



# Spatial variability of mean daily estimates of actual evaporation from remotely sensed imagery and surface reference data

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**Abstract.** Land surface evaporation has considerable spatial variability that is not captured by point-scale estimates calculated from meteorological data alone. Knowing how evaporation varies spatially remains an important issue for improving parameterisations of land surface schemes and hydrological models and various land management practices. Satellite-based and aerial remote sensing has been crucial for capturing moderate- to larger-scale surface variables to indirectly estimate evaporative fluxes. However, more recent advances for field research via unmanned aerial vehicles (UAVs) now allow for the acquisition of more highly detailed surface data.

Integrating models that can estimate “actual” evaporation from higher-resolution imagery and surface reference data would be valuable to better examine potential impacts of local variations in evaporation on upscaled estimates. This study introduces a novel approach for computing a normalised ratiometric index from surface variables that can be used to obtain more-realistic distributed estimates of actual evaporation. For demonstration purposes the Granger–Gray evaporation model (Granger and Gray, 1989) was applied at a rolling prairie agricultural site in central Saskatchewan, Canada. Visible and thermal images and meteorological reference data required to parameterise the model were obtained at midday.

Ratiometric indexes were computed for the key surface variables albedo and net radiation at midday. This allowed point observations of albedo and mean daily net radiation to be scaled across high-resolution images over a large study region. Albedo and net radiation estimates were within 5 %–10 % of measured values. A daily evaporation estimate for a grassed surface was 0.5 mm (23 %) larger than eddy covari-

ance measurements. Spatial variations in key factors driving evaporation and their impacts on upscaled evaporation estimates are also discussed. The methods applied have two key advantages for estimating evaporation over previous remote-sensing approaches: (1) detailed daily estimates of actual evaporation can be directly obtained using a physically based evaporation model, and (2) analysis of more-detailed and more-reliable evaporation estimates may lead to improved methods for upscaling evaporative fluxes to larger areas.

## 1 Background and introduction

“Actual” evaporation is the water vapour physically transferred from a surface (e.g. plants, soil, or water) to the atmosphere over a given time period (e.g. hourly or daily). Reliable estimates of actual evaporation are often needed over large spatial scales for applications such as water resource management, agriculture, ecology, and forecast modelling of weather and climate. However, estimates (or measurements) are often calculated at point scales with footprints that can range from centimetres to several kilometres or more (Brutsaert, 1982). Consequently, point-scale footprints in heterogeneous landscapes may contain large variability that needs to be considered more appropriately.

From an ecological standpoint, heterogeneous landscapes are comprised of distinct topographic features, land cover types, biological attributes, and other physical properties that exhibit observable patterns in the order of metres (e.g. Yates et al., 2006; Zhang and Guo, 2007). Therefore, variable surface properties and state conditions exert a strong control on

local surface energy fluxes. As a result, “scaling” evaporation estimates over large areas must consider a potential loss of information due to upscaling processes. The potential impacts of spatial variability on larger-scale estimates of evaporation are still not well understood, and previous estimation and scaling methods have not examined this issue in detail.

For example, hydrologic and atmospheric modelling applications often require large- to regional-scale evaporation estimates, but the underlying variability is difficult to examine practically (e.g. Avvisar and Pielke, 1989; Baldocchi et al., 2005; Brutsaert, 1998; Claussen, 1991, 1995; Klaassen, 1992; Klaassen and Claussen, 1995). Courault et al. (2005) and Gowda et al. (2007) have also reviewed remote-sensing approaches which integrate surface images to derive key variables needed to parameterise various energy-balance-type evaporation models. This generally results in estimates at moderate scales of input images (e.g. Bisht et al., 2005). Purely empirical methods have also correlated evaporation with vegetation indices (e.g. Nagler et al., 2005).

A common remote-sensing method has been to calculate evaporation indirectly as a residual of a simplified energy balance (e.g. Jackson et al., 1977; Seguin et al., 1989; Busières et al., 1996). In such cases surface temperatures derived from thermal imagery is a critical input. More complex resistance-type formulations also exist based on developments by Monteith (1965), e.g. Norman et al. (1995), Anderson et al. (1997, 2007), Boegh et al. (2002) and Houborg and Soegaard (2004). However, such approaches are computationally intensive and parameterising the resistance terms is difficult without detailed data.

Colaizzi et al. (2006) reviewed scaling approaches based on an evaporative fraction determined through complex solar-radiation modelling. Mu et al. (2007) and Fisher et al. (2008) discuss advanced methods for deriving global-scale estimates based on expert knowledge and detailed data sets obtained from the AmeriFlux network in association with the global FLUXNET (Baldocchi et al., 2001). As an alternative to more complex methods, Granger (2000) integrated a complementary feedback approach with Penman’s combination model and remote-sensing imagery that can directly estimate actual evaporation, even in data-sparse regions.

Previous remote-sensing methods have been valuable for integrating generalised representations of moderate- to larger-scale variability. However, most methods fail to include fundamental interactions governing the evaporation process which can be more realistically captured with an energy balance and aerodynamic combination model approach. More importantly, few (if any) have addressed the issue of how detailed surface variability may impact upscaled evaporation estimates over larger areas. The acquisition of high-resolution imagery from a plane (or even unmanned aerial vehicles; UAVs) combined with new methods of obtaining detailed surface information could be valuable for examining the spatial variability of point-scale evaporation estimates.

