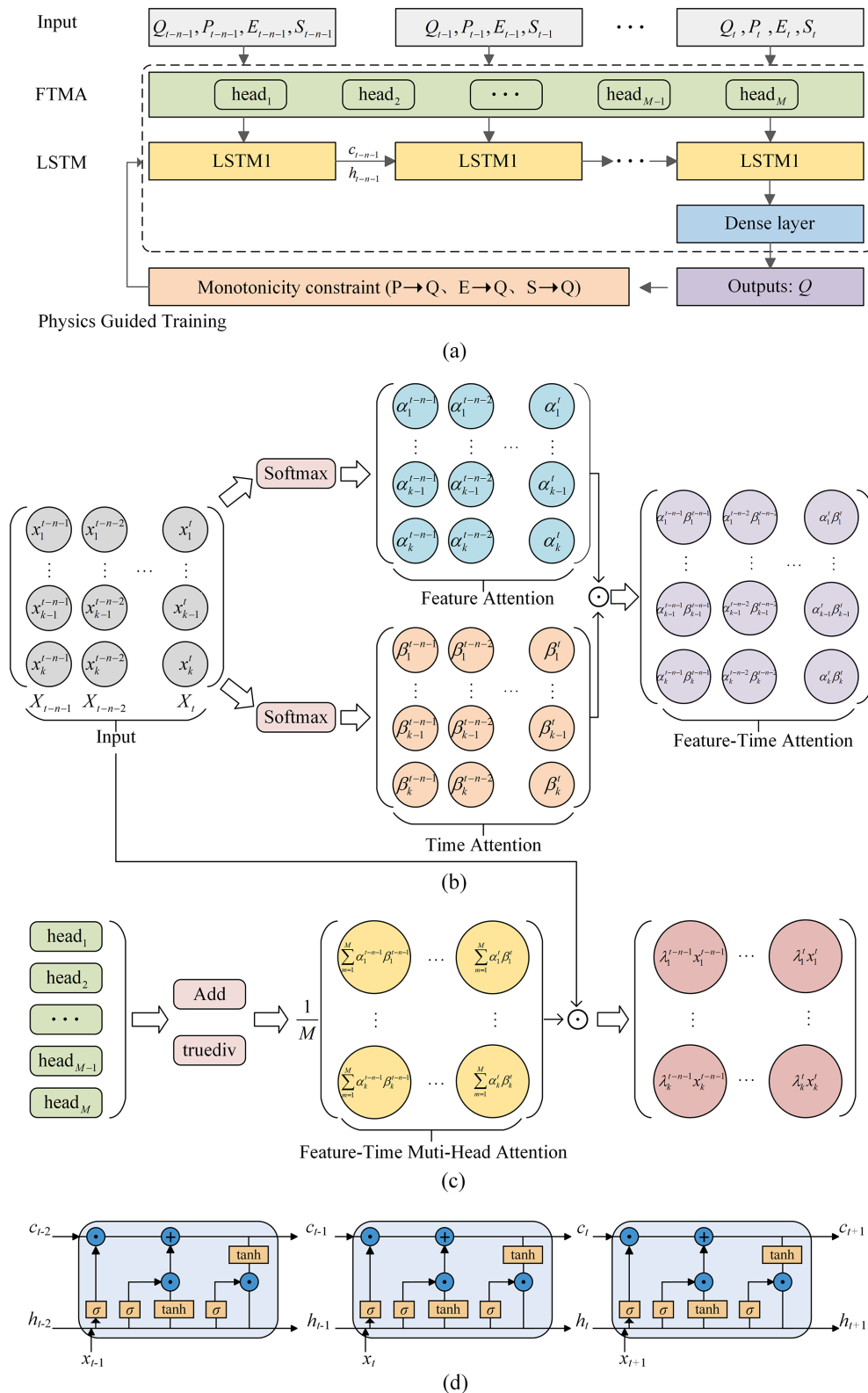


Figure 1. (a) The PHY-FTMA-LSTM model architecture. (b) Feature-time-based attention matrix generation process for each attention head. (c) Feature-time-based multi-head attention workflow. (d) The internals of LSTM cells.

(Eq. 11).

$$\begin{aligned} \text{FTA} &= \text{FA} \odot \text{TA}^T \\ &= \begin{bmatrix} \alpha_1^{t-n-1} \beta_1^{t-n-1} & \cdots & \alpha_1^t \beta_1^t \\ \vdots & \ddots & \vdots \\ \alpha_k^{t-n-1} \beta_k^{t-n-1} & \cdots & \alpha_k^t \beta_k^t \end{bmatrix}_{k \times n} \end{aligned} \quad (11)$$

where FA represents feature-based attention weight matrix, TA represents time-based attention weight matrix.

To enhance model expressiveness and interpretability, this study also employs a multi-head attention mechanism. This mechanism involves passing input sequences through m independent attention heads in parallel. Each head can be seen as a distinct representation space, enabling the model to concurrently focus on different parts of the input. As a result, the model becomes more capable of capturing the intricate relationships between inputs and gaining a deeper understanding of the input data.

The multi-head attention mechanism computes m sets of attention coefficients based on the number of heads, adds the output tensor of the attention heads using the Add function, and then balances the effects of different sub-heads by averaging operations. Finally, the average output tensor is multiplied by the input to get the final output, which makes the attention head weights more discriminative and better captures the relationship between sequences. The feature-time-based multi-head attention weight matrix is as follows:

$$\begin{aligned} \text{FTMA} &= \\ &= \frac{1}{M} \begin{bmatrix} \sum_{m=1}^M \alpha_1^{t-n-1} \beta_1^{t-n-1} & \cdots & \sum_{m=1}^M \alpha_1^t \beta_1^t \\ \vdots & \ddots & \vdots \\ \sum_{m=1}^M \alpha_k^{t-n-1} \beta_k^{t-n-1} & \cdots & \sum_{m=1}^M \alpha_k^t \beta_k^t \end{bmatrix}_{k \times n} \end{aligned} \quad (12)$$

where M represents the number of attention heads.

2.3 Physical constraints

The LSTM is a black-box model that ignores complex physical processes, making it difficult to maintain consistency with the basic principles of flood forecasting (Yokoo et al., 2022). To overcome this limitation, the physical constraints can be combined with the DL models to enhance the physical consistency by modifying the model loss function and transforming the prior knowledge of flood forecasting into the penalty term of the loss function. A soft penalty is often utilized to enforce constraints on the model's behavior (Karniadakis et al., 2021), ensuring adherence to physical principles such as conservation and monotonicity.

In the DL models for flood forecasting, the occurrence of flooding due to heavy rainfall is influenced by various factors, including rainfall intensity, evapotranspiration, infiltration, and storage dynamics. When considering the input features of rainfall, evapotranspiration, and initial soil moisture, it is important to maintain a monotonic relationship between

each feature and the resulting runoff. However, the traditional DL models disregard the physical relationships between inputs and outputs. This lack of consistency with the physical principles of water balance equations undermines the overall reliability of the model. Therefore, this study incorporates inequality constraints to enforce the desired monotonic relationships between rainfall, evapotranspiration, initial soil moisture, and runoff. Under the assumption that all other input variables remain unchanged, a new time series of rainfall, evapotranspiration, and initial soil moisture is generated respectively by applying random minor increments within the range $[0, 0.1)$ using the random.uniform function. These new time series are then combined with the unchanged time series to form new input data. The difference between the predicted values corresponding to the new data and the predicted values corresponding to the original input data is calculated. This difference is then converted into a specific loss value using the Rectified Linear Unit (ReLU) function and added to the loss function.

For rainfall, the runoff should increase if there is a slight increase in rainfall at the current time step, provided that other variables are constant, and the monotonic relationship and losses for rainfall-runoff are expressed as follows:

$$f[p(t) + \Delta p, t] - f[p(t), t] \geq 0 \quad (13)$$

Loss_p =

$$\frac{1}{N_p} \sum_{i=1}^{N_p} \{\text{ReLU}\{f[p(t), t] - f[p(t) + \Delta p, t]\} \geq 0\}^2 \quad (14)$$

where Δp is the small increase in rainfall, Loss_p is the error in the monotonic relationship of rainfall runoff, N_p is the sample length of the perturbed rainfall, and ReLU is the response function.

For evapotranspiration, the runoff should decrease if there is a slight increase in evapotranspiration at the current time step, provided that other variables are constant, and the monotonic relationship and losses for evapotranspiration runoff are expressed as follows:

$$f[e(t) + \Delta e, t] - f[e(t), t] \leq 0 \quad (15)$$

Loss_e =

$$\frac{1}{N_e} \sum_{i=1}^{N_e} \{\text{ReLU}\{f[e(t), t] - f[e(t) + \Delta e, t]\} \leq 0\}^2 \quad (16)$$

where Δe is the small increase in evapotranspiration, Loss_e is the error in the monotonic relationship of evapotranspiration runoff, N_e is the sample length of the perturbed evapotranspiration.

