



Heavy-tailed flood peak distributions: what is the effect of the spatial variability of rainfall and runoff generation?

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Abstract. The statistical distributions of observed flood peaks often show heavy-tailed behaviour, meaning that extreme floods are more likely to occur than for distributions with an exponentially receding tail. Falsely assuming light-tailed behaviour can lead to an underestimation of extreme floods. Robust estimation of the tail is often hindered due to the limited length of time series. Therefore, a better understanding of the processes controlling the tail behaviour is required. Here, we analyse how the spatial variability of rainfall and runoff generation affects the flood peak tail behaviour in catchments of various sizes. This is done using a model chain consisting of a stochastic weather generator, a conceptual rainfall-runoff model, and a river routing routine. For a large synthetic catchment, long time series of daily rainfall with varying tail behaviours and varying degrees of spatial variability are generated and used as input for the rainfall-runoff model. In this model, the spatial variability and mean depth of a sub-surface storage capacity are varied, affecting how locally or widely saturation excess runoff is triggered. Tail behaviour is characterized by the shape parameter of the generalized extreme value (GEV) distribution. Our analysis shows that smaller catchments tend to have heavier tails than larger catchments. For large catchments especially, the GEV shape parameter of flood peak distributions was found to decrease with increasing spatial rainfall variability. This is most likely linked to attenuating effects in large catchments. No clear effect of the spatial variability of the runoff generation on the tail behaviour was found.

1 Introduction

Extreme floods often come as a surprise, and many examples of surprising floods can be found in the literature (Merz et al., 2015). This is partly because of the low occurrence probability of extreme floods. Human intuition tends to expect light-tailed behaviour (Taleb, 2007), and this would mean that extremes are very unlikely. However, when a distribution is heavy-tailed rather than light-tailed, the occurrence probability of extreme flood events is much higher. The upper tail of a distribution is called heavy when it decreases more slowly than exponentially, indicating that the occurrence of extremes is more likely than for an exponentially receding tail (El Adlouni et al., 2008; Papalexiou and Koutsoyiannis, 2013). One example is the surprising and devastating flood that happened in the Ahr Valley in western Germany in summer 2021. The flood peak distribution which was used to derive flood hazard maps before the 2021 event was almost light-tailed, suggesting an extremely low occurrence probability (return period > 1 million years) of floods of the magnitude of the 2021 event. However, considering historical floods in the same area results in a flood peak distribution that is extremely heavy-tailed (Vorogushyn et al., 2022). In fact, many streamflow and precipitation time series exhibit heavy-tailed behaviour (Bernardara et al., 2008; Farquharson et al., 1992; Smith et al., 2018; Villarini et al., 2011).

To quantify the tail heaviness of a distribution, different indices exist (Wietzke et al., 2020). One that is frequently used in hydro-meteorological studies is the shape parameter of the generalized extreme value (GEV) distribution. The GEV distribution is the asymptotic distribution of independent block

maxima (Fisher and Tippett, 1928) and is widely accepted as a suitable distribution for annual maximum series. When the shape parameter of a GEV distribution is larger than 0, the distribution is considered to be heavy-tailed (El Adlouni et al., 2008). The estimation of the upper-tail behaviour is however associated with high uncertainties as it is sensitive to the few largest events (Merz and Blöschl, 2009). This is especially true for the short observational time series that are typically available. Possible ways of achieving more robust estimations of the tail behaviour can be regionalization approaches, the inclusion of historical floods, the simulation of long time series, and the improvement of the understanding of processes that control the tail behaviour (e.g. Merz and Blöschl, 2005; Vorogushyn et al., 2022; Macdonald et al., 2024).

Several studies have addressed the potential controls of heavy-tailed behaviour and related characteristics of flood peak distributions (Merz et al., 2022). These range from data-based approaches (e.g. Macdonald et al., 2022; Thorarinsdottir et al., 2018; Villarini and Smith, 2010) to model-based approaches (e.g. Struthers and Sivapalan, 2007; Rogger et al., 2013; Macdonald et al., 2024) and review studies (e.g. Merz et al., 2022). While some of the studies looked specifically at indicators of tail behaviour like the GEV shape parameter (e.g. Macdonald et al., 2024; Villarini and Smith, 2010), others considered the entire flood frequency curve (e.g. Struthers and Sivapalan, 2007; Rogger et al., 2013) or flood skewness (McCuen and Smith, 2008; Merz and Blöschl, 2009).

In their review, Merz et al. (2022) formulated nine hypotheses on the influence of atmospheric, catchment, and river network factors on flood peak tail behaviour. Previous studies linked characteristics of rainfall (Gaume, 2006), runoff generation (Macdonald et al., 2022), and catchment characteristics such as size (Villarini and Smith, 2010) or aridity (Farquharson et al., 1992) to the tail behaviour of flood peak distributions. Rainfall characteristics and runoff generation processes especially have been found to be relevant, and their influence on the tail behaviour is closely interlinked (McCuen and Smith, 2008; Macdonald et al., 2024). Macdonald et al. (2024) concluded that, for both aspects, i.e. rainfall generation and runoff generation, the spatial structure can strongly affect flood peak generation and should therefore also be considered in the context of flood peak tail behaviour.

For small homogeneous catchments, Macdonald et al. (2024) found that the rainfall tail dominates the flood peak tail beyond a certain return period. Similarly, Gaume (2006) stated that the statistical properties of rainfall asymptotically control the shapes of flood peak distributions. However, it is not clear from those studies whether this also holds for spatially variable rainfall. Using simulation-based approaches, it has been found that the influence of rainfall spatial variability on floods increases with return periods (Peleg et al., 2017; Zhu et al., 2018). This indicates that it might also affect the tail behaviour. Haberlandt and Radtke (2011) found

differences in derived flood probabilities when different degrees of spatial rainfall variability (uniform vs. random) were used to force a hydrological model. While they do not state a clear impact of rainfall spatial variability on flood peak tail behaviour, their Fig. 4b suggests a heavier tail for spatially uniform rainfall than for variable rainfall. In contrast, Wang et al. (2023) concluded, based on simulations for five catchments in Germany, increasing spatial variability of rainfall results in heavier tails of flood peak distributions beyond a certain degree of variability. They argued that spatially variable rainfall creates more opportunities for partial saturation excess because the soil moisture becomes more heterogeneous than with spatially uniform rainfall. So, on the one hand, spatially variable rainfall could lead to more variability in resulting flood flows and a higher chance of floods that are significantly larger than the bulk of the events, which would make a heavy-tailed distribution likely. On the other hand, spatially variable rainfall could also lead to an attenuation of flood peaks and thus reduce the differences between small and large events, which would make a light-tailed distribution likely.

Runoff generation can affect the tail behaviour of flood peak distributions, especially through threshold processes (Macdonald et al., 2024). Threshold processes in runoff generation have also been found to result in step changes in flood frequency curves (FFCs) (Rogger et al., 2012; Struthers and Sivapalan, 2007). In a data-based study of 480 catchments in Germany and Austria, Macdonald et al. (2022) found that heavy-tailed flood peak distributions emerge, especially when there are distinct differences in the catchment responses between small and large flood events. Such distinct differences and step changes have been found to decrease with a more variable spatial distribution of storage capacities in a catchment (Rogger et al., 2013). Similarly, Struthers and Sivapalan (2007) found that spatially variable soil depth “simplifies” FFCs by allowing a smooth rather than abrupt transition from unsaturated to saturated. They stated that homogeneous conditions lead to binary saturation behaviour and heterogeneous conditions to a steadily increasing partial saturation. Basso et al. (2015) linked heavy tails of streamflow distributions to highly non-linear storage–discharge relations, and in a follow-up study they suggested that the spatial heterogeneity of hydraulic properties between hillslopes is one factor leading to such non-linear relationships (Basso et al., 2016). Based on these studies, Merz et al. (2022) concluded in their review that, while the importance of the catchment response for heavy-tailed behaviour is clear, “there are contrasting answers to the question whether spatial variability in runoff generation enhances or dampens the tail heaviness” of flood peak distributions.

Catchment size has been found to influence flood peak tail behaviour, and it also interacts with the spatial variability of rainfall and runoff generation. In data-based studies, tail heaviness has been found to decrease with increasing catchment size in Austria (Merz and Blöschl, 2009), Ger-

many and Austria (Macdonald et al., 2022), and the eastern United States (Villarini and Smith, 2010). In contrast, studies in the Appalachian region (Morrison and Smith, 2002) and the entire United States (Smith et al., 2018) did not find an effect of the catchment size on flood peak tail behaviour. Catchment size could influence the tail behaviour in different ways. First, the dominant factors in flood generation can shift with catchment size: for example, convective rainfall bursts are more relevant for small catchments, while the effects of flood routing become more important in large catchments (Merz and Blöschl, 2009). Second, the catchment size interacts closely with the spatial variability of rainfall and runoff generation. Zhu et al. (2018) found that the spatial rainfall structure is more important for peak discharges in large catchments compared to small ones, partly because rainfall is generally less spatially variable in smaller catchments. In contrast, Wang et al. (2023) found that tail heaviness starts to increase at a lower degree of rainfall variability in small catchments than in large ones and concluded that small catchments are less resilient to the spatial variability of rainfall with respect to the emergence of heavy flood peak tails. With regards to runoff generation, Rogger et al. (2012) stated that the catchment storage tends to become more spatially variable with increasing catchment size. This makes the widespread simultaneous saturation in a catchment and thus the occurrence of a step change in the FFC more likely in small catchments (Rogger et al., 2012), while at larger scales such pronounced non-linear behaviour of the runoff generation tends to be averaged out (Merz et al., 2022).