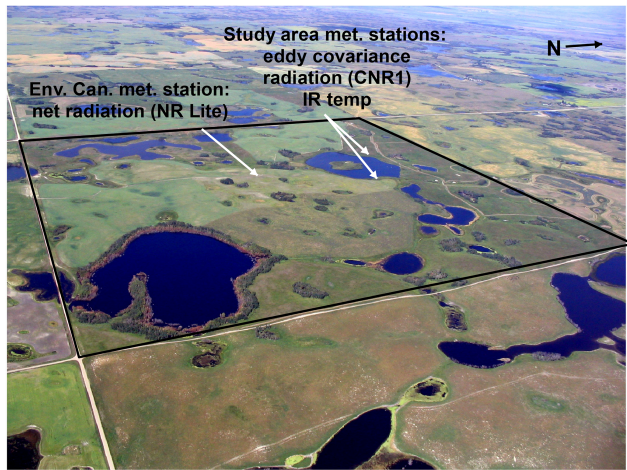
Such analysis could then help advance understanding how the underlying surface variability may impact upscaling of point evaporation estimates to larger areas.

The goal of this study is to examine the spatial variability of key surface variables driving point-scale evaporation estimates and their impact on upscaled evaporation estimates to larger areas, and this includes two objectives. The first is to use the spatial variability captured from high-resolution one-time-of-day visible and thermal images taken at midday to scale (i.e. distribute) energy-balance factors that drive combination evaporation models. This objective required the development of a scaling method that derives a radiometric index of surface variables from the midday images. The resulting information can then be used to distribute a measured value of mean daily net radiation which can be used as an input for deriving detailed estimates of evaporation. The second objective is to examine impacts of variations of the key surface variables on daily estimates of evaporation, including point-scale and larger areal estimates.

Methods applied here integrated high-spatial-resolution images with an initial pixel size of less than 5 m taken during a flight on 5 August 2007 over a rolling prairie agricultural landscape. It also included point measurements of surface reference data, a physically based evaporation model, and analysis using ArcGIS (v9.x) software. Estimates of mean daily actual evaporation were calculated with the Granger–Gray complementary feedback model (G–D) (1989). The model is a useful alternative to more complex methods that require resistance parameters and is well suited for a variety of Canadian environments (e.g. agricultural, prairie, and boreal).

## 2 Study area

A case study was conducted on 5 August 2007 at St. Denis National Wildlife Area (SDNWA) located in the parkland ecoregion of the Canadian Prairies in central Saskatchewan (see Armstrong et al., 2008). Figure 1 shows a photo of the study region taken during the study flight on 5 August to capture visible and thermal images from handheld cameras. The landscape was characterised by hummocky, gently rolling terrain and a few slopes of 1 %–10%. Elevations ranged from 540 to 565 m, and the land use consisted of mixed cool-season grasses, tall brome grass, cultivated land, and wetlands surrounded by trees or dense grass; all grasses and crops were C<sub>3</sub> types. The soil region is classified as dark-brown chernozem, and the soil texture is predominately silty loam (van der Kamp et al., 2003).



**Figure 1.** Photo of the study area at St. Denis National Wildlife Area taken during the flight on 5 August 2007 and locations of micrometeorological measurement stations.

### 3 Data and methods

#### 3.1 Granger–Gray evaporation model (G–D model)

Granger and Gray (1989) developed the G–D model from the complementary relationship of the combination model of Bouchet (1963) and Penman (1948). The G–D model extends the potential evaporation model to non-saturated surfaces using the relative evaporation term,  $G$ . This is defined as a ratio of actual to potential evaporation which depends on the relative drying power of the air,  $D$ . The underlying theory is based on the reduction of water availability as a surface dries, but the “potential” evaporation increases due to a subsequent rise in surface temperature.

The development of  $G$  eliminated the need for observations of surface temperature and vapour pressure. As a result, estimates of actual evaporation were obtainable for non-saturated surfaces with atmospheric data alone (Granger, 1989). The general form of the equation is

$$E = \frac{\Delta G (Q^* - Q_g) + \gamma G E_A}{\Delta G + \gamma}. \quad (1)$$

The available energy term is driven by net radiation,  $Q^*$  ( $\text{W m}^{-2}$ ), calculated as a sum of the net shortwave and longwave radiation components and the ground heat flux,  $Q_g$  ( $\text{W m}^{-2}$ ), and the slope of the saturation vapour pressure curve,  $\Delta$ .

The aerodynamic term includes the psychrometric constant,  $\gamma$ , and “drying power of the air”,  $E_A$ , calculated using a Dalton-type formula.

$$E_A = f(u) (e_a^* - e_a), \quad (2)$$

where  $f(u)$  is a vapour transfer function, and the atmospheric vapour pressure deficit at 2 m height is derived from

$e_a^*$  (saturated) and  $e_a$  (actual). Pomeroy et al. (1997) empirically derived  $f(u)$  as a function of wind speed and aerodynamic roughness length and  $Z_0$  (m) from extensive field data collected for prairie, boreal forest, and northern cold-region environments in western Canada.

$$f(u) = 8.19 + 22Z_0 + (1.16 + 8Z_0)u, \quad (3)$$

where  $u$  is the mean daily wind speed ( $\text{m s}^{-1}$ ).

