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Supplement of

Using altimetry observations combined with GRACE to select parameter sets of a hydrological model in a data-scarce region

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Supplements

1 Background on the altimetry data from LEGOS

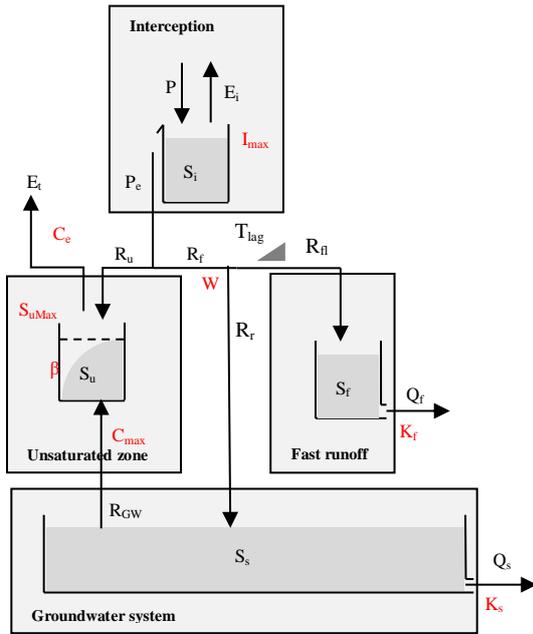
5 The altimetry data obtained from LEGOS come from the acquisitions of ENVISAT and Jason-2 radar altimetry missions on their nominal orbit (03/2002–10/2010 and 06/2008–10/2016 respectively). All the parameters necessary to estimate water levels (Crétau et al., 2017) are contained in the Geophysical Data Records (GDR) made available by the space agencies. These data were obtained from Centre de Topographie des Océans et de l'Hydrosphère (CTOH - <http://ctoh.legos.obs-mip.fr>). Ranges used to derive altimeter heights are those processed using OCOG/Ice retracking algorithm (Wingham et al., 1986). Previous studies showed that altimeter heights
10 derived using this retracking algorithm are more suitable for hydrological studies in terms of accuracy of water levels and availability of the data (Frappart et al., 2006; Santos da Silva et al., 2010; Sulistioadi et al., 2015) among the commonly available retracked data present in the GDRs.

The Multi-mission Altimetry Processing Software (MAPS) was used to visualize and process the altimetry data in order to obtain the virtual stations (VS) at the cross-sections between the altimeter ground tracks and the rivers
15 (Frappart et al., 2015; Normandin et al., 2018). Data processing is composed of three main steps: (i) a coarse delineation of the VS using Google Earth; (ii) a refined selection of the valid altimetry data based on visual inspection; and (iii) the computation of the time series of water level. The altimetry-based water level is computed for each cycle using the median of the selected altimetry heights, along with their respective deviation (i.e., mean absolute deviation). This process is repeated each cycle to construct the water level time series at the
20 virtual stations; see Frappart et al., 2015; Normandin et al., 2018 for more details.

Literature

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45 2 Model equations, parameter ranges and constrains



50 Figure S1: Model structure. Parameters are marked in red, storages and fluxes in black. Symbol explanation: **Fluxes** [mm d⁻¹]: precipitation (P), effective precipitation (P_e), potential evaporation (E_p), interception evaporation (E_i), plant transpiration (E_t), infiltration into the unsaturated zone (R_u), drainage to fast runoff component (R_f), delayed fast runoff (R_n), groundwater recharge (R_r), upwelling groundwater (R_{GW}), fast runoff (Q_f), groundwater/slow runoff (Q_s), total runoff (Q_m). **Storages** [mm]: storage in interception reservoir (S_i), storage in unsaturated root zone (S_u), storage in groundwater/slow reservoir (S_s), storage in fast reservoir (S_f). **Parameters**: interception capacity (I_{max}) [mm], maximum upwelling groundwater (C_{max}) [mm d⁻¹], maximum root zone storage capacity (S_{uMax}) [mm], splitter (W) [-], shape parameter (β) [-], transpiration coefficient (C_e) [-], time lag (T_{lag}) [d], reservoir time scales [d] of fast (K_f) and slow (K_s) reservoirs.

