



Supplement of

Dynamics of hydrological-model parameters: mechanisms, problems and solutions

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Introduction

This supporting information includes five sections that support the analysis. The 1 SCE-UA algorithm sections are used to support the 3.1 calibration schemes section in the main manuscript. The 2 Violin plot section is used to support the 5.2.1 A tool for convergence evaluation of dynamized parameters section in the main manuscript. The 3 evaluation results of model performance in Mumahe basin and Xunhe basin section is used to account for 4 results section in the main manuscript. The 4 Convergence performance in Mumahe basin and Xunhe basin and Xunhe basin section is used to supplement 5.2.2 Convergence assessment section in the main manuscript.

S1 SCE-UA

The shuffled complex evolution approach (SCE-UA), as an effective global optimization method, is a commonly used algorithm, because it is open source and was the first algorithm aimed specifically at calibrating hydrological models (Khakbaz and Kazeminezhad, 2012;Eckhardt and Arnold, 2001;Duan et al., 1994;Sorooshian et al., 1993). The technical details about

5 the SCE-UA can be shown in the flowchart (see Figure S1) (Duan et al., 1994). In the SCE-UA, the upper limit of the objective function evaluation is set to 10,000 times. All other settings of the SCE-UA technique are the default.



Figure S1. The flowchart of the SCE-UA algorithm (Duan et al., 1994; 1993; 1992).

S2 Violin plot

- 10 A violin plot is a combination of a Box Plot and a Density Plot showing more details of data distribution. As shown in Figure S2, the thick black bar in the center represents the interquartile range. The white dot represents the median. The thin black line is extended from the thick black bar and represents the 95% confidence intervals. On each side of the thin black line is a kernel density estimation to show the distribution shape of the data. Wider sections of the violin plot represent a higher probability that members of the population will take on the given value; the skinnier sections represent a lower probability (Hintze and
- 15 Nelson, 1998). The violin plots can exactly show the kernel density distribution, avoiding the overlapping traditional density plot occur to become difficult to identify. Moreover, unlike bar graphs with means and error bars, violin plots contain all data points, which makes them an excellent tool to visualize samples of small sizes. Violin plots are perfectly appropriate even if your data do not conform to normal distribution. They work well to visualize both quantitative and qualitative data.



Figure S2. Anatomy of a violin plot

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S3 Evaluation results of model performance in Mumahe basin and Xunhe basin

Table S1. Evaluation results of model performance for scheme 1 and scheme 5 in the Mumahe basin. The best performance is marked red.

	NSE	LNSE	RMSE_Q5	RMSE_Q20	RMSE_mid	RMSE_Q70	RMSE_Q95	
				Calibration				•
Scheme 1	0.691	0.445	0.953	0.357	0.118	0.554	0.909	
Scheme 5	0.324	0.262	0.362	0.070	0.112	0.288	0.729	
				Verification				•
Scheme 1	0.750	0.686	1.082	0.342	0.183	0.825	1.450	
Scheme 5	0.345	0.325	0.338	0.056	0.165	0.524	0.717	
			Ca	libration-verificatio	n			•
Scheme 1	0.059	0.241	0.129	-0.015	0.065	0.271	0.541	
Scheme 5	0.021	0.062	-0.023	-0.013	0.053	0.236	-0.013	

Table S2. The parameter sets of scheme 1 and scheme 5 in the Mumahe basin.

		$H_{ m uz}$	В	alpha	$K_{ m q}$	$K_{\rm s}$
Scheme 1		916.692	1.990	0.048	1.000	0.079
	Dry period	999.540	1.990	0.051	0.501	0.038
Scheme 5	Rainfall period I	999.998	1.900	0.010	0.713	0.143
	Rainfall period II	27.799	1.990	0.010	0.801	0.237
	Rainfall period III	644.639	1.990	0.010	0.501	0.090

Minimum Maximum

Table S3. Evaluation results of model performance for scheme 1 and scheme 5 in the Xunhe basin. The best performance is marked red.

NSE	LNSE	RMSE_Q5	RMSE_Q20	RMSE_mid	RMSE_Q70	RMSE_Q95	

Calibration									
Scheme 1	0.617	0.334	0.495	0.164	0.304	0.192	0.573		
Scheme 5	0.252	0.183	0.165	0.153	0.157	0.166	0.724		
Verification									
Scheme 1	0.683	0.478	0.616	0.271	0.322	0.091	0.674		
Scheme 5	0.253	0.258	0.186	0.071	0.076	0.092	0.292		
Calibration-verification									
Scheme 1	0.066	0.144	0.120	0.107	0.018	-0.100	0.101		
Scheme 5	0.001	0.074	0.021	-0.055	-0.081	-0.074	-0.432		

Table S4. The parameter sets of scheme 1 and scheme 5 in the Xunhe basin. The best performance is marked red.

		$H_{ m uz}$	В	alpha	$K_{ m q}$	Ks
Scheme 1		999.991	1.259	0.342	0.894	0.024
	Dry period	999.943	0.391	0.565	0.506	0.011
Scheme 5	Rainfall period I	988.154	1.602	0.031	1.000	0.112
Selfence 5	Rainfall period II	353.777	0.641	0.010	0.500	0.319
	Rainfall period III	456.369	0.418	0.104	1.000	0.121

Minimum Maximum



Figure S3. Fluxes assessment. All fluxes (including AE, OV, Q_q , Q_s , and Q_{sim}) for five schemes in the whole calibration period in Hanzhong basin.



Figure S4. State variables assessment. All state variables (including $XH_{UZ} XC_{UZ} X_{q1}, X_{q2}, X_{q3}$, and X_s) for five schemes in the whole calibration period in Hanzhong basin.



Figure S5. Fluxes assessment. All fluxes (including AE, OV, Q_q , Q_s , and Q_{sim}) for five schemes in the calibration period in Hanzhong basin.



Figure S6. State variables assessment. All state variables (including $XH_{UZ} XC_{UZ} X_{q1}, X_{q2}, X_{q3}$, and X_s) for five schemes in the calibration period in Hanzhong basin.



Figure S7. Fluxes assessment. All fluxes (including AE, OV, Q_q , Q_s , and Q_{sim}) for five schemes in the whole verification period in Hanzhong basin.



Figure S8. State variables assessment. All state variables (including $XH_{UZ} XC_{UZ} X_{q1}, X_{q2}, X_{q3}$, and X_s) for five schemes in the whole verification period in Hanzhong basin.

4 Convergence assessment in Mumahe basin and Xunhe basin



Figure S9. Convergence assessment. Convergence performance for scheme 1 and scheme 5 in Mumahe basin.



Figure S10. Convergence assessment. Convergence performance for scheme 1 and scheme 5 in Xunhe basin.

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