For soil moisture, the runoff should increase if the initial soil moisture of the watershed increases slightly for each flood event, provided that other variables are constant, and the monotonic relationship and losses between initial soil

moisture and runoff are expressed as follows:

$$f[s(t) + \Delta s, t] - f[s(t), t] \geq 0 \quad (17)$$

Loss_s =

$$\frac{1}{N_s} \sum_{i=1}^{N_s} \{\text{ReLU}\{f[s(t), t] - f[s(t) + \Delta s, t]\} \geq 0\}^2 \quad (18)$$

where Δs is the small increase in initial soil moisture, Loss_s is the error in the monotonic relationship of initial soil moisture runoff, N_s is the sample length of the perturbed initial soil moisture.

Based on the above physical constraints of flood forecasting, the loss function of the traditional LSTM model is improved with the following equation:

$$\text{Loss} = \lambda_{\text{data}} \text{Loss}_{\text{data}} + \lambda_p \text{Loss}_p + \lambda_e \text{Loss}_e + \lambda_s \text{Loss}_s \quad (19)$$

where Loss is the loss function of the LSTM guided by the physical constraints of flood forecasting; Loss_{data} is the mean squared error (MSE) of the observed and predicted values of the LSTM; λ_{data} , λ_p , λ_e , λ_s are the weighting coefficients of different losses, respectively. To treat the three physical constraints equally, the weighting coefficients of the four losses are set to {0.7, 0.1, 0.1, 0.1}.

2.4 Evaluation metrics

To evaluate the accuracy of different models for flood forecasting, the Nash-Sutcliffe efficiency (NSE), Kling-Gupta efficiency (KGE), the coefficient of determination (R^2), root mean squared error (RMSE), and mean absolute error (MAE) are selected for evaluation. The specific equations are as follows:

$$\text{NSE} = 1 - \frac{\sum_{i=1}^n (Q_t - Q'_t)^2}{\sum_{i=1}^n (Q_t - \bar{Q}_t)^2} \quad (20)$$

$$\text{KGE} = 1 - \sqrt{(R-1)^2 + (\alpha-1)^2 + (\beta-1)^2} \quad (21)$$

$$R^2 = \frac{\left(\sum_{i=1}^n (Q_t - \bar{Q}_t)(Q'_t - \bar{Q}'_t)\right)^2}{\sum_{i=1}^n (Q_t - \bar{Q}_t)^2 \sum_{i=1}^n (Q'_t - \bar{Q}'_t)^2} \quad (22)$$

$$\text{RMSE} = \sqrt{\frac{\sum_{i=1}^n (Q_t - Q'_t)^2}{n}} \quad (23)$$

$$\text{MAE} = \frac{1}{n} \sum_{i=1}^n |Q_t - Q'_t| \quad (24)$$

where Q_t is the observed value; Q'_t is the predicted value; $\bar{Q}_t$ is the observed mean value; $\bar{Q}'_t$ is the mean value of the predicted series; α between the standard deviation of the predicted value and that of the observed value; β is the ratio between the mean of the predicted value and that of the observed value; n is the total number of samples. The NSE is commonly used to evaluate hydrological prediction models, KGE considers the contribution of mean, variance and correlation on model performance, R^2 is often used to evaluate

the linear correlation between the forecast process and the observed process. The values of NSE, KGE and R^2 range from 0 to 1. The closer the result is to 1, the more accurate the forecast result is and the higher the model credibility is. RMSE and MAE are used to reflect the degree of deviation between the predicted and observed values, the smaller the value the smaller the deviation.

3 Study area and data

3.1 Study area

In this study, the watershed controlled by the Sandaohezi station in the Luan River Basin was selected as the study area. The Luan River originates from the northern foot of Bayangurtu Mountain in Hebei Province, with a total length of 888 km, and flows through Inner Mongolia, Hebei, and Liaoning provinces before injecting into the Bohai Sea at Laoting County, Hebei Province. The station is in the middle reaches of the mainstream of the Luan River, controlling a watershed area of 17 100 km², accounting for about 40 % of the total area of the Luan River basin. Geographically, it is located between 115.5 to 117.7° E longitude and 40.7 to 42.7° N latitude. The elevation of the study area ranges from 370 to 2300 m, with a high northwest to low southeast topography. Based on geological conditions and geomorphological features, the area can be divided into two dominant landform types: plateau and mountainous terrain. The plateau dominates the northern part of the basin, with elevations ranging from 1400 to 1600 m and a gentle channel gradient averaging approximately 0.5‰. The remaining area comprises mountainous terrain, exhibiting complex topography shaped by prolonged denudation and erosion. This zone features steep mountains, densely distributed hills, and interspersed basins, with slope angles varying between 20 and 40°. In certain areas, rivers demonstrate downward cutting action, resulting in significantly steeper channel gradients – typically 2‰–6‰, while some and small tributaries exceed 20‰. Notably, flood wave propagation velocities reach 2.0–3.5 m s^{−1} due to these topographic conditions. The northwest of the basin is located in the temperate continental climate zone, precipitation is scarce and concentrated in summer; the southeast is located in the temperate monsoon climate zone, with cold, dry winters and hot, rainy summers. The average annual temperature of the basin ranges from 5 to 12 °C, and the average annual runoff is about 480 × 10⁶ m³. The average annual rainfall is about 500 mm, and the spatial and temporal distribution of rainfall within the year is uneven, mainly concentrated from May to September, and the precipitation decreases from south to north. Floods in the basin are mostly formed by heavy rainfall, which is short-lived and strong, making the flooding process steep up and steep down, often causing disasters in the downstream areas. Consequently, accurate flood forecasting is of utmost importance for effective

flood control and water resources management in the Luan River basin. The location of the study area and the stations are shown in Fig. 2.

3.2 Data

The rainfall and runoff data were obtained from the Hydrological Yearbook of the Haihe River Basin, including rainfall data from 15 rainfall stations, such as Sandaohezi, Zhangbaiwan, and Baorono, and runoff data from Sandaohezi hydrological station. The period covers 39 years from 1964 to 1989, 1991, and 2006 to 2017. There is a gap in the data for 1990 and 1992 to 2005 due to incomplete data collection.

The evapotranspiration and soil moisture data were obtained from the Global Land Surface Data Assimilation System (GLDAS) using the GLDAS-Noah model product $0.25^\circ \times 0.25^\circ$ spatial resolution, 3 h temporal resolution dataset, and the evapotranspiration data were averaged backward 3 h, and the soil moisture data were instantaneous values. Among them, GLDAS-2.0 provides data from 1964 to 2014, and GLDAS-2.1 provides data from 2015.

In this study, 30 flood events during the 39 years were selected (Table 1), and the collected observed runoff data were linearly interpolated to 1 h step data, the observed rainfall data were averaged to 1 h step data, and the Tyson polygon method was used to derive the areal rainfall. For evapotranspiration and soil moisture, the average values were calculated for each grid in the watershed at each period, where the soil moisture was taken as the initial soil moisture before the onset of rainfall for each flood event. Twenty flood events were used for model training, ten flood events were used for model validation. The partitioning of training and validation sets was designed to ensure balanced representation of flood characteristics across both datasets, specifically considering temporal occurrence, peak discharge, and flood duration. This stratification achieves comprehensive inclusion of major, moderate, and minor flood magnitudes while encompassing diverse hydrograph types – including both single-peak and multi-peak events – to maintain hydrological process representativeness.

Since different input features have different magnitudes, maximum-minimum normalization was used to process the input data into the range [0, 1], see Eq. (25).

$$x_{\text{norm}} = \frac{x_i - x_{\min}}{x_{\max} - x_{\min}} \quad (25)$$

where x_{norm} is the normalized data, x_i is the original data, and $x_{\min}$ and $x_{\max}$ are respectively the minimum and maximum values of the original data.

3.3 Model construction

This study is based on Python 3.9, and the Numpy, Pandas, and Scikit-Learn packages in Python are used for data processing, and the LSTM, FTA-LSTM, FTMA-LSTM, and

PHY-FTMA-LSTM models are constructed using the Keras library in TensorFlow 2.9.1.

The model inputs are runoff, rainfall, evapotranspiration, and initial soil moisture for a specified time step, and the outputs are the discharge from 1 to 6 h of the lead time. All four models use the ReLU activation function (Nair and Hinton, 2010), which avoids gradient vanishing and is more effective compared to the tanh and sigmoid functions. The Adam optimizer is used and the LSTM layer is a single layer, with the number of attention heads set to 3 for the FTMA-LSTM and PHY-FTMA-LSTM. The mean squared error is the loss function of the four models, and for PHY-FTMA-LSTM it incorporates physical constraints, as shown in Eq. (19). To avoid overfitting, all models employ early stopping based on the mean squared error loss function, with a maximum iteration limit of 200 epochs. The training process automatically terminates if no improvement in loss is observed for 20 consecutive epochs.