The G–D complementary feedback method is driven by the non-linear relationship between  $G$  and the relative drying power of the air,  $D$ .

$$G = \frac{1}{0.793 + 0.2e^{4.902D}} + 0.006D, \quad (4)$$

where  $D$  is a function of the humidity deficit and available energy is given by

$$D = \frac{E_A}{E_A + \frac{(Q^* - Q_g)}{\lambda}}, \quad (5)$$

and  $\lambda$  is the latent heat of vaporisation ( $\text{kJ kg}^{-1}$ ).

The feedback model approach is generally applicable for regions indicated above and can be used when detailed soil moisture information is lacking, except under conditions of severe moisture stress. Armstrong et al. (2008) evaluated point-scale evaporation estimates obtained with the G–D model over mixed grasses at the same study area under conditions of non-limiting soil moisture using field data collected during 2006. Estimates obtained with the G–D model compared well with eddy covariance (EC) measurements and was less data intensive than the Penman–Monteith model, which also performed well in that study.

Armstrong et al. (2010), however, found that the use of appropriate soil moisture constraints was required to obtain reliable estimates with the G–D model when applied under drought conditions to a mixed-prairie site at Lethbridge, Alberta, Canada.

#### 3.2 Field observations

Inputs needed to parameterise Eqs. (1)–(5) included mean daily net radiation, air temperature, humidity, wind speed, and surface roughness length. Outgoing radiation components were derived from high-resolution digital (Canon PowerShot A70 camera) and thermal (FLIR ThermoCAM P20 imaging radiometer) images taken on 5 August 2007 during a Cessna flight at midday. Meteorological and surface observations (radiation components, temperature, humidity, and wind speed) were recorded at two station locations. Figure 1 shows the relative locations, which included one reference site and one validation site. An independent station operated by the National Water Research Institute (Environment Canada, Saskatoon) was also available which provided a second validation site for estimates of daily net radiation.

Air temperature, humidity, wind speed, incoming radiation, and surface temperature were recorded as 15 min averages. Incoming and outgoing shortwave and longwave radiation were measured with a CNR1 net radiometer (Kipp & Zonen, Delft, the Netherlands). Air temperature and humidity were measured at 2 m height using a shielded Vaisala HMP45C (Campbell Scientific, Inc., Logan, Utah, USA). A shielded Exergen infrared (IR) temperature sensor (IRTC; Exergen, Watertown, Massachusetts, USA) was used to measure surface temperature.

Canopy spectral reflectance was independently sampled on 21 August 2007 for validating albedo estimates derived from the visible images taken on 5 August. Canopy reflectance was collected according to the methods of Disney et al. (2004) and Zhang and Guo (2007). Samples were taken at 4.5 m intervals along a site transect at 1 m height at the nadir (25° field of view) with an ASD FR Pro spectroradiometer (Analytical Spectral Devices, Inc., Boulder, Colorado, USA); the spectral range was 350–2500 nm with a 1 nm resolution. Samples were taken between 12:00 LT (local time) and solar noon. Reflectance was recalibrated every 10 min using a white Spectralon reflectance panel (Labsphere Inc., North Sutton, New Hampshire, USA).

Eddy covariance observations were sampled at approximately 2 m height with a CSAT3 three-dimensional sonic anemometer (Campbell Scientific, Inc., Logan, Utah, USA) and a KH20 ultraviolet krypton hygrometer (Campbell Scientific, Inc., Logan, Utah, USA). The raw EC data were reported as 15 min averages and post-processing was done with MATLAB (Mathworks, Natick, Massachusetts, USA) which included flux corrections using a standard planar-fit axis rotation algorithm (Wilczak et al., 2001). Data filtering indicated there were no missing or bad data values on the study day, and station positioning was not considered to be an issue. EC data collected at the validation site were used for a comparison against a mean estimate obtained from the G–D model upwind of the EC station.

Given the higher frequency of flux reporting (15 min averages), axis rotation, and data filtering applied, and a potential mismatch in measurement footprints, no further corrections were used to force an energy balance closure on the 15 min averages.

### 3.3 Surface reference meteorological parameters

At midday, reference observations of the shortwave,  $K \downarrow$  ( $835 \text{ W m}^{-2}$ ), and longwave,  $L \downarrow$  ( $320 \text{ W m}^{-2}$ ), irradiance and albedo (0.153 over grass) were obtained from the CNR1. Both  $K \downarrow$  and  $L \downarrow$  were assumed to be uniform over the field given the images used for calculations were cloud free. The reference values were used in the calculation of midday normalised radiometric indexes for albedo and net radiation. A mean daily reference value of  $155 \text{ W m}^{-2}$  was obtained for  $Q^*$  which was the input for distributing the final esti-

mates of the mean daily net radiation using the radiometric index (discussed in Sect. 3.4).

The daily ground heat flux measured at two locations was relatively small, 8 and  $2 \text{ W m}^{-2}$ , due to the continuous and tall grass canopy cover. For this study the ground heat flux was ignored, in part due to the small measured values, but this was also to limit errors introduced from using a numerical solution to estimate ground heat flux, which would require more-detailed cover information at each image pixel. To standardise the parameterisation of the G–D model for calculating the mean daily estimates of evaporation, the reference values of mean daily air temperature ( $19.6^\circ\text{C}$ ), humidity deficit (1.1 kPa), and wind speed ( $3 \text{ m s}^{-1}$ ) were also taken to be uniform. Differences in mean daily air temperature between the measurement locations were approximately  $1^\circ\text{C}$ .