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Table S1: Model parameter values and ranges. See Figure S1 for the parameter explanation and Table S2 for the parameter constrains applied during the random parameter generation.

Landscape class	Parameter	min	max	Unit
Entire catchment	K_s	100	100	d
	C_e	0.5	0.5	-
Plateau/Terrace	I_{max}	0	2	mm d ⁻¹
	S_{umax}	200	2000	mm
	K_f	10	12	d
	W	0.1	0.5	-
Hillslope	I_{max}	0	2	mm d ⁻¹
	S_{umax}	200	2000	mm
	β	0	2	-
	T_{lag}	1	5	d
	K_f	10	12	d
Wetland	W	0.1	0.5	-
	I_{max}	0	2	mm d ⁻¹
	S_{umax}	200	2000	mm
	K_f	10	12	d
	W	0.1	0.5	-
River profile	C_{max}	0.1	2	mm d ⁻¹
	v	0.01	5.0	m s ⁻¹
	k	5	45	m ^{1/3} s ⁻¹
	a	0.1	800	m ³ s ⁻¹
	b	1	3	-

Table S2: Parameter constrains. See Figure S1 for the parameter explanation.

Parameter	Constrain
Maximum root zone storage capacity	$S_{umax,hillslope} > S_{umax,plateau/terrace}$ $S_{umax,hillslope} > S_{umax,wetland}$
Maximum interception	$I_{max,hillslope} > I_{max,plateau/terrace}$ $I_{max,hillslope} > I_{max,wetland}$
Splitter for groundwater percolation	$W_{hillslope} > W_{plateau/terrace}$

3 Characteristics of the virtual stations

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Table S3: Characteristics of the virtual stations in the Luangwa River basin for which remotely sensed river water levels are available: station ID, coordinates (X, Y), river slope (i), river width (B), river bank slopes (i_1 and i_2), upstream catchment area, acquisition date of the image in Google Earth used to extract the river geometry information, and discharge at Luangwa Bridge gauge station (basin outlet; absolute values and relative to the maximum discharge); in the absence of discharge data on the acquisition dates, the long-term mean daily values for the entire time period available were used.

VS	X	Y	i [-]	B [m]	i_1 [-]	i_2 [-]	A [m ²]	Acquisition date	Q_{absolute} [m ³ s ⁻¹] (Q_{relative} [%])
1	30.2823°	-14.8664°	0.00049	324	36	29	10211995771	13-9-2010	68 (1%)
2	30.0864°	-14.366°	0.00062	7	17	83	14859805930	13-10-2013	65 (1%)
3	32.1715°	-12.4123°	0.00019	3	19	42	44337218380	17-12-2013	211 (4%)
4	31.1868°	-13.5927°	0.00020	129	42	8	87227195673	5-6-2013	160 (3%)
5	31.6984°	-13.2039°	0.00020	185	31	20	78090945429	20-9-2013	60 (1%)
6	32.2998°	-12.2007°	0.00039	170	30	17	40935244516	13-6-2013	146 (3%)
7	32.2805°	-12.1157°	0.00030	78	38	77	40747298483	13-6-2013	146 (3%)
8	32.831°	-11.3674°	0.00031	10	48	21	21066101487	26-9-2013	97 (2%)
9	30.2704°	-14.8809°	0.00017	99	8	5	102140213550	14-11-2009	30 (1%)
10	31.78405°	-13.0995°	0.00029	100	26	20	77559639645	26-7-2013	89 (2%)
11	31.71099°	-13.1943°	0.00020	54	34	30	78051272962	20-9-2013	60 (1%)
12	30.2740°	-14.8763°	0.00017	82	8	15	102135928406	14-11-2009	30 (1%)
13	32.15843°	-12.412°	0.00019	87	43	30	44340963341	17-12-2013	211 (4%)
14	32.15989°	-12.4127°	0.00019	128	83	19	44339840479	13-6-2013	146 (3%)
15	30.2740°	-14.8763°	0.00017	82	8	15	102139379771	13-6-2013	146 (3%)
16	32.16056°	-12.4125°	0.00019	128	83	19	44339840479	17-12-2013	211 (4%)
17	31.80001°	-13.0909°	0.00029	86	21	83	77553414963	13-6-2013	146 (3%)
18	30.61577°	-14.1852°	0.00051	227	24	20	96231647197	20-9-2014	60 (1%)
Outlet	30.21491°	-14.96678°	0.00037	149	8.62	10.10	154325857000	26-7-2016	89 (2%)