To construct the base models, the common values of the DL model parameters are used as the initial values. The base models have an observed input time step of 12 h, a learning rate of 0.001, batch size of 64, and hidden units set to 128. After evaluating the performance of the base models, parameter optimization is performed separately for each of the four models, considering that the optimal parameter combinations may differ among the models. The goal is to study the effects of the input time step and three hyperparameters (learning rate, batch size, and hidden units) on the model performance. The ranges used for parameter optimization are as follows: input time step of 3 to 24 h, learning rate of 0.00001 to 0.01, batch size of 16 to 256, and hidden units of 32 to 512. A single parameter is varied while the other parameters are taken as their initial values. Considering the stochastic nature of the DL model running process, each of the four models is repeated five times for each lead time, and the results with the best prediction performance are selected for analysis.

4 Results

4.1 Model optimization

The LSTM, FTA-LSTM, FTMA-LSTM, and PHY-FTMA-LSTM base models are established individually, and their average NSE values during the 1–6 h lead time, measure to evaluate flood prediction accuracy, are found to be 0.925, 0.930, 0.936, and 0.950, respectively. These results indicate that all four base models can effectively predict flooding events. In order to determine the optimal parameter combination for each model and how individual parameter variations affect the model performance, the following parameters are investigated while keeping the other three parameters constant: input time step, learning rate, batch size, and hidden units.

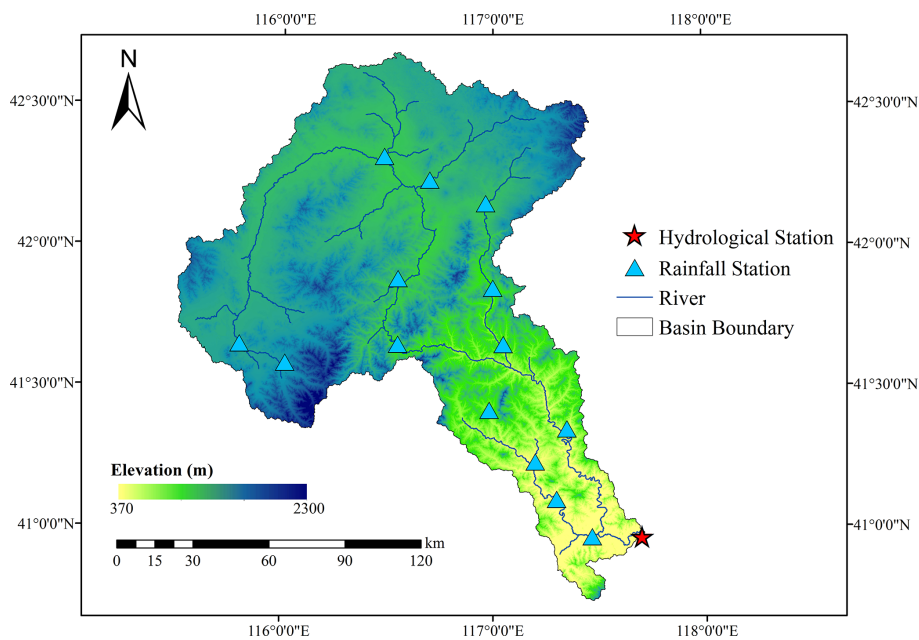


Figure 2. Geographical location of the study area and hydrological and rainfall stations.

Table 1. Flood events used in the study.

Dataset	Flood number	Peak discharge (m ³ s ^{−1})	Year	Duration (month/day/hour)
Training	1	314.2	1964	08/01/04:00–08/09/12:00
	2	218	1964	08/13/02:00–08/16/00:00
	3	313	1965	07/17/20:00–07/21/12:00
	4	204	1966	07/27/16:00–07/31/20:00
	5	260	1968	07/27/12:00–07/30/22:00
	6	154	1969	08/20/12:00–08/27/12:00
	7	296	1971	07/17/15:00–07/29/08:00
	8	153	1972	07/19/08:00–07/24/08:00
	9	742	1973	08/12/04:00–08/26/08:00
	10	213	1975	08/11/00:00–08/16/08:00
	11	218	1978	08/25/12:00–09/03/08:00
	12	246	1982	07/22/12:00–07/29/16:00
	13	313	1983	08/04/00:00–08/11/20:00
	14	400	1985	08/24/05:00–08/31/04:00
	15	210	1986	08/08/04:00–08/13/08:00
	16	87.5	1987	08/19/12:00–08/23/04:00
	17	465	1991	06/10/04:00–06/18/00:00
	18	70.1	2008	08/10/00:00–08/16/00:00
	19	149	2010	07/30/17:00–08/04/20:00
	20	80.4	2015	07/27/16:00–07/31/16:00
Validation	21	241	1965	08/26/21:00–08/30/20:00
	22	260	1967	06/27/12:00–06/29/22:00
	23	164	1970	07/14/12:00–07/16/04:00
	24	506.7	1974	07/23/12:00–08/06/08:00
	25	313	1979	08/13/04:00–08/21/08:00
	26	132	1985	08/11/16:00–08/14/04:00
	27	212	1989	06/03/22:00–06/07/04:00
	28	205	2011	08/14/10:00–08/20/04:00
	29	95.9	2013	07/21/08:00–07/25/16:00
	30	84.2	2013	08/13/09:00–08/21/00:00

Regarding the input time step of observations, experiments are conducted by varying the time step within a certain range. The result depicted in Fig. 3a shows that the average NSE value for all four models is highest at a time step of 12 h and decreases with increasing time step. The worst performance is observed at a time step of 24 h. This observation suggests that longer input sequences introduce more noise, and the inclusion of extraneous information adversely affects the final prediction. Therefore, a 12 h input time step is identified as the optimal choice for flood forecasting in all four models and is adopted for subsequent experiments. The samples are constructed through a sliding window, resulting in the generation of 2859 training samples and 1166 validation samples.

For the learning rate, tests are performed using a learning rate ranging from 0.00001 to 0.01. The finding, presented in Fig. 3b, indicates that the performance of the four models is comparable at learning rates of 0.01 and 0.001. However, when the learning rate is set to 0.0001 and 0.00001, the models exhibit slow convergence and degrade performance rapidly. Considering the possibility of failure to converge at a very high learning rate, a combined analysis suggests a learning rate of 0.001 as the optimal choice for all four models in the subsequent studies.

The batch size optimization ranges from 16 to 256. The result depicted in Fig. 3c demonstrates varying performances of the four models with different batch sizes. The LSTM model achieves the highest average NSE of 0.932 at a batch size of 128. Similarly, the FTA-LSTM model attained its highest average NSE of 0.932 at a batch size of 32. On the other hand, the FTMA-LSTM and PHY-FTMA-LSTM models reach their highest average NSE values at a batch size of 64, with 0.936 and 0.950, respectively. Consequently, the optimal batch size for flood forecasting is determined as 128, 32, 64, and 64 for the LSTM, FTA-LSTM, FTMA-LSTM, and PHY-FTMA-LSTM models, respectively. These batch sizes are employed for subsequent studies.

Regarding the hidden units, tests are conducted with the count varying from 32 to 512. Figure 3d illustrates the distinct performances of the four models concerning different hidden units. The LSTM model achieves the highest average NSE of 0.925 with 64 hidden units. The FTA-LSTM and FTMA-LSTM models attain their highest average NSE values of 0.935 and 0.939 with 256 hidden units, respectively. In contrast, the PHY-FTMA-LSTM model reaches the highest average NSE of 0.950 at 128. Accordingly, the optimal hidden units for flood prediction are identified as 64, 256, 256, and 128 for the LSTM, FTA-LSTM, FTMA-LSTM, and PHY-FTMA-LSTM models, respectively.

Considering the above parameter optimization process, the model parameters used in the subsequent study are as follows (Table 2). Notably, the PHY-FTMA-LSTM model consistently outperforms the other three models across various parameter values, exhibiting the smallest variation in NSE. These findings indicate that the PHY-FTMA-LSTM model

Table 2. Parameters of models.

Models	Input time step	Learning rate	Batch size	Hidden units
LSTM	12	0.001	128	64
FTA-LSTM	12	0.001	32	256
FTMA-LSTM	12	0.001	64	256
PHY-FTMA-LSTM	12	0.001	64	128

proposed in this paper offers the best and most stable performance.