To improve the highly uncertain estimation of the upper-tail behaviour given the typical length of observations, a better understanding of the processes that control the tail behaviour and longer time series can be helpful. Both can be achieved through modelling approaches. Through a simulation-based approach, we can define and extract information about all relevant flood processes which lead to a certain tail behaviour. We can also simulate long time series to allow more robust statistical analyses. However, modelling approaches can only represent a simplified version of reality and cannot include all processes relevant to flood generation in every detail. Still, a lot can be learned through such simulations. Using a modelling approach, Macdonald et al. (2024) analysed the effects of rainfall and runoff generation properties on flood peak tail behaviour. However, they focused on small homogeneous catchments and did not analyse the effects of spatial variability and catchment size.

In this study, we analyse how the spatial variability of rainfall affects the upper-tail behaviour of flood peak distributions and whether this effect depends on the tail of the rainfall distribution. We also investigate whether the spatial variability of the runoff generation has an effect on the flood peak tail behaviour. Finally, we analyse how those effects of spatially variable rainfall and runoff generation interact with catchment size and whether there is a link between catchment size and the upper-tail behaviour of flood peak distributions. To

address these questions, we use a simulation model chain consisting of a weather generator, a rainfall-runoff model, and a river routing routine. With this model chain, long time series of precipitation and discharge can be generated and their tail behaviour subsequently assessed for catchments of various sizes.

2 Methods

A simulation model chain is used to generate long time series of precipitation and discharge. The model chain consists of a stochastic weather generator, a conceptual rainfall-runoff model, and a river routing routine (Fig. 1a). For the simulated precipitation and discharge time series, frequency analyses and an analysis of the respective upper-tail behaviour are conducted. The simulations are run on a large synthetic catchment to allow a range of spatially variable setups. The different model setups are defined according to research questions: different degrees of the spatial variability of rainfall and runoff generation are considered as well as rainfall distributions with varying tail behaviours (Fig. 1b), and the frequency analyses are conducted for catchments of various sizes. Overall, the climate conditions and catchment properties used in the model setups are characteristic of central Europe.

2.1 Synthetic catchment

The synthetic catchment on which the simulations are run is generated using the R package OCNet (Carraro et al., 2020). The package is designed to generate and analyse optimal channel networks which reproduce “all scaling features characteristic of real, natural river networks” (Carraro et al., 2020). With a resolution of $2 \times 2 \text{ km}^2$, a synthetic catchment is generated that has an area of $101\,588 \text{ km}^2$ and elevations between 0 and 805 m (Fig. 2a). In the aggregation of the river network, we aim for a number of network nodes that is high enough to allow spatial analyses over a wide range of catchment sizes while balancing this with the increasing runtime of the simulation model chain with an increasing number of nodes. The final number of nodes is 678, corresponding to 678 sub-catchments in the catchment.

2.2 Simulation model chain

The first part of the simulation model chain is a stochastic multi-site, multi-variate weather generator. It is set up based on observational data from stations in Germany (Hundecka et al., 2009; Nguyen et al., 2021) and is used to generate time series of precipitation P , temperature T , and potential evapotranspiration PET as input to the rainfall-runoff model. With regards to P , the weather generator has been evaluated as capturing well both the daily mean and the extreme intensities for a large set of weather stations in central Europe (Nguyen et al., 2021). Here, it is used to generate

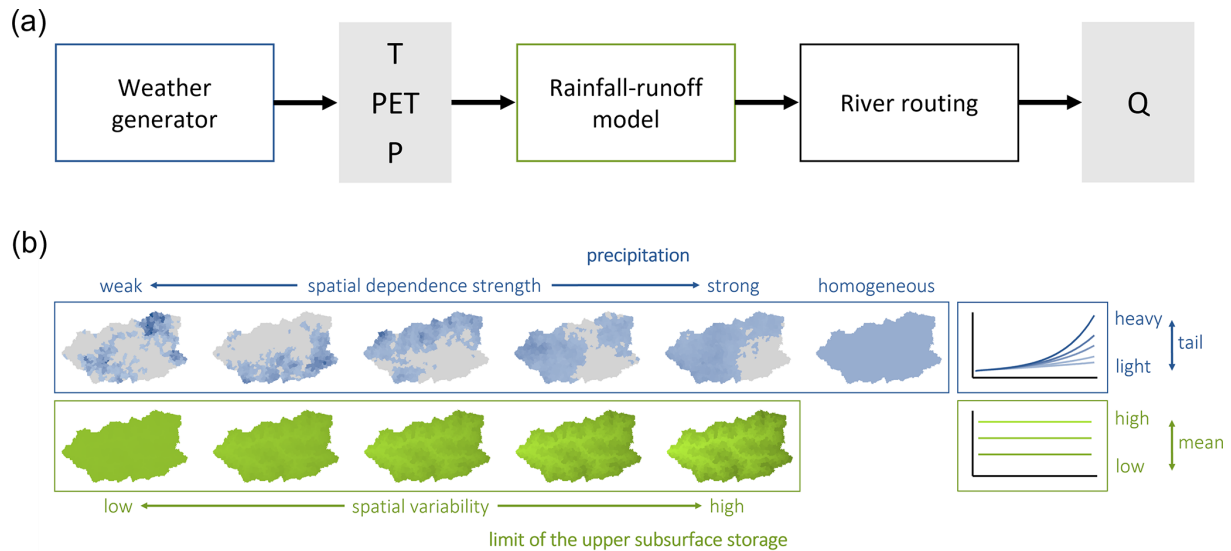


Figure 1. Schematics of the modelling approach. **(a)** The simulation model chain: using a stochastic weather generator, time series of temperature (T), potential evapotranspiration (PET), and precipitation (P) are generated. These are then fed into a conceptual rainfall-runoff model coupled with a river routing routine to simulate long, continuous discharge time series. **(b)** The model setups: in the weather generator, different setups are generated by changing the spatial dependence strength and the tail behaviour of precipitation. In the rainfall-runoff model, the mean value and spatial variability of the limit of the upper subsurface storage are varied between setups.

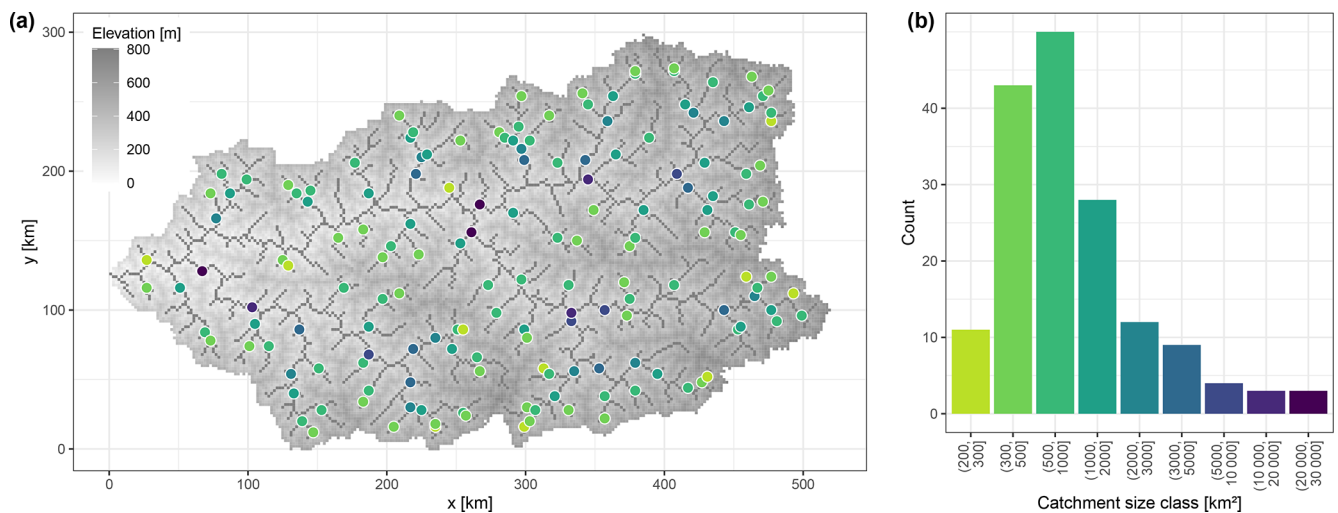


Figure 2. **(a)** The outlets of 163 catchments which are selected for analyses based on nine size classes and **(b)** the number of catchments per size class. Catchments within one class are not nested, while catchments across classes can be nested.

multi-site point data for 678 points in the synthetic catchment. Each of the points is considered to be representative of a sub-catchment and is later taken as the areal input for the respective sub-catchment. The generated time series are based on observational data from the weather station in Bamberg (DWD, 2022), which is among the stations with the longest available records in Germany. For each configuration of the weather generator, 100 realizations of the same length as the observed record, i.e. 72 years, are generated with a daily resolution. The configurations differ in the tail

behaviour of P and in the spatial variability of P . For the first aspect, the upper-tail shape parameter of an extended generalized Pareto (extGP) distribution, which was fitted to the observed P data, is modified systematically. This is done by multiplying the extGP shape parameter by a factor between 0.1 and 1.3. The lower-tail shape and scale parameters of the extGP distribution remain as fitted to the data. The P time series with different tail behaviours are then re-scaled to have the same mean. To generate P time series with different spatial variabilities, the spatial dependence strength

of E-OBS data in Germany (Cornes et al., 2018) is derived. Spatial dependence is quantified by calculating the pairwise cross-correlation of precipitation between grid cells, modelled as an exponential decay with distance, where the decay coefficient k denotes dependence strength. For Germany, k is around 0.0025 and is labelled as medium (M) dependence strength. Based on this, two weaker (weak W , medium weak MW) and two stronger (medium strong MS , strong S) dependence strength setups are derived. Note that these are “weak” and “strong” relative to the dependence strength derived for Germany and are not necessarily in absolute terms. The spatial dependence strength is used to derive data at all locations based on the Bamberg data. This approach and the manipulation of the extGP upper-tail shape parameter produce different spatial setups as well as time series with different frequencies of extremes.