Potential impacts of assuming uniform humidity and wind speed for parameterising the aerodynamic term was also considered. This was done by examining G–D evaporation estimates derived from 2006 field data collected over different surfaces at the same study area (Armstrong et al., 2008). During 2006 a fixed station obtained continuous measurements over a mixed-grass upland, and a portable EC station was moved periodically to obtain concurrent measurements over different land covers. Meteorological observations from the fixed station were initially used to estimate evaporation with the G–D model. Another estimate was obtained after substituting observations of humidity and wind speed taken from the portable EC station. This resulted in only minor variations in the respective evaporation estimates (root mean square deviation (RMSD) of 0.02 mm) derived from the concurrent measurements of humidity and wind speed taken from the different sites.

Implications of neglecting the ground heat flux and treatment of the meteorological parameters (above) with respect to modelling uncertainty are given in the discussion.

### 3.4 Deriving key surface variables from one-time-of-day images

#### 3.4.1 Theoretical basis for a normalised radiometric index for surface properties

Remotely sensed images contain valuable information that characterise highly variable surface properties (e.g. reflectance, temperature, RGB (red–green–blue) and greyscale digital numbers (DNs), etc.). Theoretically, relative variations in these properties can be quantified using a “normalised” radiometric index. For example, consider the “evaporation ratio” ( $E_R$ ), defined simply as the ratios of individual evaporation rates at different spatial locations ( $E_i$ ) to a reference rate obtained at a specified location ( $E_{\text{ref}}$ ).

$$E_R = \frac{E_i}{E_{\text{ref}}} \quad (6)$$

At the reference location  $E_R$  is 1 and will be the same at any other locations where  $E_i = E_{\text{ref}}$ , but it will vary from unity at all other spatial locations.

For obvious reasons the theory integrates well for computations with pixel-based images. Subsequently, an evaporation rate measured at the reference pixel could be scaled to all other pixels by multiplication with the value of  $E_R$  at each pixel. The concept may be extended to other surface variables (e.g. albedo, net radiation, etc.) required to parameterise an evaporation model.

### 3.4.2 Distributing surface variables using a normalised index of relative surface ratios

Methods described here assume spatial variations in surface variables driving net radiation (and driving evaporation) are near their maximum around solar noon. This is likely to be valid within 2 h from the actual time of solar noon (Colaizzi et al., 2006). Net radiation is the major component needed to determine available energy for the conversion of water to an equivalent depth of water vapour. Net radiation is determined from the shortwave and longwave radiation components measured in the electromagnetic spectrum between approximately 0.3 and 4 and 4 and 14  $\mu\text{m}$ , respectively (Zoran and Stefan, 2006).

Traditionally, radiative terms needed for estimating evaporation are derived from satellite-based imagery, e.g. Landsat, AVHRR (Advanced Very High Resolution Radiometer), and MODIS (Moderate Resolution Imaging Spectroradiometer). However, satellite-based methods are often limited by cloud contamination, varying spatial and temporal resolutions, and sensor footprint mismatches. Under clear skies it can be assumed shortwave and longwave irradiance are uniform over an agricultural field area. Very-high-resolution images taken near the surface could be used to derive the much more variable surface-reflected shortwave and emitted longwave radiation components.

For example, normalised radiometric indexes for albedo,  $\alpha_R$ , emitted longwave,  $L\uparrow_R$ , and roughness length,  $Z_{0R}$ , can be calculated at every pixel location within visible and thermal images using

$$\alpha_R = \frac{\alpha_i}{\alpha_{\text{ref}}}, \quad (7)$$

$$L\uparrow_R = \frac{L\uparrow_i}{L\uparrow_{\text{ref}}}, \quad (8)$$

$$Z_{0R} = \frac{Z_{0i}}{Z_{0\text{ref}}}, \quad (9)$$

where the subscript “i” is an individual value at each pixel and “ref” is the value at the reference pixel. Incoming shortwave ( $K\downarrow$ ) and longwave radiation ( $L\downarrow$ ) components can reasonably be assumed to be uniform over the field under clear skies, so  $\alpha_R$  and  $L\uparrow_R$  can be further integrated to derive a radiometric index of the midday net radiation,  $Q_R^*$ .

$$Q_R^* = \frac{Q_i^*}{Q_{\text{ref}}^*} = K\downarrow(1 - \alpha_R\alpha_{\text{ref}}) + L\downarrow - L\uparrow_R L\uparrow_{\text{ref}} \quad (10)$$

Subsequently, single measured values of albedo and mean daily net radiation taken at a reference pixel can be scaled (i.e. distributed) across all other pixels via multiplication with the surface ratios derived for  $Q_R^*$ . The next section illustrates the indexing method for deriving accurate estimates of albedo.

### 3.4.3 Radiometric-index method for albedo estimates from digital visible images

Surface albedo ( $\alpha$ ) represents a crucial radiation loss term for radiative transfer calculations and surface–atmosphere energy and mass exchanges (Sellers et al., 1997; Liang, 2000; Lucht et al., 2000; Roberts, 2001; Liang et al., 2003; Disney et al., 2004). Its calculation can be complex and is typically a major source of uncertainty (Yang et al., 2008).