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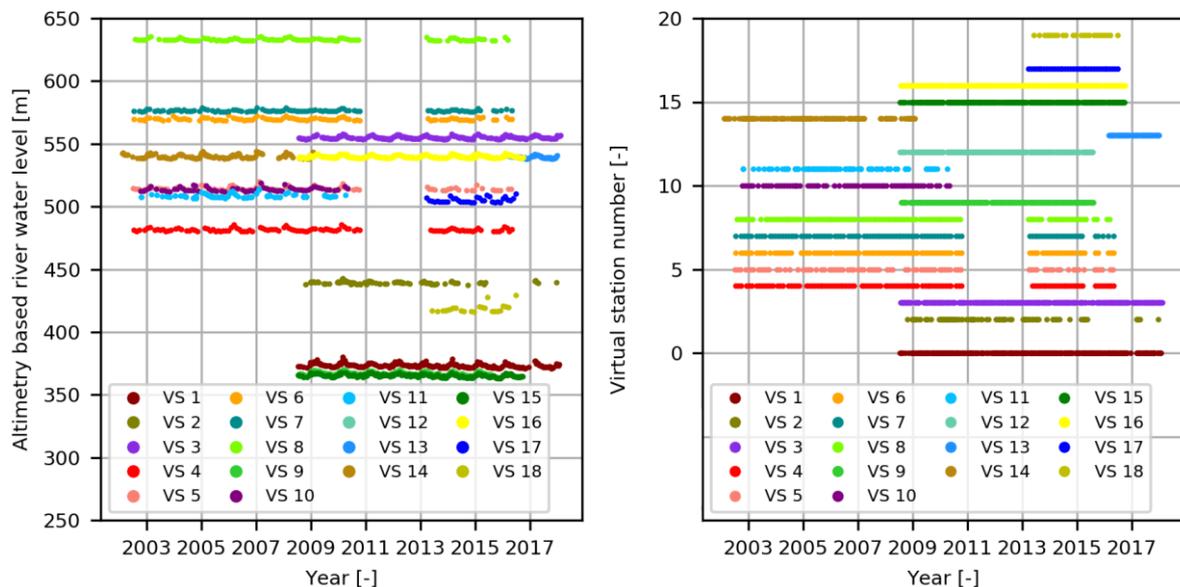


Figure S2: Visualisation of the altimetry time series relative to a reference ellipsoid (left) and altimetry data availability (right) for all virtual stations used in this study. The colours for the individual stations correspond with those in Figure 1 and 3.

80 **4 Influence of the number of good virtual stations used for calibration/validation**