The second part of the simulation model chain is a conceptual rainfall-runoff model following the structure of the HBV model (R package TUWmodel; Parajka et al., 2007). It consists of snow, soil moisture, response, and catchment routing routines with a total of 15 model parameters. The model is run in a lumped way in each of the 678 sub-catchments of the large synthetic catchment (101 588 km²). It is forced by the time series of P , T , and PET simulated with the weather generator as areal input. The temporal specifications are the same as for the weather generator, i.e. 100 realizations of 72 years of daily data for each setup. However, the first 2 years of each realization and setup are used as a warm-up period for the model and are later removed from the analyses; 14 of the 15 model parameters are set to fixed values and do not vary between model setups. The values are based on the average parameter values of model calibrations for 273 Austrian catchments as reported by Merz et al. (2011) and can be found in Table A1 in Macdonald et al. (2024). The only model parameter that varies between model setups is the storage capacity of the upper subsurface storage L_{UZ} . When this storage capacity is exceeded, an additional and faster runoff component q_0 is triggered:

$$q_0 = \frac{S_{UZ} - L_{UZ}}{k_0}, \quad (1)$$

where S_{UZ} is the storage in the upper zone and k_0 is the storage coefficient for the very fast runoff response. The spatial variability in L_{UZ} thus affects whether saturation excess runoff is triggered locally or widely. In the model setups, three different mean levels of the storage capacity \bar{L}_{UZ} are considered (23, 43, and 63 mm) as well as different spatial configurations: for five degrees of variability, L_{UZ} varies across space following the topography (Fig. 1b). The lowest storage capacity $L_{UZ,\min}$ is assumed at the highest elevation z_{\max} , and it increases linearly for lower elevations:

$$L_{UZ,i} = \frac{L_{UZ,\min} - \bar{L}_{UZ}}{z_{\max} - \bar{z}} \cdot z_i + \frac{\bar{L}_{UZ} \cdot z_{\max} - L_{UZ,\min} \cdot \bar{z}}{z_{\max} - \bar{z}}, \quad (2)$$

where $L_{UZ,i}$ is the storage capacity at elevation z_i and \bar{z} is the mean elevation of the entire catchment. The five degrees of spatial variability are achieved by setting $L_{UZ,\min}$ to different values of \bar{L}_{UZ} : between 2 mm (lowest variability) and 1 mm (highest variability). The mean values and ranges of L_{UZ} are defined based on the ranges reported in previous studies (Parajka et al., 2007; Macdonald et al., 2024) and findings from test runs. The ratio of the mean rainfall depth to the catchment storage is relevant for the frequency of storage exceedances, and so L_{UZ} is defined as covering a wide range of exceedance frequencies with the pre-defined rainfall data.

The last part of the model chain is a river routing module, which routes the simulated runoff of each sub-catchment along the river network to the final outlet. The routine uses a cascade reservoir approach and is based on the Streamflow Synthesis and Reservoir Regulation (SSARR) model (USAEDNP, 1975). For a given catchment with a median length of river sub-reaches of 10 km, the routing needs to be run on a sub-daily timescale to achieve accurate results. Through test runs, the optimum value between accuracy and computational time is found to be a 2-hourly resolution. The daily runoff simulated with the rainfall-runoff model is disaggregated to 2-hourly values using linear interpolation between the simulated values and is re-aggregated to daily time series after the routing. The river routing is defined by three model parameters: the number of sub-reaches per river reach (nbr), a coefficient affecting the time of storage per sub-reach (kts), and an exponential coefficient controlling the impact that a change in discharge has on the time of storage per sub-reach (n) (NOAA, 2003). The time of storage (TS) per sub-reach is defined as

$$TS = \frac{kts}{Q^n}, \quad (3)$$

with Q being the discharge. The parameter nbr is commonly estimated using the characteristic reach length LC by taking the ratio between the total length of a river reach and LC (Pelin and Pahlsson, 2012). The three parameters are kept constant between all model runs and their values are based on physical considerations: the parameter values should result in realistic peak flows and travel times for a catchment of a given size. Previous studies found travel times of flood peaks for 500 km river reaches between 1.5 and 6 d (He, 2020; Allen et al., 2018; Meyer et al., 2018). Using the relation between catchment size and maximum observed daily peak flow of the 360 German catchments analysed by Macdonald et al. (2022), a peak flow of 4500 to 7500 m⁴ s⁻¹ is estimated for a catchment of 101 588 km². Travel times and peak flows within these ranges at the final outlet were used as criteria for defining the model parameters of the routing routine. The parameters are set to $L_C = 10$ km, $kts = 10$, and $n = 0.3$. These values are within the ranges reported in previous studies (Pelin and Pahlsson, 2012; USAEDNP, 1975).

The output of each run of the model chain consists of the simulated discharge time series at each outlet, along with the

time series of the share of the very fast runoff component and the respective model parameters and precipitation time series which were used in the model run. While we aimed to set up the model with climate conditions and catchment properties which are realistic for central Europe, the simulated time series do not relate to real-world catchments. Instead, the focus is on analysing the effects that specific changes in the model configurations have on the tail behaviour of flood peak distributions.

2.3 Analysis of the simulated time series

The simulated time series of P and Q and the spatial indices are analysed for catchments of different sizes. To this end, a subset of the 678 sub-catchments and their upstream catchments is selected as follows: first, lower and upper size limits are determined. The catchments should consist of at least three sub-catchments to allow spatial analyses, which results in a lower size limit of 200 km². Further, there should be at least three distinct catchments of similar sizes to allow robust results, which leads to an upper size limit of 30 000 km². Second, nine catchment size classes within this range were defined with the following breaks: 200, 300, 500, 1000, 2000, 3000, 5000, 10 000, 20 000, and 30 000 km². Third, within each size class, all distinct catchments are selected. If there are nested catchments within one size class, only the largest one of them is considered. This results in 163 catchments (Fig. 2), which consist on average of 14 sub-catchments and for which all subsequent analyses are conducted.

To analyse the tail behaviour, annual maxima of the simulated P and Q time series are derived. For P , this is done for all 678 locations used in the weather generator. For Q , this is done only for the 163 selected outlets. After removing the warm-up periods, the 100 realizations of each model setup are combined into one long time series of 7000 years for distribution fitting. GEV distributions are fitted to the annual maximum series (AMS) of P and Q using L-moments. L-moment fitting has been evaluated as reasonably efficient in parameter estimation compared to the maximum likelihood method (Hosking, 1990) while being a lot less computationally expensive. In addition to this, a recent study by Vogel et al. (2024) highlighted the advantages of using L-moments when working with heavy-tailed data, as L-moments are always finite when the mean exists, even if higher moments do not exist. To make the tail behaviour of P and Q comparable, the shape parameters of the P distributions are aggregated to the same 163 outlets where Q is analysed: for each outlet, the median shape parameter of the P distributions of all the upstream sub-catchments is estimated.

The spatial variability of P is quantified for each model setup and for each of the 163 outlets. First, the spatial coefficient of variation $CV_{P,t}$ of P across all sub-catchments upstream of an outlet is estimated for each day t :

$$CV_{P,t} = \frac{\sqrt{\frac{1}{N} \sum_{n=1}^N (P_{t,n} - \bar{P}_t)^2}}{\bar{P}_t}, \quad (4)$$

where N is the number of sub-catchments upstream of the respective outlet, $P_{t,n}$ is the rainfall depth in sub-catchment n on day t , and \bar{P}_t is the mean rainfall depth across all N sub-catchments on day t . Second, the median of $CV_{P,t}$ of all rainy days within the 7000-year time series is estimated ($CV_{P,med}$). Rainy days are defined as all days on which it rained in at least one sub-catchment ($P > 0$ mm).

The spatial variability of the runoff generation is quantified for each model setup and for each of the 163 outlets. As a measure of spatial runoff variability, we consider how locally or widely saturation excess runoff is usually triggered in a catchment. For each day t , the number of sub-catchments upstream of an outlet where the very fast runoff component q_0 was active is evaluated. The mean of this number is estimated for all days on which q_0 was active in at least one sub-catchment, and it is then divided by the total number of sub-catchments. This gives the average share of sub-catchments in which the very fast runoff component is triggered simultaneously. That is, it is a measure of whether saturation excess runoff is usually triggered locally or widely in a catchment.