In this case, a measured value of broadband albedo obtained at a reference pixel location could be scaled to every other pixel within a high-resolution visible image. In 2007, digital photos were taken with a Canon PowerShot A70 camera with a maximum resolution of  $2048 \times 1536$  pixels, a CCD (charge-coupled device) imager, and a DIGIC (Digital Imaging Core) processor. This resulted in very-high-resolution ( $< 1$  m pixels) “visible images” without cloud cover issues.

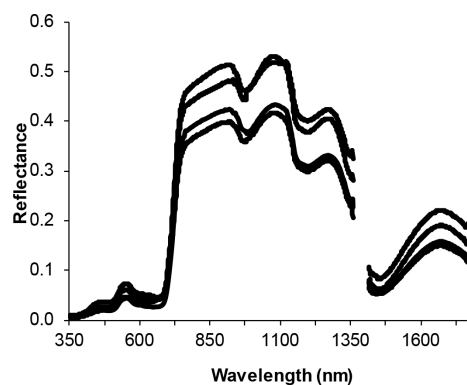
While digital cameras may not cover the full visible and near-infrared spectrum of advanced measurement sensors, the imaging techniques are based on the same principles. Corripio (2004) demonstrated how accurate estimates of snow albedo could be obtained from digital images using a linear scaling technique applied to a measured albedo at a reference pixel location. A key step for our analysis was to transform an RGB digital photo to a single-band 8 bit greyscale image with DNs ranging from 0 to 255.

This resulted in higher DNs associated with more-reflective surfaces (i.e. brighter) and lower DNs with less-reflective surfaces (i.e. darker) in accordance with the principles for calculating albedo. The resulting albedo map was aggregated to a pixel size of 5 m for a practical analysis and georectified to 100 GPS ground control points. The study area included some dried wetlands and others containing open water. This allowed for application of a simple dark-object subtraction (DOS) method to correct potential atmospheric effects (Song et al., 2001; Liang, 2000).

Applying Eq. (11) made it possible to accurately estimate albedo at individual pixel locations,  $\alpha_i$ , from a measured broadband value taken at the reference location,  $\alpha_{\text{ref}}$ , and a radiometric index for DNs calculated at each pixel.

$$\alpha_i = \alpha_{\text{ref}} \frac{\text{DN}_i}{\text{DN}_{\text{ref}}}, \quad (11)$$





**Figure 2.** Reflectance spectra collected at four sample points over mixed-grassland vegetation at the upland area on 5 August 2007. Reflectance values affected by noise at corresponding wavelengths were removed.

where  $DN_i$  is the digital number of an individual pixel and  $DN_{ref}$  is the reference pixel value.

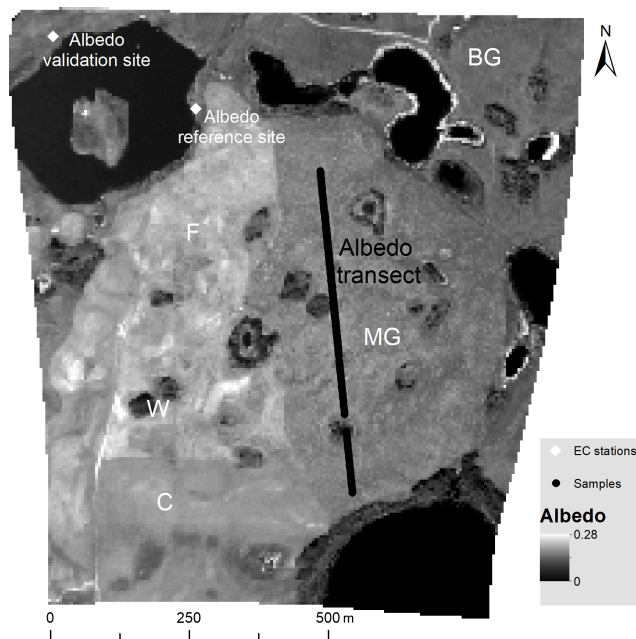
Angular measurements of broadband albedo from 0.3 to  $3.0\ \mu\text{m}$  with a hemispherical CNR1 directly accounted for bidirectional reflectance properties of the mixed grassed surface. Therefore, the point observations satisfied the bidirectional reflectance considerations related to albedo estimation techniques (Nicodemus et al., 1977; Lucht et al., 2000; Roberts, 2001).

Figure 2 shows a sample of measured reflectance values from a grassed upland area. The spectral reflectance from the mixed grasses was virtually identical to the response for healthy (green) winter wheat (see Disney et al., 2004). For wheat, they concluded reflectance was directionally invariant and reasonably could be assumed to behave as a Lambertian surface (i.e. scattering light equally in all directions). The field-measured spectral reflectance over the grassed surface was therefore treated similar to a Landsat-measured reflectance and divided into respective wavelengths for Landsat wavebands 1, 3, 4, 5, and 7.