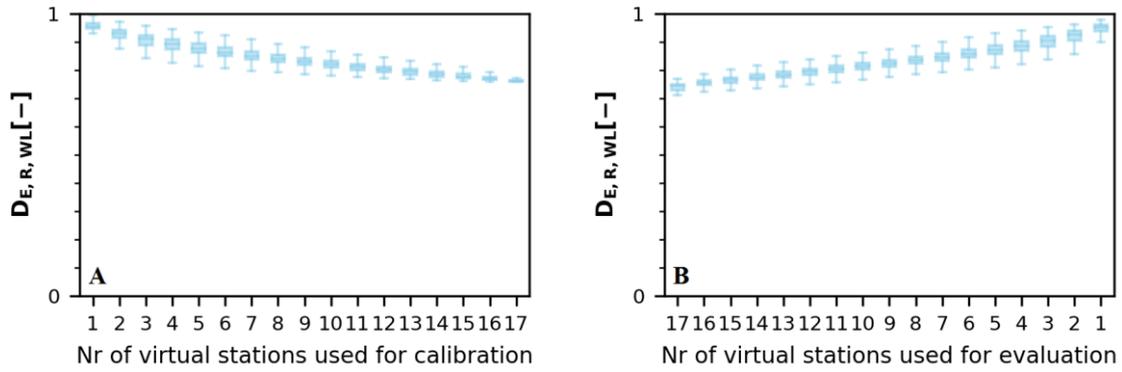
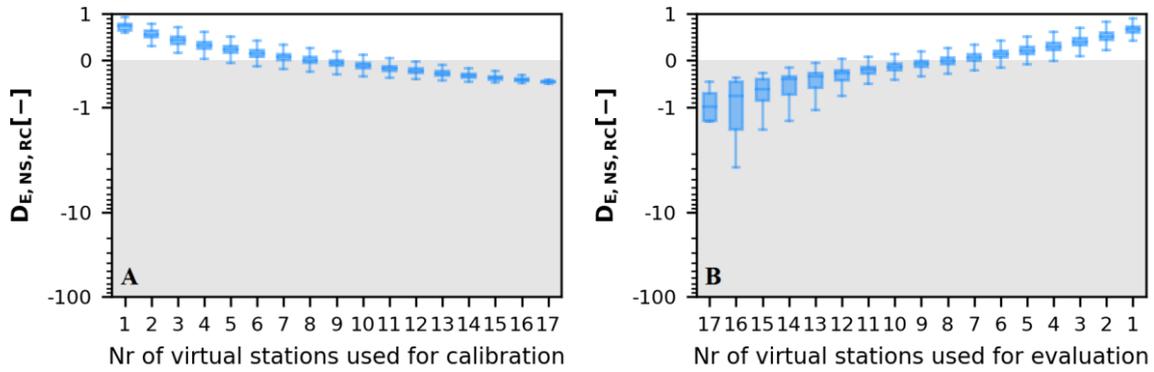


Figure S3: Influence of the number of virtual stations used for A) model calibration and B) evaluation on the model performance $D_{E,R,WL}$ applying Altimetry Strategy 1.



85 Figure S4: Influence of the number of virtual stations used for A) model calibration and B) evaluation on the model performance $D_{E,NS,RC}$ applying Altimetry Strategy 2.