3 Results

Simulated discharge time series of 375 different model setups are analysed for 163 catchments ranging in size from 200 to 30 000 km². We find a clear downward trend in the GEV shape parameter of flood peak distributions with increasing catchment size (Fig. 3). While there is a large spread in the shape parameters between the different model setups for each catchment, there is a significant (p value < 0.001) linear trend across the catchment sizes. The GEV shape parameter decreases by 0.04 per order of magnitude of catchment size.

The catchment size is found to interact with the spatial variability of rainfall. For 25 different setups of the weather generator, which were evaluated at 163 catchments of various sizes, the spatial variability of P expressed as $CV_{P,med}$ increased with increasing catchment size (Fig. 4). This means that rainfall tends to be more variable in larger catchments. As expected, we also see a clear stratification of $CV_{P,med}$ with the spatial dependence strength specified in the respective setup of the weather generator. A weak spatial dependence strength of P results in more spatially variable rainfall and thus a higher $CV_{P,med}$ than a strong spatial dependence strength.

When the GEV distribution of the forcing rainfall has a high shape parameter, the resulting discharge also tends to have a higher GEV shape parameter than that resulting from rainfall with a lighter tail (Figs. 3 and 5). This is observed for

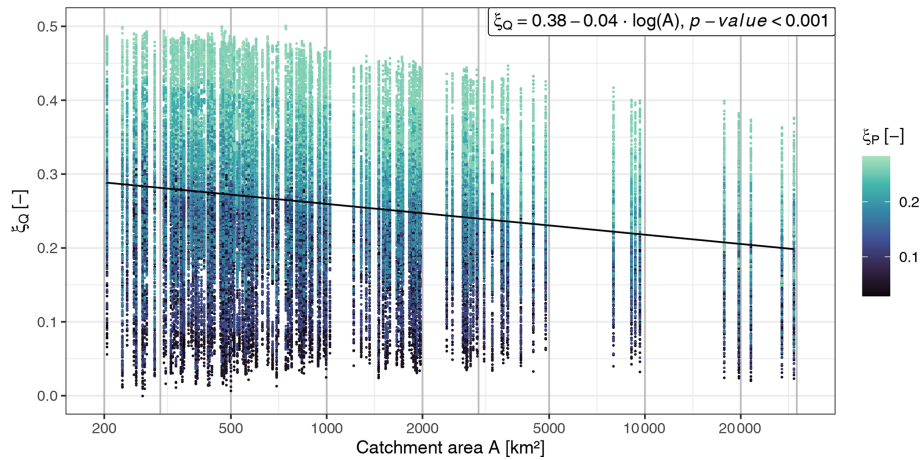


Figure 3. Shape parameters (ξ_Q) of generalized extreme value (GEV) distributions fitted to simulated discharge series versus catchment area (A). Results are based on 375 model setups which are evaluated at 163 catchment outlets. The model setups differ in the tail behaviour (ξ_P) and spatial variability of the rainfall input as well as in the mean value and spatial variability of the limit of the subsurface catchment storage. GEV distributions were fitted to annual maximum series of 7000 years. A linear trend (black line) and its formula are displayed.

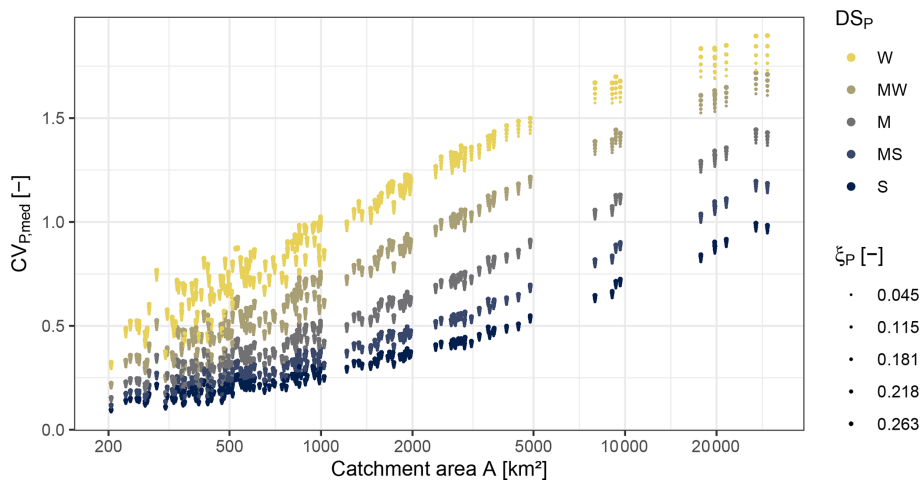


Figure 4. The median spatial coefficient of variation of precipitation ($CV_{P,med}$) versus A for 163 catchments. $CV_{P,med}$ is based on the daily rainfall in all sub-catchments of a catchment, and the median is taken across all rainy days of the 7000-year time series. Results are based on 25 setups of the weather generator: five values of spatial dependence strength DSP from weak (W) to strong (S) and five values of the tail heaviness (ξ_P) of the underlying rainfall distribution.

different catchment sizes (Fig. 3) and for different degrees of spatial variability of the rainfall (Fig. 5).

Increasing spatial variability of rainfall tends to lead to a decrease in the flood peak shape parameter, at least when the spatial variability of the catchment storage capacity is low (Fig. 5, left column). With increasing spatial variability of the catchment storage capacity, the downward trend becomes less clear. Especially when the spatial variability of rainfall is low but that of the storage capacity is high (Fig. 5, right column), there is a large spread in the tail behaviour of flood peak distributions. In contrast, when the spatial variability of both rainfall and storage capacity is high, we see a downward

trend in flood peak shape parameters against rainfall variability. This indicates that, as rainfall variability increases, it starts dominating the flood peak tail behaviour, independent of the degree of storage variability.

The overall downward trend in flood peak shape parameters with increasing rainfall variability should be considered with care, as we see a clear relation between the spatial variability of rainfall and catchment size (Fig. 4). As higher degrees of rainfall variability are often related to larger catchments, the observed trend might show the combined effect of rainfall variability and other processes that change with catchment size, such as peak attenuation and river routing.

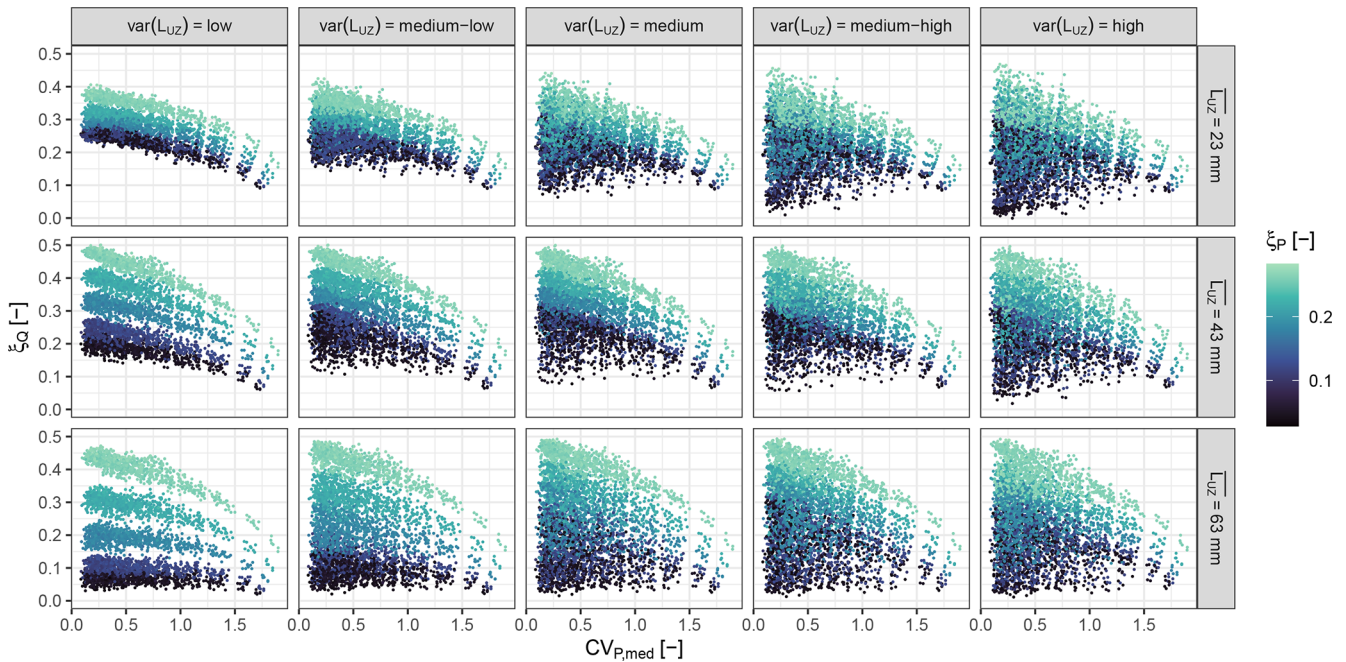


Figure 5. ξ_Q of GEV distributions fitted to simulated discharge series versus spatial rainfall variability expressed as $CV_{P,med}$. Results are based on 375 model setups which are evaluated at 163 catchment outlets. The model setups differ in the tail behaviour (ξ_P) and spatial variability ($CV_{P,med}$) of the rainfall input as well as in the mean value ($\overline{L_{UZ}}$) and spatial variability ($\text{var}(L_{UZ})$) of the limit of the subsurface catchment storage. GEV distributions are fitted to annual maximum series of 7000 years.