An empirical linear approximation for narrow-to-broadband albedo conversion applicable to Landsat imagery (see Liang, 2000) was then applied to the field-measured spectral reflectance data. This allowed for a direct comparison of albedo estimates and measurements along the sampling transect shown in Fig. 3. Due to the 4.5 m sampling distance some pixels contained a single value, whilst others contained two values, in which case the mean value was used for comparison.

#### 3.4.4 Surface temperature (emitted longwave radiation)

For the case of surface temperatures the indexing method was not needed because high-resolution observations were obtained directly with a handheld forward-looking infrared (FLIR) ThermoCAM P20 imaging radiometer. The



**Figure 3.** Albedo map (5 m resolution) derived from visible images taken at midday. Also shown are the location of reference and validation sites; letter codes indicate major land cover types: fallowed (F), mixed grass (MG), brome grass (BG), cultivated (C), and wetlands (W).

P20 used a focal plane array uncooled microbolometer with a maximum image resolution of  $320 \times 240$  pixels, a  $24^\circ \times 18^\circ$  field of view, and a spatial resolution of 1.3 mrad. The spectral range was  $7.5\text{--}13\ \mu\text{m}$ , which is similar to traditional satellite sensors (e.g. Landsat, MODIS, and AVHRR with a spectral range of  $10\text{--}12.5\ \mu\text{m}$  and ASTER with a spectral range of  $8\text{--}12\ \mu\text{m}$ ).

A standard emissivity of 0.98 was assumed for the cover types encountered, and ambient air temperature and humidity and the distance between the surface and camera detector were set based on observations. The Stefan–Boltzmann equation was applied to transform surface temperatures into values of outgoing longwave radiation needed to estimate the net radiation. For the flight height of approximately 1 km the FLIR produced a surface pixel resolution of approximately 3 m. The longwave radiation map was then aggregated to a 5 m resolution and georectified using the resulting map of albedo estimates as the reference.

#### 3.4.5 Surface roughness length

The study area is characterised by a complex landscape with rolling terrain covered by tall grasses, cultivated land, and narrow rings of tall grasses, tall shrubs, or tall trees surrounding ponds and dried wetlands (see Fig. 1). Such surface characteristics (e.g. discontinuities and protrusions) are expected to produce variations in wind speed and turbulent

energy through interactions with the different surface types and roughness.

Variations in the aerodynamic roughness length,  $Z_0$ , and wind speed are important factors considered in the turbulent transfer function used for calculating the aerodynamic terms of the G–D model (Eqs. 2 and 3). Previous developments (e.g. Pomeroy et al., 1997) have considered boundary layer (friction velocity) and surface parameters (roughness length) estimated from EC measurements and wind profiles over boreal forests and Canadian Prairie land covers such as bare soil and  $C_3$ -type crop and grasses.

Due to the general surface complexity at the study area, roughness classes for  $Z_0$  were needed to adjust the vapour transfer function to reflect potential increases or decreases in turbulent exchanges as result of variations in surface properties and local roughness. For example, lower values of  $Z_0$  associated with fallowed areas and crops would imply increased wind speeds near the ground and a reduction in turbulent energy. In contrast, larger  $Z_0$  values associated with taller dense grasses, shrubs, and trees would effectively reduce wind speeds and increase turbulent exchanges.

For the purposes here, a roughness length classification map for  $Z_0$  was derived from the 8 bit grayscale image used for estimating surface albedo. This was achieved based on knowledge of the various land covers at the site and segmentation analysis using the IDRISI Kilimanjaro surface analysis tool (Clark Labs, Clark University, Worcester, Massachusetts, USA). Grayscale DNs were initially classified into 13 zones of similarity, and a segmentation analysis was applied. The method computes a standard deviation for each pixel using a  $3 \times 3$  moving window filter. The standard deviation and associated DN for each pixel are then sorted (low to high), and a bin range is assigned. A class width tolerance was set for pixels having similar standard deviations, and all values within a specified range were assigned to the same class. Where pixel values were outside the range, but class boundaries overlapped, a midpoint was determined and a new class was created.

The initial 13 classes were manually reclassified into three general classes (fallowed/cropped, grass, and trees) based on the extents of the dominant land cover types observed in the original and classified images. Characteristic roughness lengths,  $Z_0$ , were then selected for each class based on values reported for similar surface types (Brutsaert, 1982). In this case, a value of 0.05 m was used for the fallowed/cropped class, and 0.10 m was used for the taller- and denser-grass class. Narrow rings of shrubs and trees around wetlands were also dense and much taller than the surrounding cover with heights varying from 3 to 10 m. Brutsaert (1982) reported roughness lengths between 0.2 and 0.4 m for similar type surface elements. The value of 0.40 m was chosen to reflect an expected increase in roughness and turbulent exchange due to a likely reduction in wind speed compared to the surrounding cover types.

### 3.5 Exploratory analysis of surface variables and evaporation estimates

Exploratory analysis of key surface variables and evaporation estimates was conducted using the R software environment (Grunsky, 2002). Data analysis consisted of boxplot summaries giving the 25th and 75th quartiles (i.e. the interquartile range) defined by the box, and an inner solid line indicating the median value was also given. Data points were plotted with jitter to reflect the density of outliers greater than 1.5 times larger or smaller than the interquartile range with the upper and lower limits defined by box whiskers.