4.2 Model performance evaluation

The LSTM, FTA-LSTM, FTMA-LSTM, and PHY-FTMA-LSTM models are constructed using the optimal parameters mentioned above, the evaluation metrics of the forecasting performance of the four models in the training and validation periods are shown in Figs. 4 and 5. Detailed metrics data can be found in the Supplement (Tables S1 and S2). All the metrics of the four models almost outperform the validation period in the training period. And with the increase of the lead time, the gap between the performance of the models in the training period and the testing period gradually increases. It can be seen that the three models based on the attention mechanism outperform the original LSTM model in all lead times. It indicates that the dual attention module of time and feature proposed in this paper effectively focuses on the more significant historical moments and feature variables, improving the performance of the LSTM model. Among the attention-based models, the FTMA-LSTM model, which utilizes a multi-headed attention mechanism, achieves better performance than the FTA-LSTM model with a single attention head in most cases. This demonstrates that the parallel computation of the multi-head attention mechanism enables the model to emphasize more important information in the input compared to the single-head attention mechanism. Furthermore, the PHY-FTMA-LSTM model, which incorporates physical constraints, outperforms the other three models across almost all metrics. Specifically, at the lead time $t + 1$, compared to the original LSTM model, the PHY-FTMA-LSTM model shows an improvement in NSE, KGE, and R^2 , increasing from 0.977 to 0.988, from 0.953 to 0.984 and from 0.979 to 0.988, respectively. Additionally, the RMSE and MAE decrease by 27.4 % and 49.6 %, respectively. At the lead time $t + 6$, NSE increases from 0.865 to 0.908, KGE from 0.851 to 0.905, R^2 from 0.886 to 0.911, and RMSE and MAE decrease by 21.1 % and 15.1 %, respectively. These results mean that incorporating physical constraints enables the DL model to understand the monotonic relationship presented in the flooding process, improving forecast accuracy by enhancing the model's physical consistency.

As the lead time increases, the performance of all four models declines, suggesting that their robustness and gen-

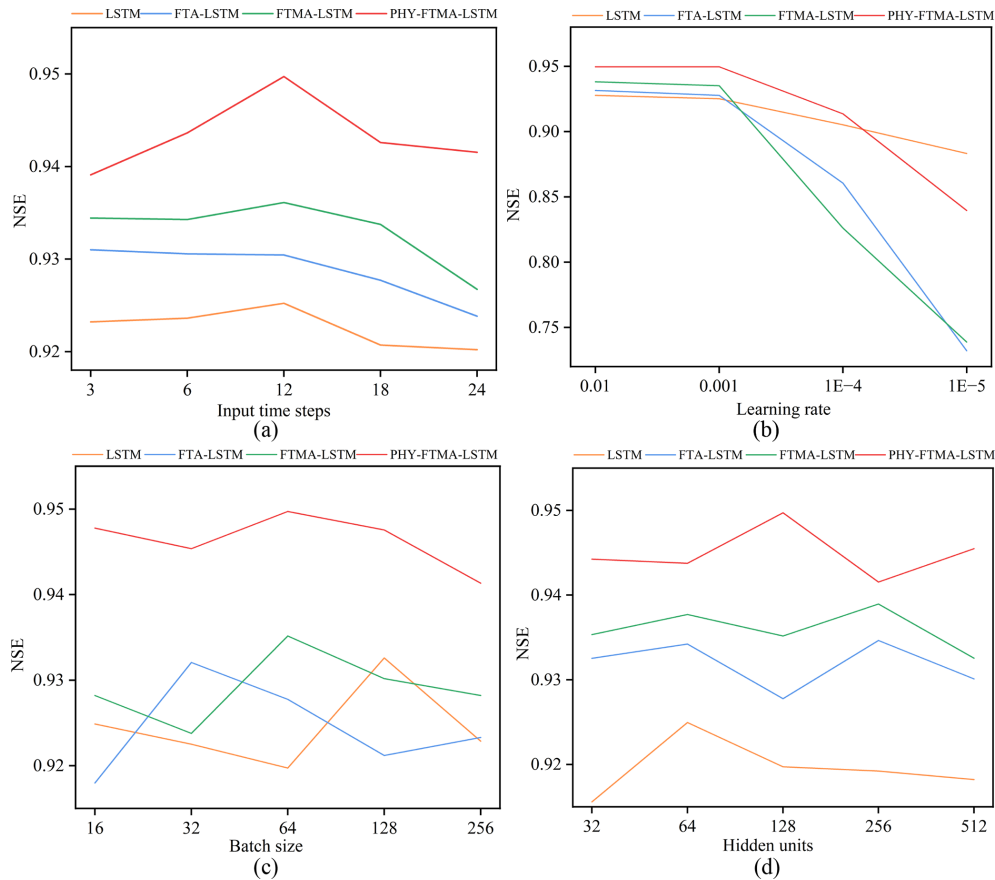


Figure 3. The NSE values for 6 lead times with different (a) Input time steps of observations, (b) Learning rate, (c) Batch size, and (d) Hidden units.

eralization gradually deteriorate. However, the extent of the decline in the four model metrics varies. In terms of NSE, when transitioning from a 1 to a 6 h lead time, the PHY-FTMA-LSTM model exhibits the smallest decline of 0.065 during the training period, while the LSTM, FTA-LSTM, and FTMA-LSTM models experience decreases of 0.072, 0.079, and 0.073 respectively. During the validation period, the NSE value decreases by 0.080 for the PHY-FTMA-LSTM model and by 0.112, 0.109, and 0.104 for the LSTM, FTA-LSTM and FTMA-LSTM models, respectively. Maintaining high accuracy in longer lead times is crucial in practical applications. Extended lead times necessitate more comprehensive information for accurate predictions, presenting challenges for the models. Nonetheless, the PHY-FTMA-LSTM model exhibits minimal degradation, indicating its superior ability to adapt to longer lead times and maintain high precision. This superiority may be attributed to the unique characteristics and structure of the PHY-FTMA-LSTM model. It likely encompasses considerations of physical factors and key input features, enabling a better capture of flood complexity and variability. This advantage positions the model favorably in scenarios requiring predictions further into the future.

Figure 6 displays the scatter plots for the LSTM, FTA-LSTM, FTMA-LSTM, and PHY-FTMA-LSTM models during the training and validation periods. When the foresight period is 1 h, all models demonstrate predictions that closely track the ideal 1 : 1 line. The PHY-FTMA-LSTM model outperforms the others, exhibiting the narrowest scatter distribution. However, as the lead time increases, the scatter plots of the four models show varying degrees of deterioration, becoming more uneven and scattered. The high discharge prediction error increases in the training period, and the validation period reveals numerous underestimated discharges. Among them, the PHY-FTMA-LSTM model performs the best (with the narrowest scatter distribution), followed by the FTA-LSTM and FTMA-LSTM models. The LSTM model performs the worst. Notably, during the validation period, for longer foresight periods, the high flow scatter of all models deviates further from the ideal 1 : 1 line. One possible explanation is the scarcity of high flow instances in the training data. As the lead time increases, the models struggle to capture the necessary information, leading to underestimation and poorer predictions. For a foresight period of 6 h, the scatter plots of the LSTM, FTA-LSTM, and FTMA-LSTM models both in the training and validation periods exhibit discrete