To address this aspect, the effect of the spatial variability of rainfall is analysed separately for two catchment size classes.

By considering only simulations with low variability of the catchment storage capacity and by evaluating size classes separately, we can reduce confounding effects. For the 54 smallest catchments (200–500 km²), the rainfall variability $CV_{P,med}$ ranges between 0.085 and 0.83, while $CV_{P,med}$ is between 0.62 and 1.9 for the 10 largest catchments (5000–30 000 km²) (Fig. 6). There are fewer sub-catchments in the smaller catchments, and therefore variability cannot get as high as in the larger catchments. For the small catchments, there is a very slight or hardly any trend of flood peak shape parameters with increasing rainfall variability. For the large catchments, flood peak shape parameters decrease with increasing rainfall variability. Here, the downward trends are especially clear for high rainfall shape parameters and low catchment storage capacities. Further, we see an effect of the mean level of the catchment storage capacity $\overline{L_{UZ}}$: for smaller catchment storages, the range of flood peak shape parameters for any given rainfall variability is smaller than for larger catchment storage capacities (Fig. 6). The larger storage capacity seems to enhance the differences in flood peak shape parameters which are induced by different rainfall shape parameters.

To quantify the spatial variability of runoff generation, we consider whether saturation excess runoff is usually triggered locally or widely in a catchment. This is characterized here

by the average share of sub-catchments in which the very fast runoff component q_0 is triggered simultaneously (n_{q_0}/N). In analysing the effect of spatially variable runoff on flood peak tail behaviour, we are particularly interested in the variability that is induced by catchment properties such as the storage capacity rather than by spatially variable rainfall. However, spatially variable rainfall has a strong effect on the spatial variability of runoff generation: for spatially variable rainfall, the share of sub-catchments in which the very fast runoff component is triggered simultaneously is not affected by the spatial variability of the catchment storage capacity (Fig. 7). On the other hand, for homogeneous rainfall, we see a clear relation: the higher the spatial variability of the catchment storage capacity, the lower the n_{q_0}/N , meaning that saturation excess runoff occurs rather locally for very variable storage capacities. If we want to analyse the spatial variability of runoff generation that is related to catchment properties, we need to consider homogeneous rainfall to exclude strong confounding effects. However, assuming homogeneous rainfall conditions over a catchment of 101 588 km² is not very realistic. The following results should therefore not be mistaken for realistic simulations, but they can still provide insights into how certain processes affect the flood peak tail behaviour.

By considering only model runs with homogeneous rainfall, we can eliminate the effect of rainfall variability on saturation excess runoff, so that we see only the effect of

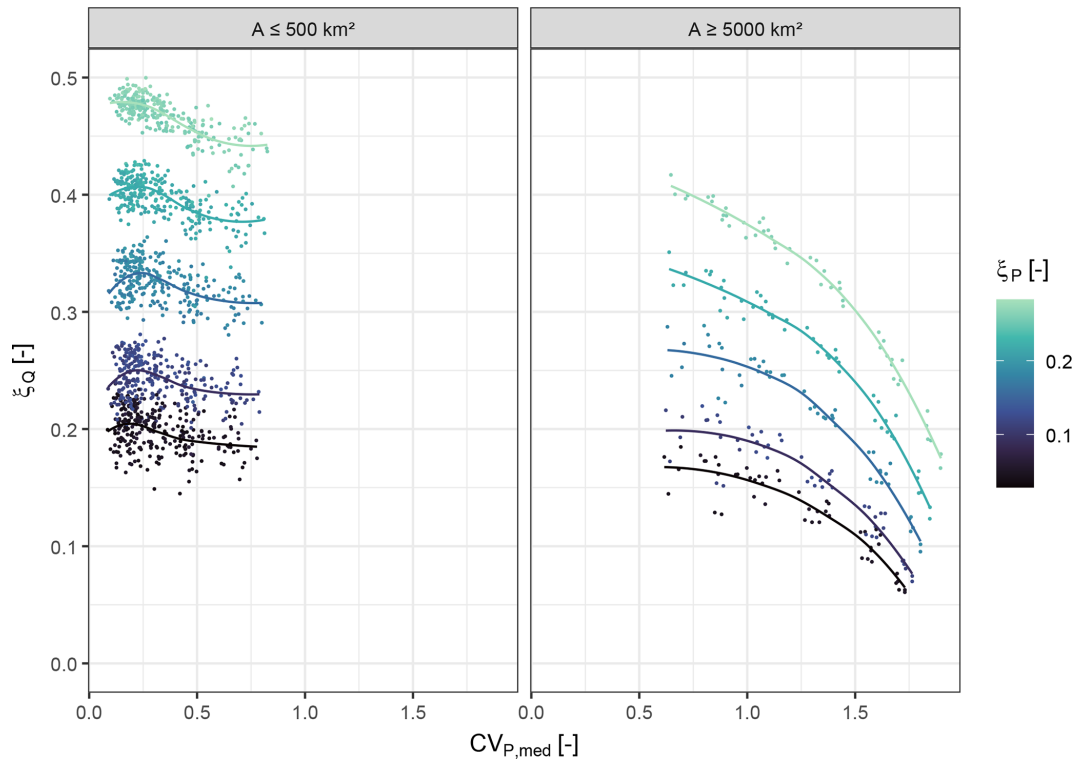


Figure 6. ξ_Q of GEV distributions fitted to simulated discharge series versus spatial rainfall variability expressed as $CV_{P,med}$. Results are based on 75 model setups with close to homogeneous catchment storage (i.e. $var(L_{UZ}) = \text{low}$). The setups differ in the tail behaviour (ξ_P) and spatial variability ($CV_{P,med}$) of the rainfall input as well as in the L_{UZ} . The simulations are evaluated for the 54 smallest and 10 largest catchments. GEV distributions are fitted to annual maximum series of 7000 years. Locally estimated scatterplot smoothing (LOESS) curves are fitted to subsets of simulations with the same rainfall tail behaviour.

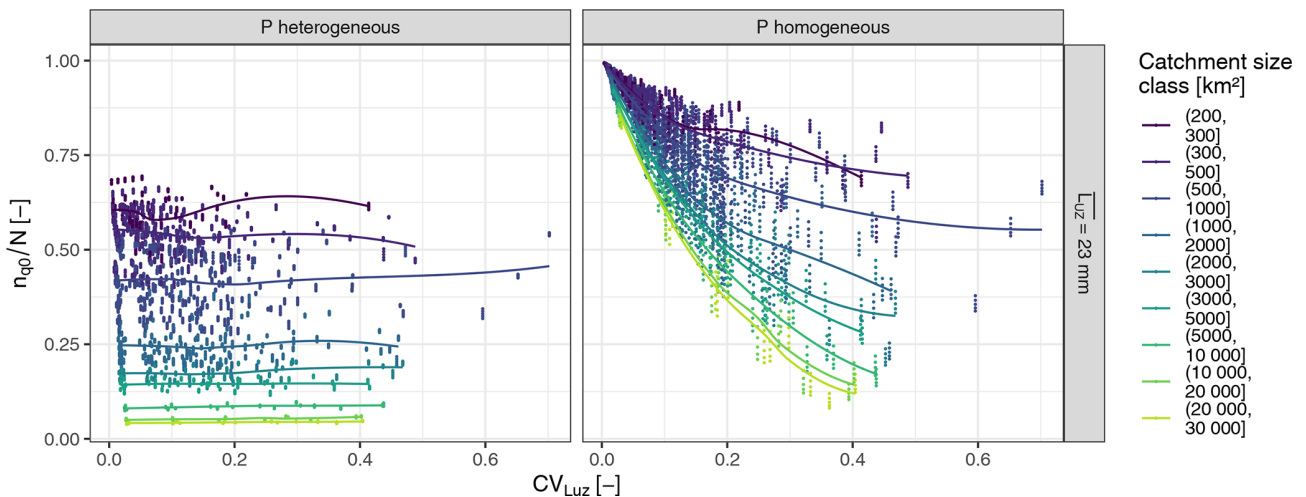


Figure 7. Average share of sub-catchments with simultaneous activation of the very fast runoff component (n_{q_0}/N) against the spatial coefficient of variation of the catchment storage ($CV_{L_{UZ}}$). Results are based on 50 model runs which are evaluated at 163 catchment outlets. Model setups differ in the tail behaviour and spatial variability of the rainfall input and in the spatial variability of the limit of the sub-surface catchment storage (L_{UZ}). Heterogeneous precipitation (P) relates to the model setup with the weakest spatial dependence strength for P , while for a homogeneous P the same time series of P is assumed for all the sub-catchments. LOESS curves are fitted for different catchment size classes.