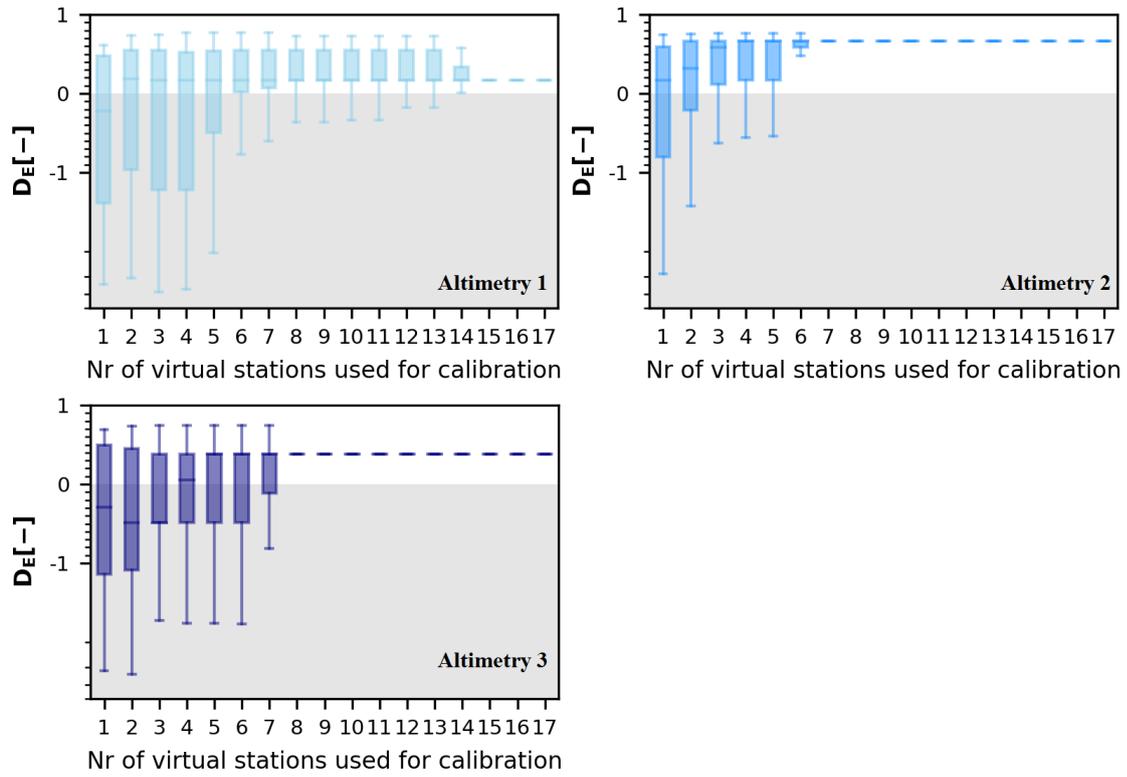


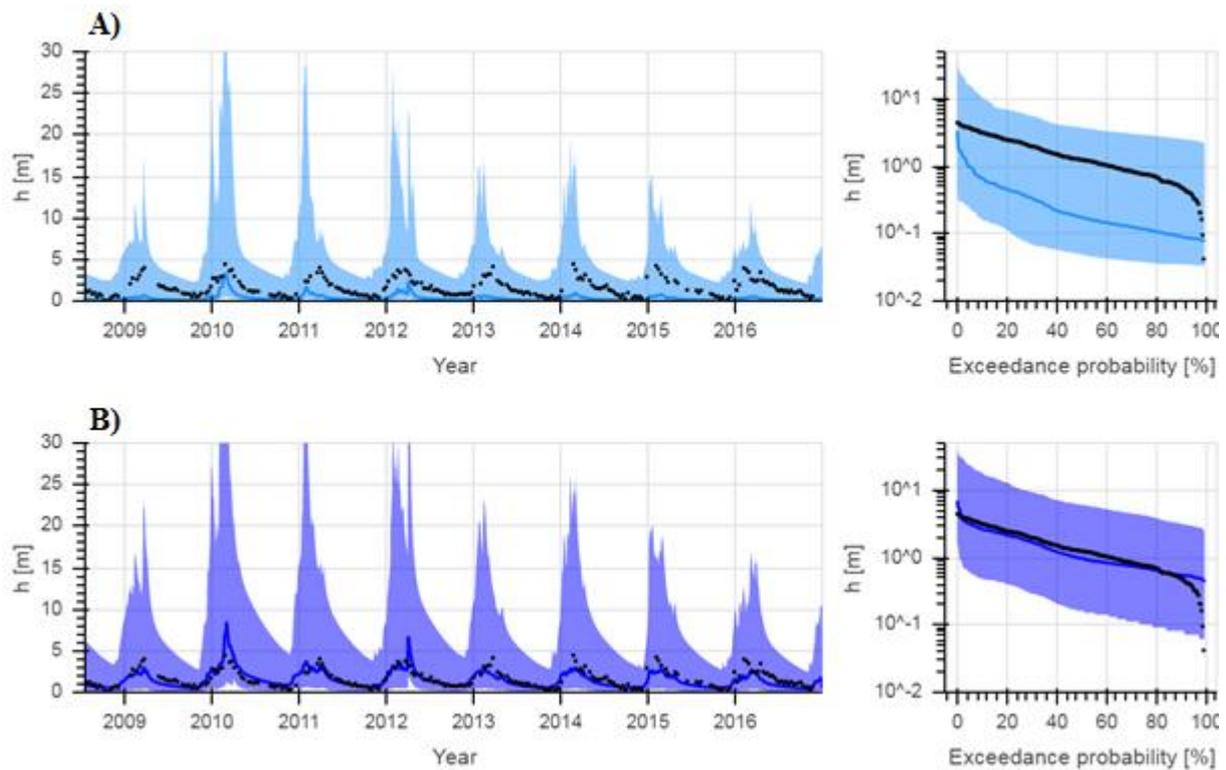
Figure S5: Influence of the number of virtual stations used for model calibration on the model performance D_E with respect to discharge

5 Model performance with respect to discharge

Table S4: Model performance with respect to each flow signature separately ($E_{NS,Q}$, $E_{NS,\log Q}$, $E_{NS,FDC}$, $E_{NS,\log FDC}$, $E_{R,RCdry}$, $E_{R,RCwet}$, $E_{NS,AC}$, $E_{R,RLD}$) for each parameter identification strategy.