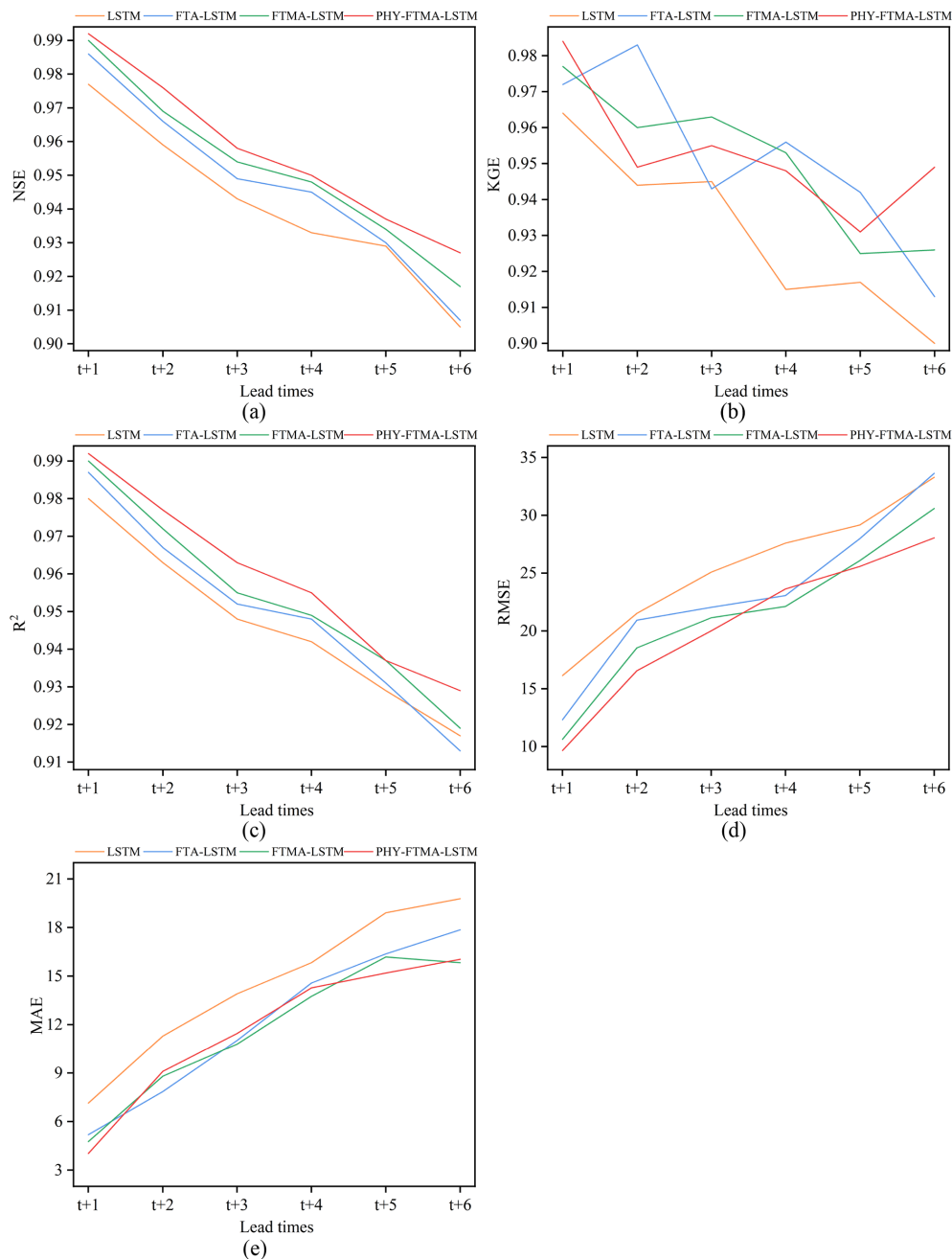


Figure 4. Performance of the four models for flood forecasting at different lead times for training (a) NSE, (b) KGE, (c) R^2 , (d) RMSE, and (e) MAE.

distributions. In contrast, the PHY-FTMA-LSTM model's scatter plot shows the narrowest band and is closest to the ideal 1 : 1 line. Consequently, the PHY-FTMA-LSTM model achieves the highest prediction accuracy, effectively reducing prediction errors for longer lead times. The FTA-LSTM and FTMA-LSTM models follow while the LSTM model performs the worst in terms of prediction accuracy.

4.3 Typical flood event forecast results

Floods in the basin are mainly two types, single-peak and double-peak, so two typical flood events were selected to analyze the specific flood process: a double-peak flood event (19740723) with a peak discharge of 507 and 290 $\text{m}^3 \text{s}^{-1}$, and a single-peak flood event (19790813) with a peak discharge of 313 $\text{m}^3 \text{s}^{-1}$. Figures 7 and 8 illustrate the flood processes of the two events predicted by the four models. It can

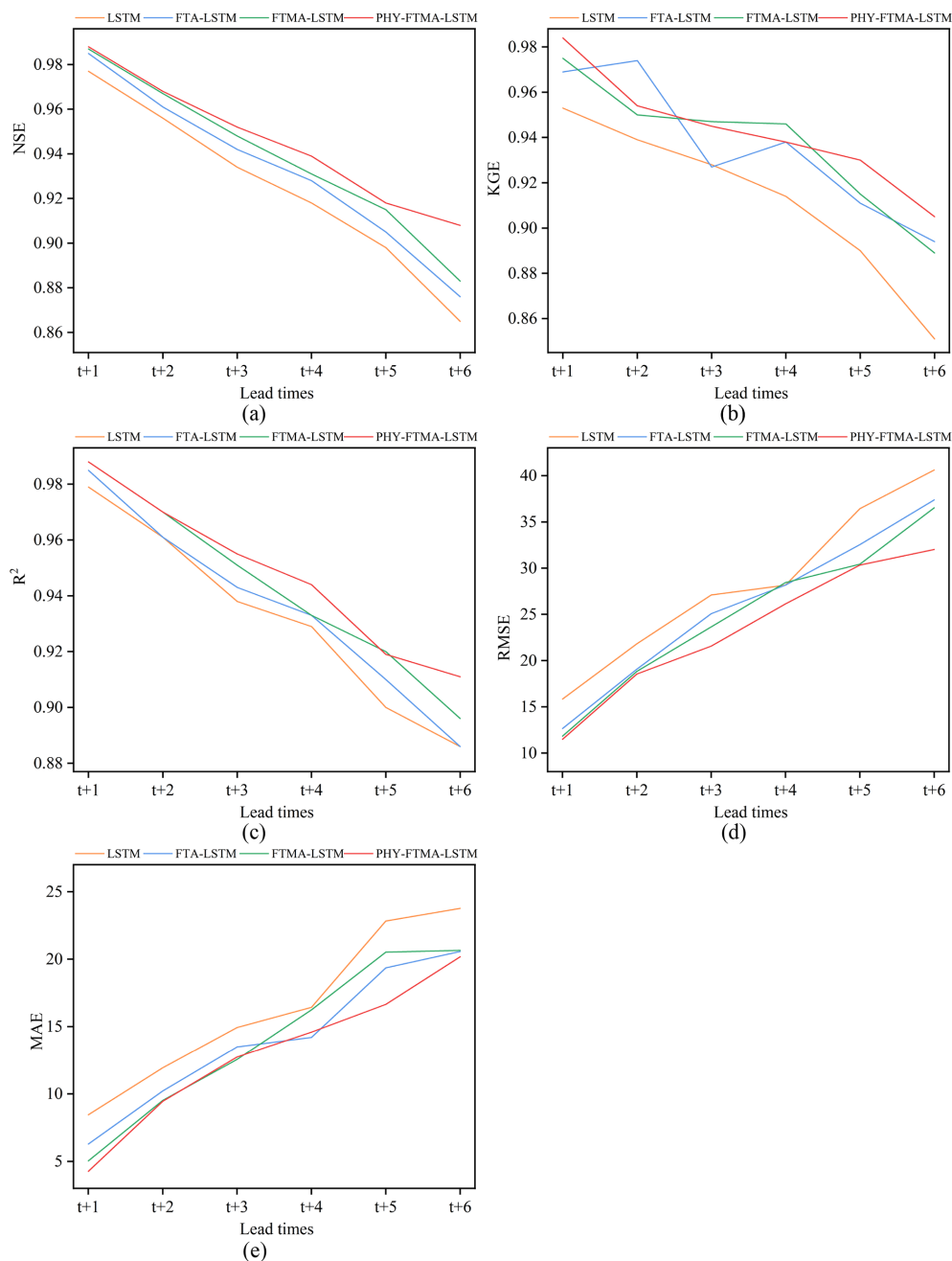


Figure 5. Performance of the four models for flood forecasting at different lead times for validation (a) NSE, (b) KGE, (c) R^2 , (d) RMSE, and (e) MAE.

be observed that as the lead time increases, the prediction hydrographs from all four models gradually deviate from the observed values and the three evaluation metrics decrease. Notably, the LSTM model exhibits the greatest decline in prediction performance, followed by the FTA-LSTM and FTMA-LSTM models. In contrast, the PHY-FTMA-LSTM model demonstrates relatively better performance across the evaluated flood events.

Based on the analysis of prediction hydrographs, the four models exhibit better performance in predicting the double-peak flood event compared to the single-peak flood event. Additionally, the models demonstrate higher accuracy in predicting the rising stage of floods in contrast to the falling stage. Specifically, the prediction errors increase as the duration of the flood increases, and there is a time lag in predicting the occurrence of the second flood peak. When it comes to the single-peak flood event, the predictions by the four