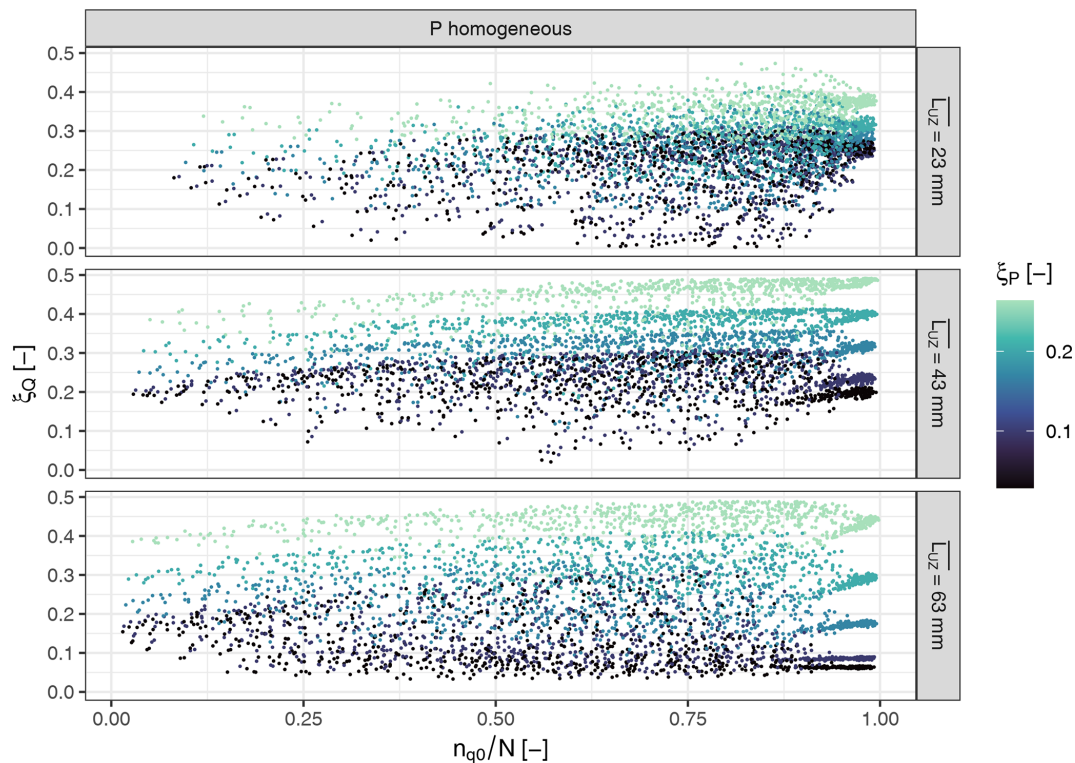


Figure 8. ξ_Q of GEV distributions fitted to simulated discharge series versus the average share of sub-catchments with simultaneous activation of a very fast runoff component (n_{q0}/N). Results are based on 75 model setups with homogeneous rainfall, which are evaluated at 163 catchment outlets. The model setups differ in the tail behaviour (ξ_P) of the rainfall input as well as in the \bar{L}_{UZ} and spatial variability of the limit of the sub-surface catchment storage. GEV distributions are fitted to annual maximum series of 7000 years.

runoff generation variability caused by spatial variability in the catchment storage capacity. Whether saturation excess runoff is triggered locally or widely has no clear effect on the tail behaviour of flood peak distributions (Fig. 8). When saturation excess runoff is usually triggered very widely in a catchment, i.e. when the average share of sub-catchments with simultaneous activation of very fast runoff component is close to 1, the GEV shape parameters are clustered around a few values – those clusters differ in terms of the tail behaviour of the rainfall distribution and in the mean storage depth. For spatially variable runoff generation, i.e. when saturation excess is usually triggered more locally, we see point clouds with no clear trends or relations. These point clouds however look different for the different mean levels of the catchment storage capacity.

There appears to be a non-linear relationship between the shape parameters of the flood peak distributions and the average depth of the sub-surface catchment storage (Fig. 9). The flood peak shape parameters are low for small and large catchment storage capacities and have a maximum for medium storages. This non-linear behaviour seems to be related to the distribution fitting rather than to hydrological processes: when looking at the frequency curves of simulated annual maxima and the respective fitted distributions

(Fig. 10), the tail behaviour of the simulated peak discharges is not always represented well by the fitted GEV distribution. There can be a step change in the annual maxima, and the return period of the step change affects how well the fitted distribution can represent the data. The return period in turn depends on rainfall characteristics and the catchment storage. For example, in cases with small catchment storage capacities and light-tailed precipitation, the fitted GEV distributions overestimate the flood peaks with high return periods (Fig. 10, top row).

In the setup with the least variable catchment storage capacities, the estimated mean storages for all 163 catchments cluster around the mean values used in the model setups, i.e. 23, 43, and 63 mm (Fig. 9). In contrast, for the most variable setup of catchment storage capacities, the estimated mean storages range from 4 to 102 mm. The mean values are fixed in the model setup for the entire large catchment, but we analyse sub-catchments, and they can have very different mean storages depending on where in the large catchment they are located.

How locally or widely saturation excess runoff is usually triggered in a catchment only has a very little effect on the flood peak shape parameter compared to the mean catchment storage (Fig. 9). For heavy-tailed rainfall distributions, more

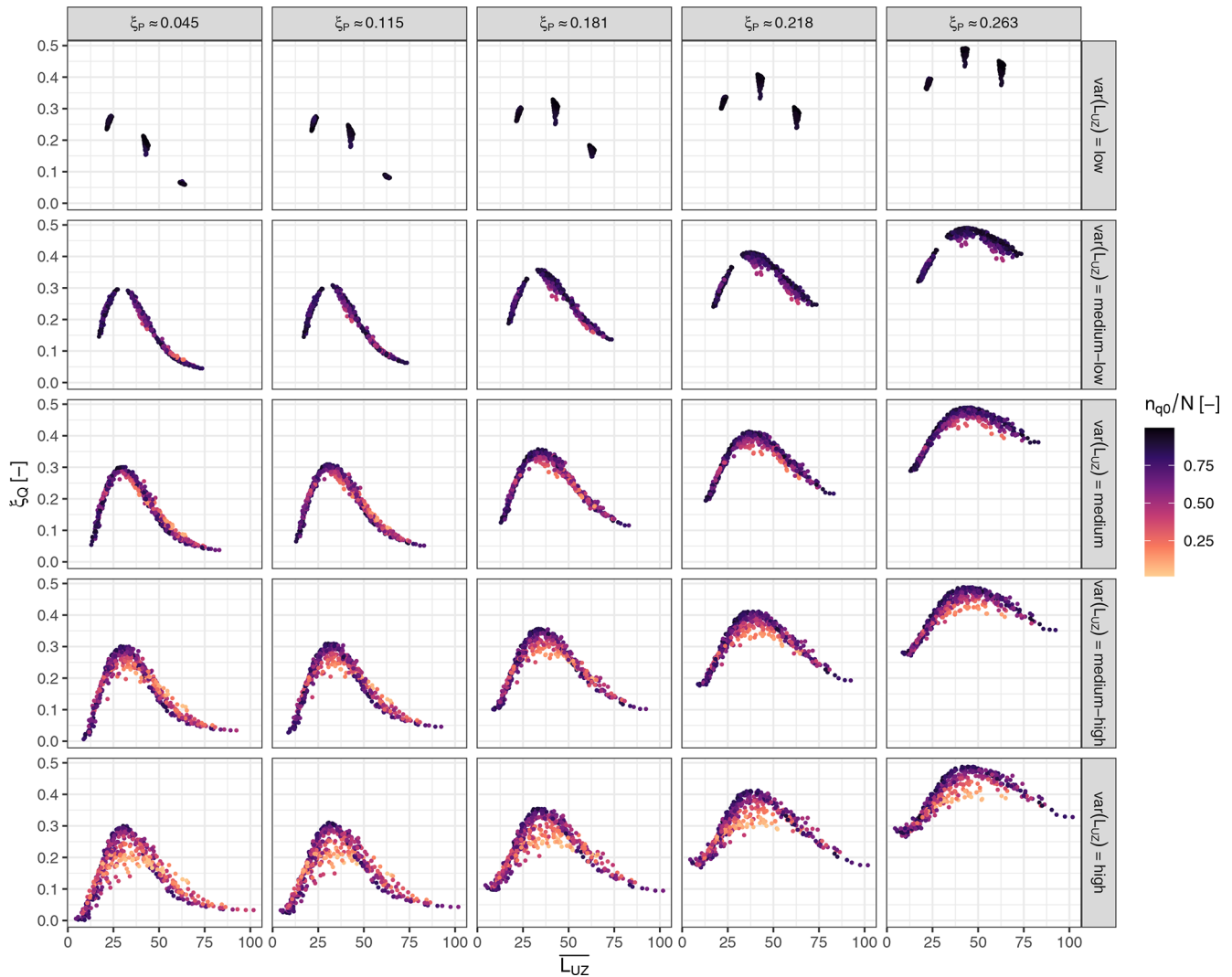


Figure 9. ξ_Q of GEV distributions fitted to simulated discharge series versus the $\overline{L_{UZ}}$. Results are based on 75 model setups with homogeneous rainfall, which are evaluated at 163 catchment outlets. Model setups differ in the tail behaviour (ξ_P) of the rainfall input and in the mean value and spatial variability of the limit of the sub-surface catchment storage. The latter results in spatial variability of runoff generation, which is expressed here as the average share of sub-catchments with simultaneous activation of a very fast runoff component (n_{q0}/N). GEV distributions are fitted to annual maximum series of 7000 years.

variable runoff generation at the same level of the mean storage capacity tends to lead to a lower flood peak shape parameter (Fig. 9, bottom right). For light-tailed rainfall distributions, this is only true for medium catchment storage capacities, while for larger storage capacities more variable runoff generation leads to higher shape parameters (Fig. 9, bottom left).