	$E_{NS,Q}$	$E_{NS,\log Q}$	$E_{NS,FDC}$	$E_{NS,\log FDC}$	$E_{R,RCdry}$	$E_{R,RCwet}$	$E_{NS,AC}$	$E_{R,RLD}$
Discharge	0.78 (0.68 – 0.76)	0.56 (0.61 – 0.78)	0.95 (0.81 – 0.97)	0.88 (0.80 – 0.97)	0.08 (0.11 – 0.97)	0.67 (0.61 – 0.84)	0.94 (0.89 – 0.97)	0.73 (0.29 – 0.75)
Seasonal water storage	-1.38 (-2.2 – -0.05)	0.09 (0.11 – 0.73)	-0.80 (-1.6 – 0.40)	0.25 (0.27 – 0.93)	0.52 (0.45 – 0.97)	0.27 (0.24 – 0.36)	0.98 (0.97 – 0.99)	0.61 (0.14 – 0.79)
Altimetry Strategy 1	0.65 (-2.9 – 0.08)	0.69 (0.20 – 0.69)	0.93 (-2.0 – 0.68)	0.85 (0.37 – 0.89)	0.87 (0.42 – 0.81)	0.64 (0.22 – 0.44)	0.92 (0.97 – 0.99)	0.15 (0.10 – 0.46)
Altimetry Strategy 2	-0.31 (-2.5 – 0.27)	0.26 (-0.12 – 0.66)	0.10 (-1.9 – 0.73)	0.41 (0.05 – 0.88)	0.55 (0.38 – 0.89)	0.34 (0.23 – 0.46)	0.99 (0.97 – 0.99)	0.51 (0.11 – 0.70)
Altimetry Strategy 3	0.61 (-0.30 – 0.50)	0.70 (0.45 – 0.78)	0.95 (0.16 – 0.88)	0.91 (0.65 – 0.99)	0.93 (0.54 – 0.98)	0.60 (0.34 – 0.54)	0.99 (0.98 – 0.99)	0.52 (0.29 – 0.79)
Water level Strategy 1	0.65 (-0.49 – 0.60)	0.74 (0.37 – 0.75)	0.97 (0.13 – 0.95)	0.94 (0.593 – 0.98)	0.83 (0.52 – 0.98)	0.64 (0.34 – 0.60)	0.98 (0.98 – 0.99)	0.76 (0.12 – 0.75)
Water level Strategy 2	0.14 (-1.2 – 0.50)	0.78 (0.53 – 0.77)	0.57 (-0.62 – 0.91)	0.98 (0.73 – 0.98)	0.64 (0.66 – 0.99)	0.40 (0.28 – 0.55)	0.98 (0.98 – 0.99)	0.57 (0.26 – 0.77)