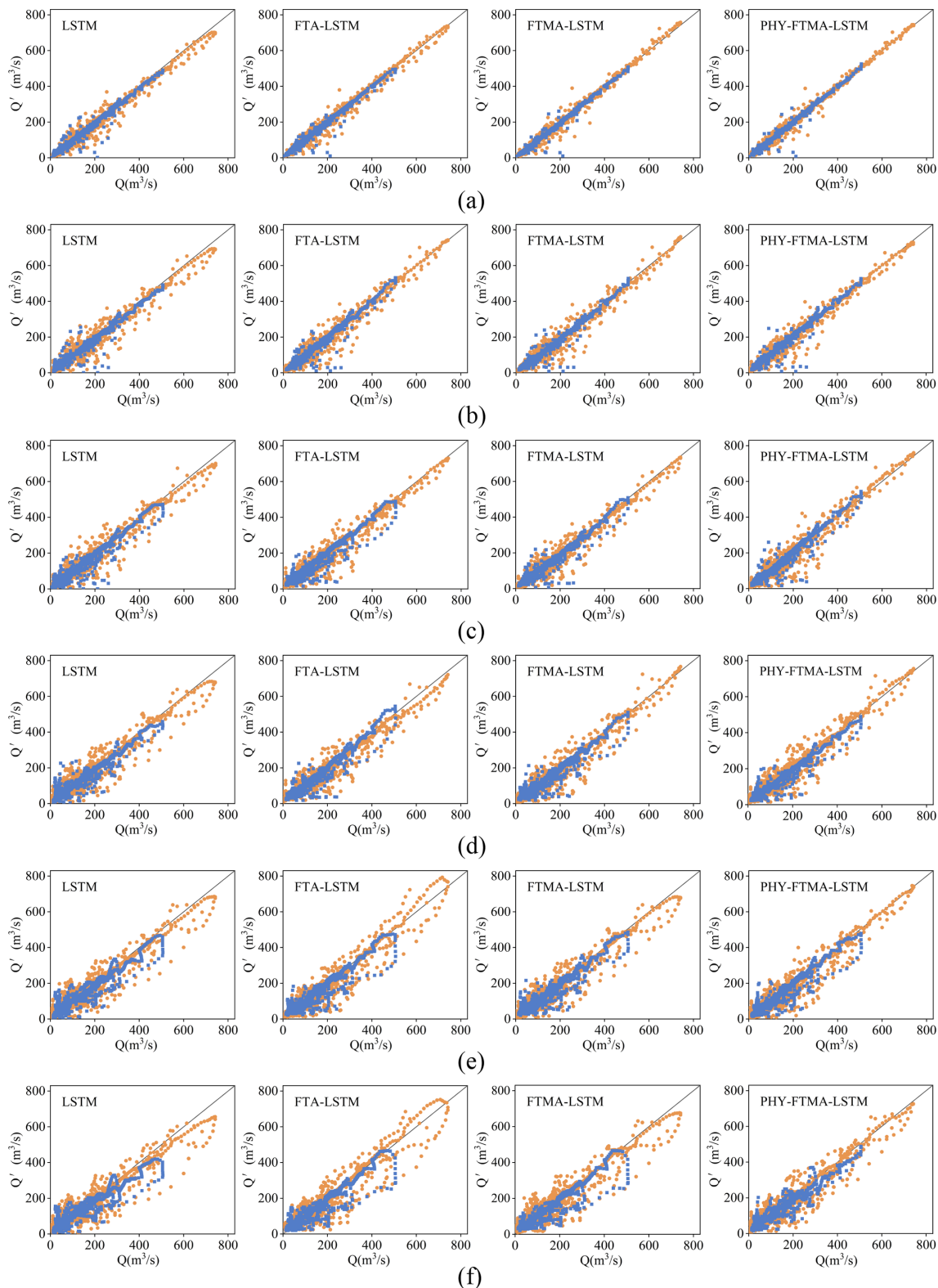


Figure 6. Scatter plots of observed and predicted discharges in the training and validation periods (a) $t + 1$, (b) $t + 2$, (c) $t + 3$, (d) $t + 4$, (e) $t + 5$, and (f) $t + 6$, in which yellow represents the training period and blue represents the validation period.

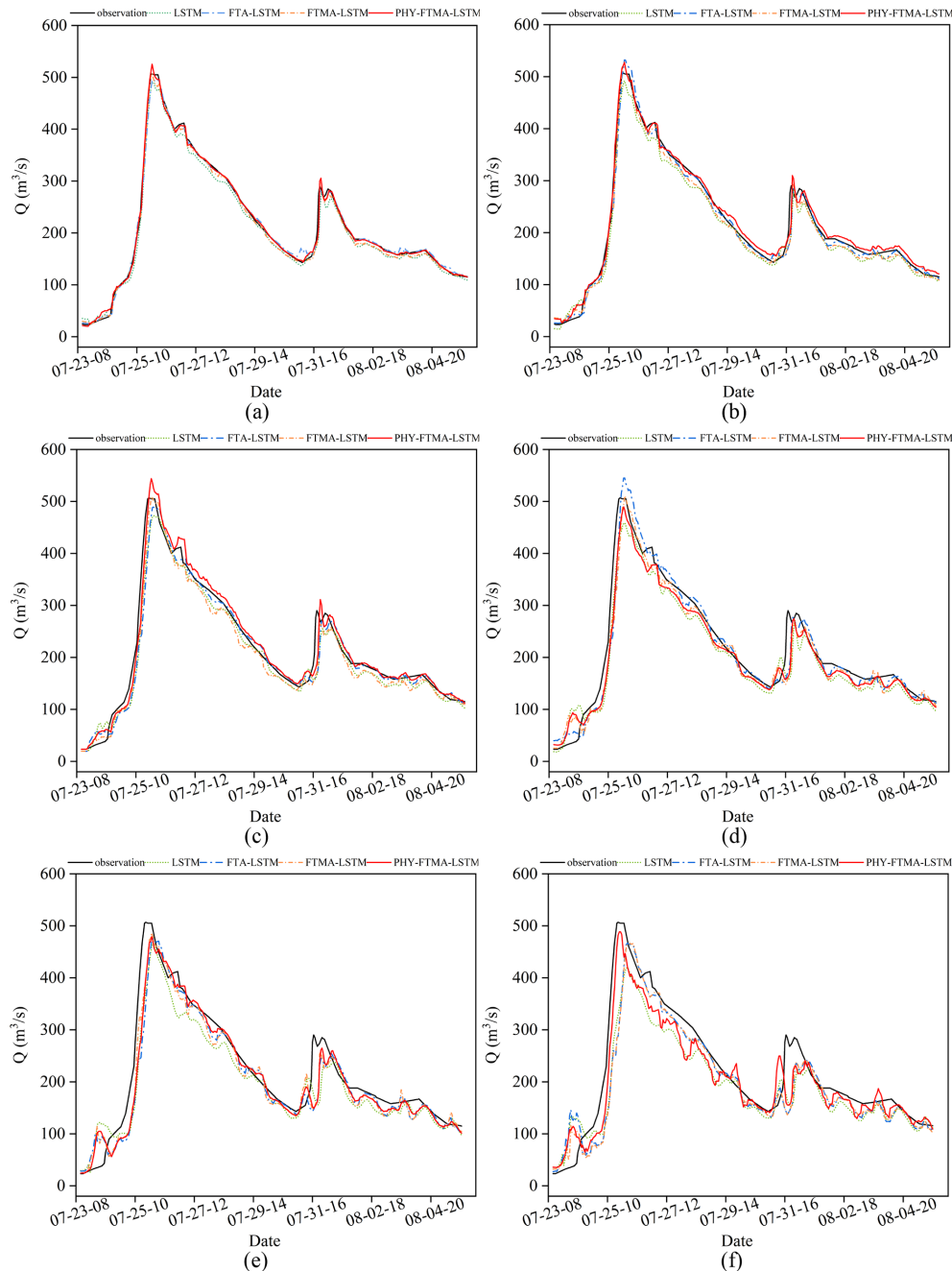


Figure 7. Comparison of observed and predicted values of the 19740723 flood event by the four models (a) $t + 1$, (b) $t + 2$, (c) $t + 3$, (d) $t + 4$, (e) $t + 5$, and (f) $t + 6$ (The x axis displays dates in MM-DD-HH format, representing month, day, and hour respectively).

models display greater fluctuations, and the time lag problem is more pronounced, along with an overestimation of the peak discharge.

Regarding the 19740723 flood event, the LSTM model generally underestimates the discharge values, and the discrepancy with the observed hydrograph gradually increases as the lead time increases. Although the FTA-LSTM and FTMA-LSTM models also underestimate the discharge, their errors are reduced, indicating improved performance com-

pared to the LSTM model. In contrast, the PHY-FTMA-LSTM model predicts the flood hydrograph more accurately. However, when the foresight period is 6 h, the PHY-FTMA-LSTM model experiences significant prediction errors due to anomalous fluctuations.

For the 19790813 flood event, the LSTM model demonstrates a noticeable deviation from the predicted hydrograph with increasing lead times. The FTA-LSTM and FTMA-LSTM models exhibit better performance, as their predicted