4 Discussion

The trend we found of decreasing flood peak shape parameters with increasing catchment sizes is in line with some previous studies (e.g. Macdonald et al., 2022; Villarini and

Smith, 2010). Other studies did not find this trend (e.g. Smith et al., 2018; Morrison and Smith, 2002). The stream gauges analysed by Morrison and Smith (2002) are most likely also included in the larger set of gauging stations analysed by Villarini and Smith (2010), and the latter ones analysed much longer time series – at least 75 years of observations compared to 30 years for Morrison and Smith (2002). The trend found by Villarini and Smith (2010) therefore appears more reliable. They found a decrease in the shape parameter of 0.07 per order of magnitude of the catchment size for 572 catchments in the eastern United States, which is slightly higher than the decrease of 0.04 resulting from our analysis. This could be a regional difference or related to differences between real-world data and simulations with a spe-

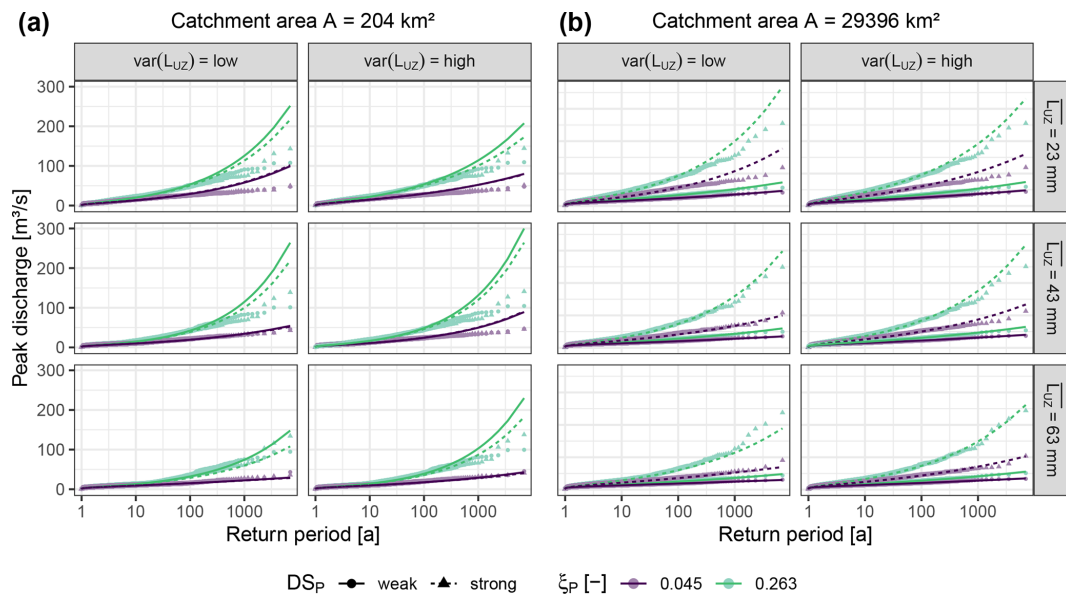


Figure 10. Example flood frequency curves (FFCs) for the (a) smallest and (b) largest catchments analysed. The annual maxima of the simulated discharge series of 7000 years are presented (dots and triangles) along with the GEV distributions fitted to those annual maxima (solid and dashed lines). The FFCs result from 16 model setups which differ in the tail behaviour (ξ_P) and spatial dependence strength (DSP) of the rainfall input as well as in the L_{UZ} and $\text{var}(L_{UZ})$ of the limit of the sub-surface catchment storage.

cific modelling setup: some studies show that rainfall tails become lighter for larger areas (Merz et al., 2022; Overeem et al., 2010; Dyrddal et al., 2016), but in our setup we keep the rainfall tail constant across catchment scales. Adding this effect could enhance the downward trend of flood peak shape parameters against catchment sizes. A potential explanation for the trend is that, in small catchments, distinct non-linear behaviours in the runoff generation and convective rainfall bursts can result in heavy tails, while in larger catchments, where routing effects become increasingly important, these effects might be averaged out (Merz and Blöschl, 2009).

Irrespective of the degree of spatial variability of rainfall, we found that a higher shape parameter of the rainfall distribution tends to lead to a higher shape parameter of the flood peak distribution. This is in line with the findings of Macdonald et al. (2024) for small homogeneous catchments and those of Gaume (2006), who stated that rainfall statistical properties asymptotically control the shape of flood peak distributions. We estimate the rainfall shape parameter for each catchment by taking the median shape parameters of the P distributions of all the sub-catchments. An alternative approach would be to aggregate P on a daily basis across the catchment area and then derive the annual maxima and shape parameters from the aggregated, areal P . We assume that the slightly simpler approach that we use gives adequate results for our setup, as we do not vary the rainfall tail behaviour in space. In each setup of the weather generator, rainfall is generated with a fixed upper-tail shape parameter of the extGP distribution across all the sub-catchments. If the rainfall tail behaviour varies strongly in space within a catchment, the

alternative approach is deemed more appropriate for estimating rainfall tail behaviour that is representative of the entire catchment.

We found a decreasing trend of flood peak shape parameters with increasing spatial variability of rainfall, especially for large catchments, and no clear trend for small catchments. For small catchments, the range of spatial variability considered was smaller than for larger catchments, as the spatial variability is limited by the number of sub-catchments in a catchment in our setup. The decreasing trend that we found for large catchments seems to oppose the results of Wang et al. (2023), who found that increasing spatial variability of rainfall leads to heavier tails of flow distributions beyond a certain degree of variability. They based this finding on scenario simulations for five German catchments (98–2841 km²). In two of their three scenarios, they kept the spatial variability of rainfall fixed in time, i.e. for all precipitation events and resulting floods. The spatial coefficient of variation of rainfall CV_P in their setups ranged from close to 0 to well beyond 10 (i.e. 1000 %), and the degree of variability beyond which they found an increase in tail behaviour was a CV_P of 2 or larger. The daily CV_P values in our study cover a similar range (Fig. 11), while the median across all rainy days in a catchment is always below 2. The rainfall variability in our setups is based on the spatial dependence strength estimated for E-OBS rainfall data in Germany, with two more levels of weaker dependence strength and two more levels of stronger dependence strength than observed. The range of rainfall variability in Wang et al. (2023) is based on the estimated spatial variability for 175 German catchments based

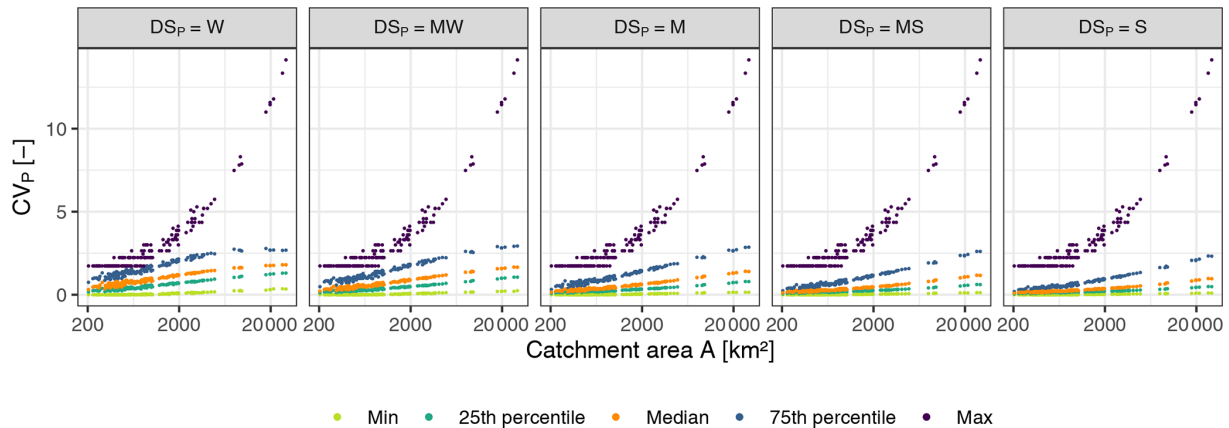


Figure 11. Percentiles of the spatial coefficient of variation of precipitation (CV_P) versus the A of 163 catchments. CV_P is based on the daily rainfall in all sub-catchments of a catchment, and for each catchment the percentiles across all rainy days of the 7000-year time series are presented. Results are based on five setups of a weather generator with W to S DSP between rainfall depths in the sub-catchments.

on REGNIE data, which is a rainfall field interpolated from point observations (Rauthe et al., 2013). The main difference seems to be that Wang et al. (2023) consider CV_P to be constant in time. They take a value above the 95th percentile of daily CV_P values as the upper bound of the spatial variability in their simulation setups – this means that values which were observed on less than 5% of the days in all the catchments are used in some setups to define the spatial variability on every day; that is, they are constant in time. Although the spatial variability of rainfall might increase in the future due to an increase in intensity and a decrease in spatial extent (e.g. Wasko et al., 2016; Peleg et al., 2018), it seems unlikely that such high degrees of variability will become persistent in time. We believe that this rather unrealistic assumption of Wang et al. (2023) is the main reason for finding opposing trends in flood peak tail behaviour with increasing spatial variability.