## 4 Results and discussion

Calculating detailed daily evaporation estimates and examining spatial scaling issues required the midday inputs and temporal-scaling function to be computed first. Analysis of midday inputs are described in Sect. 4.1–4.4. Section 4.5 and 4.6 discuss the sensitivity of the G–D model to the midday evaporation ratio and the temporal transfer function required for scaling a single measured value of mean daily radiation across a midday image. Section 4.7–4.9 discuss the accuracy of the resulting evaporation estimates, variations in statistical distributions of key driving components, and scaling implications for larger-scale evaporation estimates.

### 4.1 Validation of albedo estimates

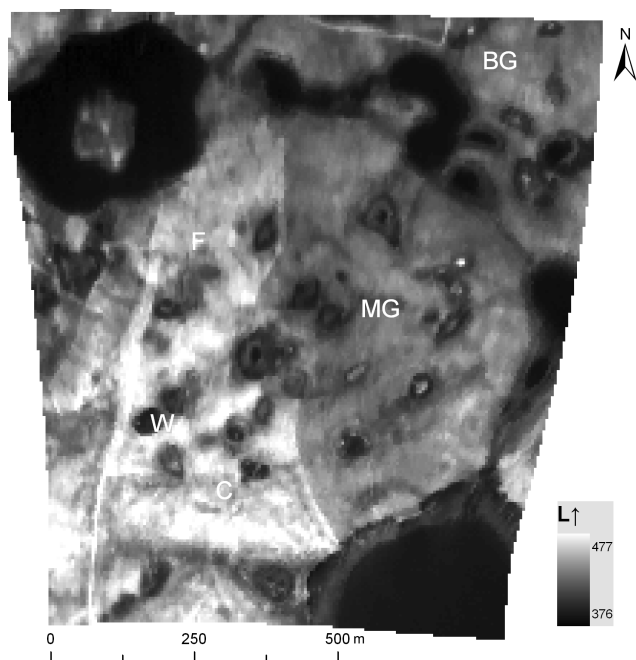
At midday on 5 August 2007 a reference albedo of  $\alpha_{\text{ref}} = 0.153$  was obtained from observed irradiance and the reflectance of shortwave radiation over the mix of green grasses. The albedo map resulting from Eq. (11) and locations of reference and validation points is shown in Fig. 3. Vegetation was similar at both EC station locations, and the scaled albedo estimate (0.164) agreed well with the measured value (0.167) at the validation site.

The validation of the mean and range of albedo estimates obtained for major land covers in Fig. 3 is summarised in Table 1. Estimates of albedo from the image compared well with values expected for grasses, agricultural crops, deciduous trees, and bare soils reported in Brutsaert (1982). The root mean square error (RMSE) of albedo estimates from the pixels and measured albedo values was approximately 3.5 %, which is within an expected error of 2 % to 5 % for research purposes (Liang, 2000).

The 5 m resolution albedo map highlighted surface information within the landscape that would be more generalised using coarser data. For example, the albedo map depicted distinct boundaries separating regions dominated by brome (BG) and mixed grasses (MG), cultivated or crop area (C), sparsely vegetated, fallow area (F), and wetland fringe vegetation (W). Also, wetland extents and fringe vegetation were observable in areas surrounded by other vegetation types (see Fig. 1 for reference). The detailed variations

**Table 1.** Approximate mean values and ranges of albedo for the major land cover types.

Land cover	Mean	Range
Wetland vegetation (W)	0.11	0.05–0.16
Brome grass (BG)	0.15	0.13–0.17
Mixed grass (MG)	0.17	0.15–0.19
Cultivated (C)	0.18	0.17–0.20
Fallow (F)	0.20	0.17–0.23

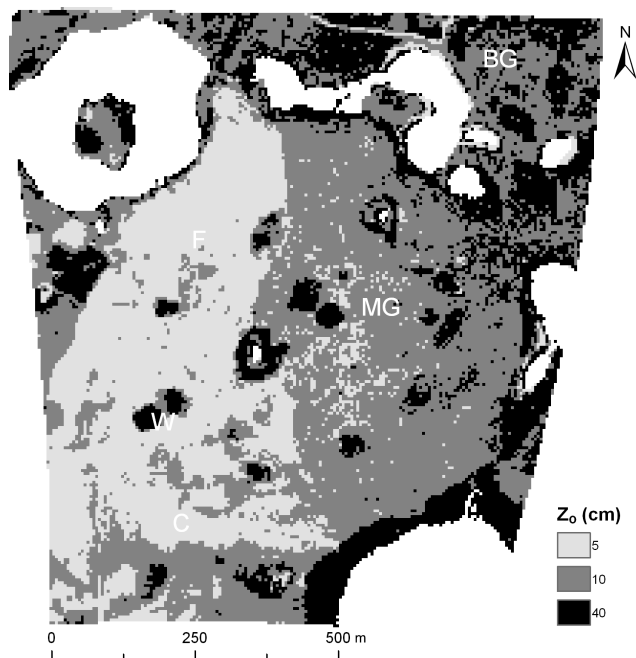
**Figure 4.** Surface-emitted longwave radiation ( $\text{W m}^{-2}$ ) map (5 m resolution) derived from a thermal image taken at midday.

are expected to impact evaporation estimates through relative increases at pixels with relatively lower values of albedo, which results in an increase in the available energy, whereas relatively higher values will reduce the available energy and estimates of evaporation.