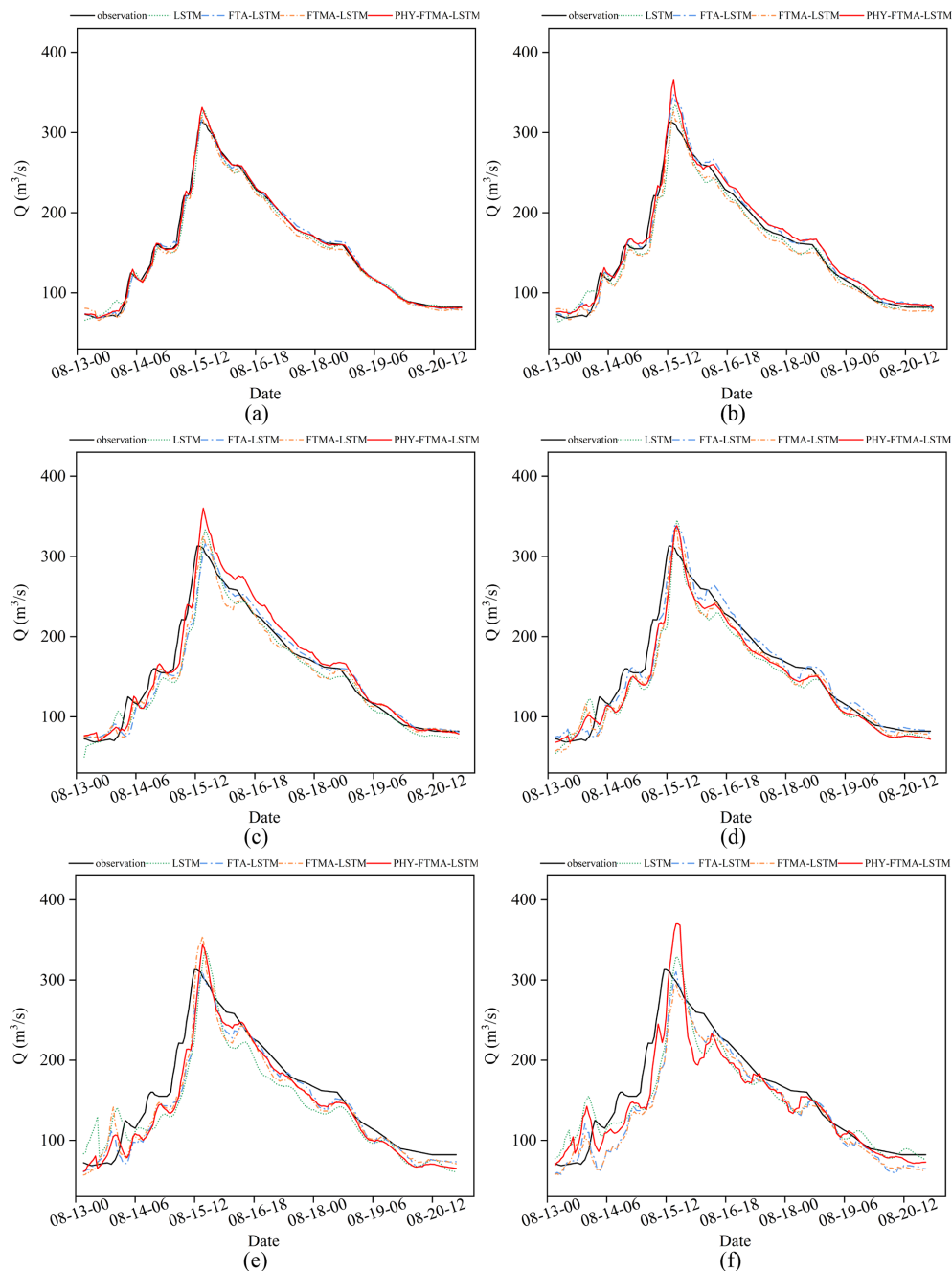


Figure 8. Comparison of observed and predicted values of the 19790813 flood event by the four models (a) $t + 1$, (b) $t + 2$, (c) $t + 3$, (d) $t + 4$, (e) $t + 5$, and (f) $t + 6$.

hydrographs are closer to the observed ones. However, there is some overestimation of the peak discharge in these models. Additionally, all three models suffer from a more severe time lag issue in longer foresight periods. In contrast, the PHY-FTMA-LSTM model shows smaller volume errors and is closer to the observed hydrograph. Nevertheless, this model exhibits a more pronounced overestimation of the peak discharge.

In conclusion, the LSTM model exhibits poor prediction performance for longer lead times. On the other hand, the FTA-LSTM, FTMA-LSTM, and PHY-FTMA-LSTM models show improved performance with longer lead times and higher forecasting accuracy. Among these models, the PHY-FTMA-LSTM model stands out by producing better predictions for both single-peak and multi-peak flood events, but it may encounter challenges with predicting anomalous fluctuations at longer lead times. Additionally, the PHY-FTMA-

LSTM model mitigates the issue of time lag to some extent by considering the physical monotonicity relationship.

4.4 Visual attention analysis

To investigate the changes in features and time attention of PHY-FTMA-LSTM with different lead times, the attention weights of PHY-FTMA-LSTM are visualized in Fig. 9. The figure consists of six subplots representing lead times ranging from $t + 1$ to $t + 6$.

From Fig. 9, it can be observed that the distribution pattern of the weights remains relatively similar across different forecasting periods. The temporal attention weights decrease as the historical moment increases. Among the feature-based weights, runoff has the highest proportion, followed by rainfall, and finally the initial soil moisture and evapotranspiration. These results align with hydrological principles, where runoff is considered the most direct manifestation of the flooding process and holds the highest importance. Rainfall, as the main driver of flood formation, significantly influences flooding. In contrast, the effects of initial soil moisture and evapotranspiration in the basin are more indirect and therefore receive lower weights. In the case of the Luan River basin, which is relatively arid, the initial soil moisture of the basin is typically not saturated. During a rainfall-induced flood, there is a possibility of transitioning from infiltration-excess runoff to saturation-excess runoff. Hence, special attention should be given to the role of the initial soil moisture, which carries slightly greater relative importance than evapotranspiration.

As the forecasting horizon extends, the feature-time-based weights of the model become more concentrated, with the time-based weights gradually moving forward. Consequently, the model places more emphasis on the values that are closer to the current moment. Additionally, the feature-based attention module exhibits a gradual increase in attention to rainfall while decreasing attention to evapotranspiration and the initial soil moisture. Notably, runoff retains its status as the most influential factor.

5 Discussion

The input time step of observations, learning rate, batch size, and hidden units are significant parameters that influence the performance of the model, and the optimal parameters may vary for different structural models (Xiang et al., 2020; Cao et al., 2022). In this study, four models, namely LSTM, FTA-LSTM, FTMA-LSTM, and PHY-FTMA-LSTM, have been constructed. To ensure that each model achieves its optimal prediction performance and to investigate the impact of different parameter variations on model performance, the same parameter values are utilized to build the four base models individually. After confirming that the base models meet the accuracy requirements for flood forecasting, the optimal pa-

rameter combination for each model is determined. This is done by selecting the parameter value associated with the highest NSE obtained through single parameter tuning. The single parameter is changed while keeping the initial values of the other three parameters constant. This approach ensures that the subsequent analysis reflects the best performance achievable by each model's specific structure. Moreover, it enables a more explicit evaluation of the performance changes resulting from the addition of attention mechanisms and physical constraints to the model.

In terms of model performance evaluation metrics, the PHY-FTMA-LSTM model demonstrates the best overall performance. However, a closer examination reveals that its KGE score may not necessarily be optimal. This could be attributed to the comprehensiveness of the KGE metric, which considers factors such as correlation, mean consistency, and variance consistency of the flow. Fluctuations in the KGE score may arise from various uncertainties related to data quality, model structure, and flood forecasting.

With an increase in the forecast period, the performance of the model, particularly the LSTM model, shows a significant decrease, consistent with the findings reported by Xu et al. (2021). They provided NSE, RMSE, and Bias indices for the LSTM model in forecast periods of 1–12 h, demonstrating that the LSTM model meets prediction requirements for short forecast periods. However, as the forecast period extends, the accuracy diminishes, leading to underestimation of flood peaks and significant fluctuations. Similar conclusions were drawn in the studies conducted (Cui et al., 2021; Ding et al., 2020). The longer the foresight period, the lower the correlation between input and output variables. The models face increased difficulty due to the lack of future information and the challenges associated with flood forecasting.

The addition of an attention mechanism effectively enhances the accuracy of flood forecasting in the original LSTM model. As the lead time increases, the temporal weights gradually shift forward, causing the model to pay greater attention to values closer to the current moment. This finding aligns with the conclusions of studies on temporal attention conducted by Ding et al. (2020) and Wang et al. (2023). However, there is a difference between their studies and the current one, as they incorporated a spatial attention module to focus on the relevance of spatial locations, while this study introduces a feature attention module to highlight the importance of different input features in flood forecasting.

Incorporating physical constraints into the model enhances the understanding of the monotonic relationships between variables in the flooding process and improves the physical consistency of the model. This study considers the monotonic relationships between rainfall, evapotranspiration, initial soil moisture, and runoff in the watershed. In a study by Xie et al. (2021), three physical conditions related to the rainfall-runoff forecasting process were encoded into the loss function at the daily scale. Experimental re-