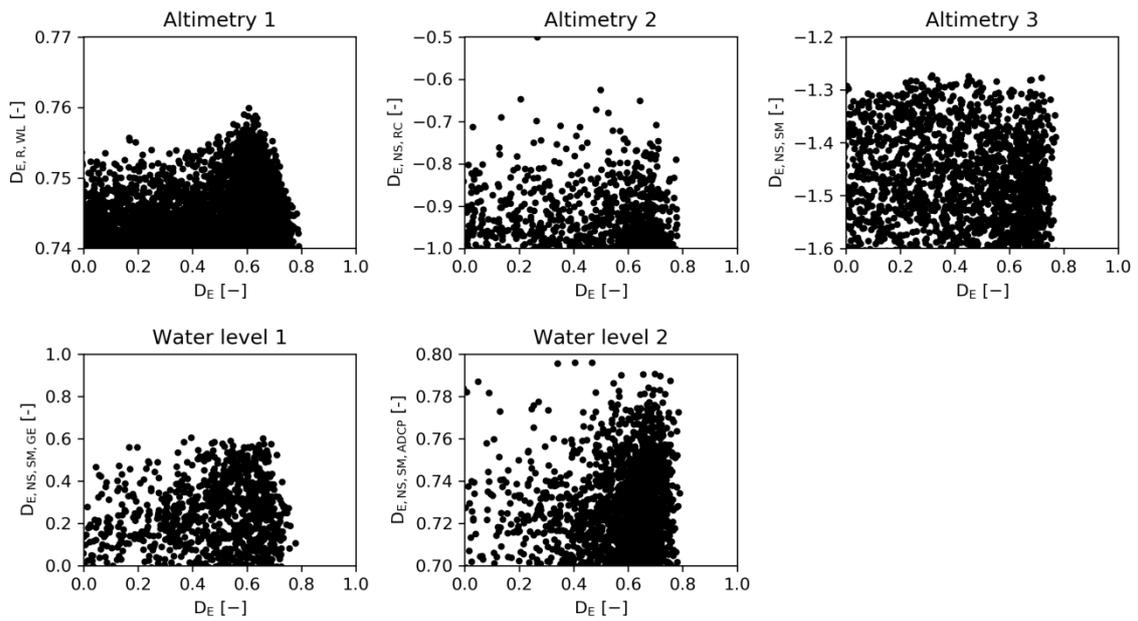
6 Model performance with respect to river water level



100 **Figure S6:** Range of model solutions for Virtual Station 4 (see Figure 1 for its location). The left panel shows the time series and the right panel the exceedance probability graph of the recorded (black) and modelled water level: the line indicates the solution with the highest calibration objective function and the shaded area the envelope of the solutions retained as feasible. Solutions retained as feasible based on altimetry observations using all virtual stations within the basin and A) calibrated rating curves for the discharge – water level conversion (Altimetry Strategy 2) or B) the Strickler-Manning equation with cross-section information retrieved from Google Earth (Altimetry Strategy 3).

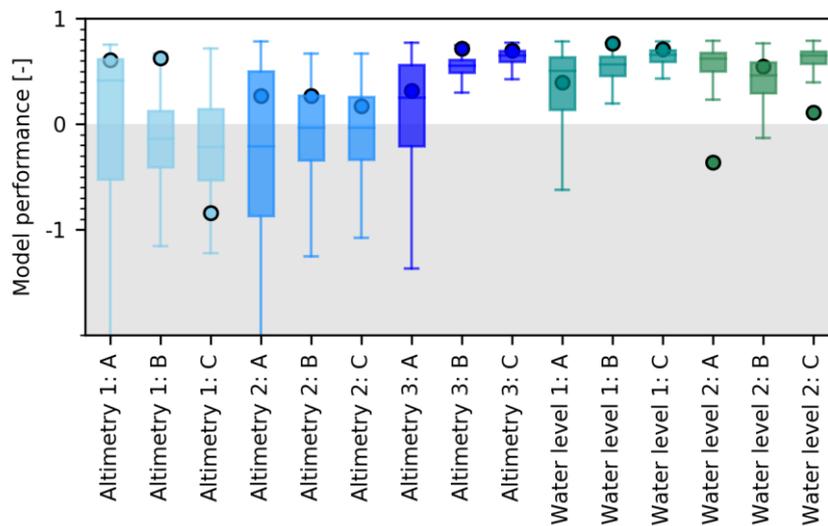
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7 Model performance comparison



110 **Figure S7: Model performance with respect to discharge (horizontal axes) vs. model performance with respect to (satellite based) river water level (vertical axes) for each calibration strategy**

8 Influence of the total water storage on the model performance



115 **Figure S8: Model performance with respect to discharge for each calibration strategy. Parameter sets were selected based on A) (satellite based) river water level only, B) first GRACE, then (satellite based) river water level, and C) first (satellite based) river water level, then GRACE**