We explain the decreasing trend in tail heaviness with the increasing spatial variability that we found for large catchments as follows: in the least variable setup, extreme rainfall events occur simultaneously in a large part of the catchment and can therefore lead to widespread enhanced runoff generation, which in turn can result in a distinctively higher flood peak at the outlet of the catchment. In a more variable setup, on the other hand, extreme rainfall events are only localized, and therefore enhanced runoff generation might also be triggered only locally. Such a local flood peak is then attenuated on its way to the catchment outlet. In small catchments, we did not find a clear trend of flood peak shape parameters against rainfall variability, and the likely reason for this is the smaller attenuation effect in smaller catchments.

Finding lighter flood peak tails for increasing spatial variability of rainfall in large catchments could be seen as good news in the light of climate change. The spatial variability of rainfall is expected to increase in a warmer climate due to an increase in intensity and a decrease in spatial extent, as stud-

ies on convective rainfall and storm cells found (Wasko et al., 2016; Peleg et al., 2018). Such spatially more concentrated precipitation can be interpreted as increased spatial variability at the scale of large catchments and might therefore reduce the tail heaviness and thus the chance of surprising floods. However, the situation looks very different for small catchments: even more localized storm cells can cover the entire catchment area and the prospective intensified rainfall would result in more severe flooding. A shift to more spatially variable rainfall in a warmer future should therefore not necessarily be taken as good news for large catchments but rather indicates that the analysis of the flood peak tail behaviour will become increasingly important for small catchments.

The spatial variability of runoff generation caused by spatially variable sub-surface catchment storage capacities does not show a clear effect on flood peak tail behaviour. When the average share of sub-catchments with simultaneous activation of the very fast runoff component is close to 1, saturation excess runoff is usually triggered widely in a catchment. In this case, the flood peak shape parameters are clustered around a few values (Fig. 8), and these clusters vary according to the tail behaviour of the rainfall distribution and the mean storage depth. This influence of the rainfall tail behaviour and the mean storage depth for near-homogeneous runoff generation can be compared to the findings of Macdonald et al. (2024). For small catchments with homogeneous rainfall and runoff generation, they found that, beyond a certain return period, the tail of the rainfall distribution asymptotically controls the tail of the flood peak distribution, and this return period depends on the ratio of catchment storage to catchment wetness. We assume the storage capacity to follow the topography, with shallow storages at high elevations and deeper storages at lower elevations, as the soil depth usually decreases with increasing elevation (Scull et al., 2003; Van Tol et al., 2013). Test runs indicated though

that the exact spatial pattern in the spatially variable setups do not affect the findings (not shown).

In contrast to its spatial variability, the average depth of the sub-surface catchment storage appears to affect the shape parameter of flood peak distributions in a non-linear way. If the storage capacity is exceeded only by large and not smaller rainfall events, this can result in a step change in the flood frequency curve (Rogger et al., 2012). The size of the storage capacity determines the return period in which the step change occurs (Rogger et al., 2012). This means that the average depth of the sub-surface storage is relevant for how often the storage capacity is exceeded for a given rainfall level. Spatial variability in the storage capacity or soil depth has been found to smooth out step changes in the FFC (Rogger et al., 2013; Struthers and Sivapalan, 2007). Our results indicate that the return period in which a step change occurs in the FFC has a stronger effect on the tail behaviour of the fitted distribution than how pronounced this step change is. However, as Fig. 10 shows, having a step change in the FFC can mean that the annual maxima are not represented well by a GEV distribution. For example, in the model setups with low storage capacity and light-tailed rainfall, some simulated annual maximum flood peaks show a kind of S shape with a step change in a low return period and a confined increase in flood peaks with increasing return periods beyond this. Such a shape of the FFC cannot be represented by a GEV distribution, and so the fitted distributions overestimate the flood peaks with high return periods. This shows that GEV distributions can have a poor fit when a process shift is present. Nevertheless, GEV distributions are commonly used in hydrological practice, e.g. for the estimation of design floods. In conclusion, the pattern of the GEV shape parameter versus the average storage capacity that we found is most likely linked to the distribution fitting and only indirectly to hydrological processes.

For some small catchments, running the model at an hourly instead of daily resolution would have been more appropriate as the concentration times might be sub-daily. However, this would have increased the computational costs drastically. For the weather generator especially, generating time series of 7000 years for the given setups at an hourly resolution did not seem feasible. Further, a higher temporal resolution would have limited the data available for setting up and calibrating the weather generator. With the aim of balancing accuracy and computational feasibility, the weather generator and rainfall-runoff model were run at a daily scale, while the data were disaggregated to a higher temporal resolution for the river routing.

The findings from this study are based on synthetic catchments and simulation runs. This has the great advantage that much longer time series can be generated than are usually available from observations. This allows a more robust estimation of the tail behaviour as the sampling uncertainty of the GEV shape parameter decreases with increasing sample size (Wietzke et al., 2020). However, results from simula-

tion runs are first of all representative of the simplified world represented by the models and are not necessarily transferable to the real world. For example, in our setup, we only considered how locally or widely saturation excess runoff is triggered to represent the spatial variability of runoff generation. In a real catchment, multiple flow paths and runoff components might be activated during extreme events. As with all models, the rainfall-runoff model that we use is a simplified representation of reality and is not able to represent all potential runoff generation processes. Nevertheless, the findings based on simulated time series can still give us valuable insights into how the analysed processes affect the tail behaviour of flood peak distributions. This is particularly the case as the different parts of the simulation model chain have been shown to represent real-world behaviour well when calibrated with real-world data (e.g. Nguyen et al., 2021; Ceola et al., 2015; Parajka et al., 2007).

5 Conclusions

Rainfall characteristics and runoff generation processes can affect the tail behaviour of flood peak distributions. Here, we analysed how the spatial variability of rainfall and runoff generation influences flood peak tail behaviour and whether and how this interacts with the sizes of catchments. To address these questions, a simulation-based approach was used: a model chain consisting of a weather generator, a rainfall-runoff model, and a river routing routine was set up for a large, synthetic catchment. Different configurations of the models were designed to represent varying degrees of spatial variability of rainfall, varying tail behaviours of the rainfall distributions, varying mean catchment storage depths, and varying degrees of spatial variability in the runoff generation. With these setups, 7000 years of discharge were simulated, generalized extreme value (GEV) distributions were fitted, and their tail behaviour was analysed. This was done for 163 catchments ranging between 200 and 30 000 km² in size.

We found that the GEV shape parameter decreases with increasing catchment size, meaning that smaller catchments tend to have flood peak distributions with heavier tails. Independent of the catchment size, a rainfall distribution with a heavier tail results in a flood peak distribution with a heavier tail. Further, the shape parameter of flood peak distributions was found to decrease with increasing spatial variability of the rainfall, especially for large catchments. This is most likely linked to the flow attenuation effects in large catchments through which local flood peaks are balanced out on their way to the catchment outlet. With regards to runoff generation, we found no clear effect on the flood peak tail behaviour, depending on whether saturation excess runoff usually occurs locally or widely in a catchment. In contrast, the average depth of the catchment storage seems to have a non-linear effect on the GEV shape parameter of flood peak dis-

tributions. These results suggest that how frequently saturation excess runoff is triggered has a stronger effect on the tail behaviour of flood peak distributions than how locally or widely this happens. However, the identified effect of the mean storage capacity on the GEV shape parameter might be to some degree related to aspects of the distribution fitting. When process shifts are present in a catchment, the flood frequency curve might show a step change, and as a result the flood peaks might not be represented well by a GEV distribution. This should always be kept in mind when using GEV distributions for the estimation of design floods.

Overall, the spatial variability of rainfall shows a much stronger effect on the tail behaviour of flood peak distributions than the spatial variability of runoff generation. The effect of spatially variable rainfall is closely interlinked with the catchment size, and attenuating effects in large catchments are assumed to lead to lighter tails. The findings are based on simulation runs so that future studies are required to validate the findings in real-world catchments.

Code and data availability. The code of the regional weather generator is available upon request (viet.dung.nguyen@gfz.de). The TUW rainfall-runoff model is available as an R package (<https://CRAN.R-project.org/package=TUWmodel>, Viglione and Parajka, 2020). The observational data from the weather station in Bamberg can be obtained from the Climate Data Centre of the Deutsche Wetterdienst (https://opendata.dwd.de/climate_environment/CDC/observations_germany/climate/; DWD, 2022).

Author contributions. BM, SV, and EM conceptualized the study. BM and SV supervised the study. EM performed the simulations and formal analysis with contributions from DN. EM prepared the manuscript with contributions from all the co-authors.

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