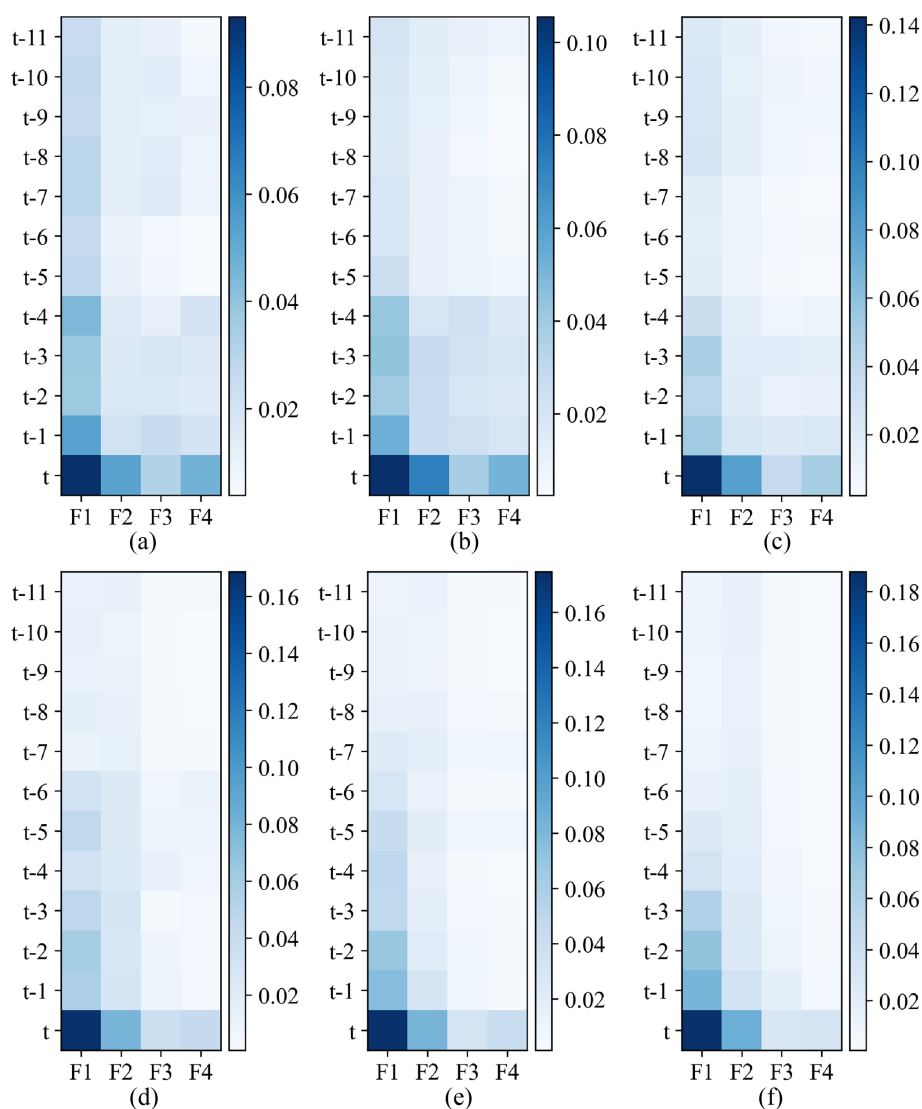


Figure 9. The visualization of feature-time-based attention weights of the PHY-FTMA-LSTM (a) $t + 1$, (b) $t + 2$, (c) $t + 3$, (d) $t + 4$, (e) $t + 5$, and (f) $t + 6$ (The X coordinate variables F1 to F4 represent the input features of runoff, rainfall, evapotranspiration, and initial soil moisture of the watershed, respectively. The Y coordinate variables represent the input history moments).

sults on 531 watersheds in the CAMELS dataset showed that the model achieved an improvement from 0.52 to 0.61 in the NSE mean compared to the LSTM model. In this study, flood forecasting is performed at a finer time scale, specifically at the hourly scale, and additional monotonic relationship constraints between evapotranspiration, initial soil water content, and runoff are incorporated.

Notably, across all forecast periods – particularly at $t + 5$ and $t + 6$ – scatterplot points (Fig. 6) exhibit deviant behavior forming curve patterns for discharge values exceeding approximately $300 \text{ m}^3 \text{ s}^{-1}$. The analysis reveals that the outliers primarily cluster during the 19740723 flood event, mainly attributable to training dataset limitations. This extreme event featured both an exceptionally prolonged duration and high peak discharge – characteristics absent from the

training data. Consequently, the model demonstrates insufficient capacity to simulate such threshold-exceeding events, yielding suboptimal performance. However, as this represents an extreme scenario, model accuracy is expected to improve with expanded data accumulation.

Furthermore, the dataset was partitioned solely into training and validation sets primarily due to limitations in available historical flood events – only 30 events were utilized, most with relatively short durations. This resulted in a limited sample size and insufficient additional floods for model testing; future data acquisitions will be incorporated to enhance robustness. To maximize coverage of flood diversity and capture spatiotemporal heterogeneity, we partitioned data based on temporal occurrence, peak discharge, and flood duration. This methodology follows established precedents (e.g., Lv

et al., 2020; Read et al., 2019; Xie et al., 2021; Jiang et al., 2020) where dual-set partitioning is widely adopted beyond flood forecasting applications. Crucially, our results are contingent upon the specific flood event partitioning of training and validation sets detailed in Table 1, with no investigation of alternative partitioning impacts. Future research could employ cross-validation or bootstrapping to evaluate model robustness and stability across different dataset divisions.

Flood forecasting is challenged by various complex factors such as meteorological conditions and rainfall patterns, and the uncertainty of these factors increases over time (Cheng et al., 2021; Hu et al., 2019). Consequently, the models are prone to significant prediction errors. When the forecast period extends to 6 h, each model exhibits a significant deviation from the observed hydrograph and more anomalous fluctuations. While our framework currently caps at 6 h predictions, extending this horizon requires confronting two fundamental constraints: (1) Input deficiency: The absence of real-time meteorological forecasts prevents runoff anticipation prior to precipitation; (2) Structural saturation: Memory decay in recurrent units limits long-range dependency capture. To address current limitations, future research will pursue a dual-track improvement strategy: Near-term efforts will focus on implementing error correction techniques, specifically K-nearest neighbors (KNN) and backpropagation (BP) algorithms, coupled with advanced data assimilation methods such as Ensemble Kalman and Particle filters to enhance real-time forecasting accuracy. While more fundamental enhancements will involve the strategic integration of numerical weather prediction inputs – specifically the European Centre for Medium-Range Weather Forecasts (ECMWF) and China Meteorological Administration Global Forecast System (CMA-GFS) datasets – to enable pre-rainfall runoff anticipation and systematically extend predictive lead times beyond the current 6 h threshold. Thereby addressing both immediate performance gaps and long-term capability requirements in flood forecasting.

6 Conclusions

This research introduces a DL model called PHY-FTMA-LSTM, which combines feature-time-based multi-head attention mechanisms with physical constraints. The primary aim is to explore how incorporating interpretability and physical constraints into DL models affects flood forecasting accuracy. The evaluation of the flood forecasting results from 1 to 6 h during the foresight period in the Luan River basin yields the following conclusions:

1. The attention mechanism that considers both features and time effectively enhances the model's prediction performance, surpassing that of the original LSTM model. The FTMA-LSTM model, equipped with an increased number of attention heads, further improves accuracy by considering more information through par-

allel computation. Taking the integration of physical constraints into account, the PHY-FTMA-LSTM model achieves the best performance, exhibiting stable results. For a lead time of $t + 1$, the NSE, KGE, R^2 , RMSE, and MAE reaches 0.988, 0.984, 0.988, 11.50, and 4.26, respectively. Additionally, NSE, KGE, and R^2 also could reach 0.908, 0.905, and 0.911 for a lead time of $t + 6$.

2. The incorporation of a feature-time-based multi-head attention mechanism improves interpretability by directing attention to the most valuable features and historical moments within the inputs. The weight matrix visualization reveals that runoff emerges as the most influential feature in flood forecasting, followed by rainfall, and finally initial soil moisture and evapotranspiration. Furthermore, the weight distribution becomes more concentrated with increasing lead time.
3. The model combines physical constraints by considering the monotonic relationships between rainfall, evapotranspiration, initial soil moisture, and runoff at an hourly scale. This augmentation significantly improves the model's predictive capacity for flood processes, including flood peaks, while reducing the lag time.

In this study, we have successfully incorporated both the attention mechanism and physical mechanism into a DL model to improve the accuracy of flood prediction while ensuring interpretability and physical consistency. While our current framework demonstrates strong performance within 6 h predictions, we recognize two key constraints for extending this horizon: the input deficiency due to missing real-time meteorological forecasts and the structural saturation caused by memory decay in recurrent units. To address these limitations, future research will provide improvements through error correction techniques and data assimilation, as well as fundamental enhancements through the integration of ECMWF/CMA-GFS numerical weather prediction inputs to enable pre-rainfall runoff prediction and extend the forecast period beyond 6 h. Additionally, we suggest exploring other interpretation techniques to deepen understanding of the model's decision-making, while expanding the physical-DL integration through more detailed basin subsurface information and novel combination methods.

Code and data availability. The rainfall and flood data and model codes used in this study are available at https://github.com/zran1/PHY_FTMA_LSTM (last access: 13 October 2025) (<https://doi.org/10.5281/zenodo.17337746>, Zhang, 2025). The evapotranspiration and initial soil moisture data are extracted from the GLDAS Noah Land Surface Model (Beaudoin and Rodell, 2019; D. Beaudoin and Rodell, 2020), which is freely available at <https://disc.gsfc.nasa.gov/datasets> (last access: 13 October 2025).

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Author contributions. TZ: Conceptualization, Methodology, Writing-original draft, Writing – review and editing. RZ: Conceptualization, Methodology, Software, Validation, Writing – original draft. JL: Validation, Writing – review and editing. PF: Validation, Writing – review and editing.

Competing interests. The contact author has declared that none of the authors has any competing interests.

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