#### 4.2 Validation of longwave radiation estimates

Figure 4 shows the resulting map of emitted longwave radiation,  $L_{\uparrow}$ , derived from the image of observed surface temperatures, with estimates ranging between 380 to  $480 \text{ W m}^{-2}$ . At the two EC station locations a comparison was made among the midday surface longwave measurements from the P20 camera, a narrow-beam Exergen infrared thermocouple (IRTC) radiometer, and surface-emitted longwave values obtained from the CNR1.

The P20 measurement compared well with the IRTC values with differences less than  $-12 \text{ W m}^{-2}$ . Compared with the CNR1 values, the differences were slightly larger at

**Figure 5.** Classification map of aerodynamic surface roughness length derived from a visible image taken at midday and typical values found in Brutsaert (1982).

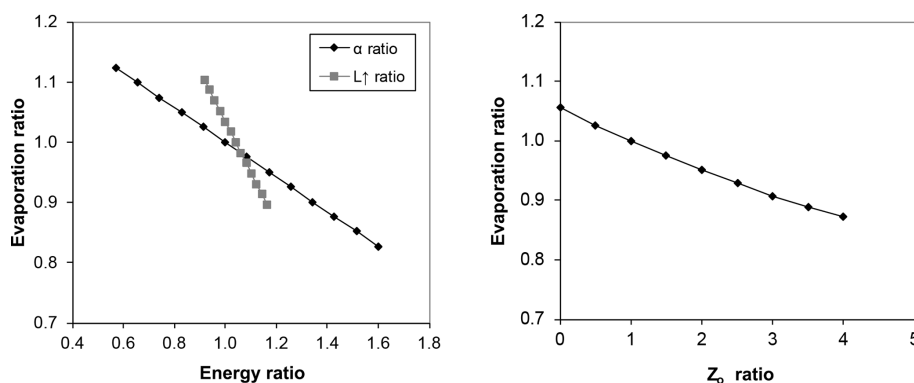
$-30 \text{ W m}^{-2}$  but was still within 8 % error. Generally, the differences were small considering relative changes in midday surface net radiation, and the magnitude of incoming radiation components is considerably larger. The variable footprints of the different measurements and absorption properties of water vapour, which can reduce the signal, are likely sources of error. Also, dust and heating of the CNR1 downward-facing pyrgeometer may introduce another source of error.

For estimating evaporation, the smaller emitted longwave values resulting from lower surface temperatures will increase the available energy relative to larger values which imply reduced water availability and evaporative cooling.

#### 4.3 Surface roughness length map

Figure 5 shows the resulting classified surface roughness length,  $Z_0$ , map. A visual comparison with the study area map (Fig. 1) and albedo map (Fig. 3) suggests that the classification map provides a physically realistic representation of variations in roughness over a large portion of the study area. Notable changes in the reflected surface properties and roughness length classification among the key land cover types can be observed. This is particularly true where distinct boundaries separate the transition between the dominant cover types such as where taller shrubs and trees surround ponds, compared to more broad regions of the fallow, cropped areas and grasses.





**Figure 6.** Sensitivity of the evaporation ratio to key inputs at midday. The measured range of input values is shown to demonstrate potential variation in this case study.

#### 4.4 Sensitivity of the evaporation ratio to key variables at midday

Normalised indexes for albedo, surface temperature, and roughness were considered to examine the relationships of variations in these variables compared to the evaporation ratio. Figure 6 shows the expected physical behaviour of these variables within the G–D model. Only the actual range of values computed for the radiometric index was considered so that the physical variations could be shown more clearly. In this case, the impacts of relative changes in the apparent inverse linear relationships between  $E_R$  and  $\alpha_R$  and  $L\uparrow_R$  and slight non-linear relationship between  $E_R$  and  $Z_{0R}$  on evaporation estimates can be computed. The results can be used to illustrate the impacts of required changes in key driving variables to produce notable changes in the evaporation ratio.

For example, a relative increase in the surface temperature via  $L\uparrow_R$  of 0.18 (or 18 %) was shown to reduce  $E_R$  by 10 %. By comparison, an increase in reflected shortwave radiation via  $\alpha_R$  of 0.30 (or 30 %) reduced  $E_R$  by only 5 %. In the case of surface roughness, an increase of 250 % was needed to reduce  $E_R$  by 10 %. Consequently, a relative reduction in evaporation rates may be expected where albedo, surface temperature, and surface roughness tend to be larger. In the latter case, step changes in surface roughness would increase the relative drying power,  $D$ , but the relative evaporation,  $G$ , results in a relative decrease due to the inverse non-linear relationship. The increased sensitivity of  $E_R$  to  $L\uparrow_R$  also indicates that detailed spatial variations in surface longwave radiation is an important factor for estimating evaporation.

#### 4.5 Temporal transfer function: normalised radiometric radiation index

Net radiation is known to vary dynamically on a sub-daily basis. Equation (10) shows how a radiation ratio,  $Q_R^*$ , can be used as a temporal transfer function to scale estimates of mean daily net radiation over an image. In order to scale the normalised net radiation ratios from a temporal “point” at

midday to a mean daily value, it was necessary to examine whether a stable proportionality existed between measured values at midday and mean daily net radiation. Verification of a proportionality under clear skies would eliminate the need for an empirical scaling function.

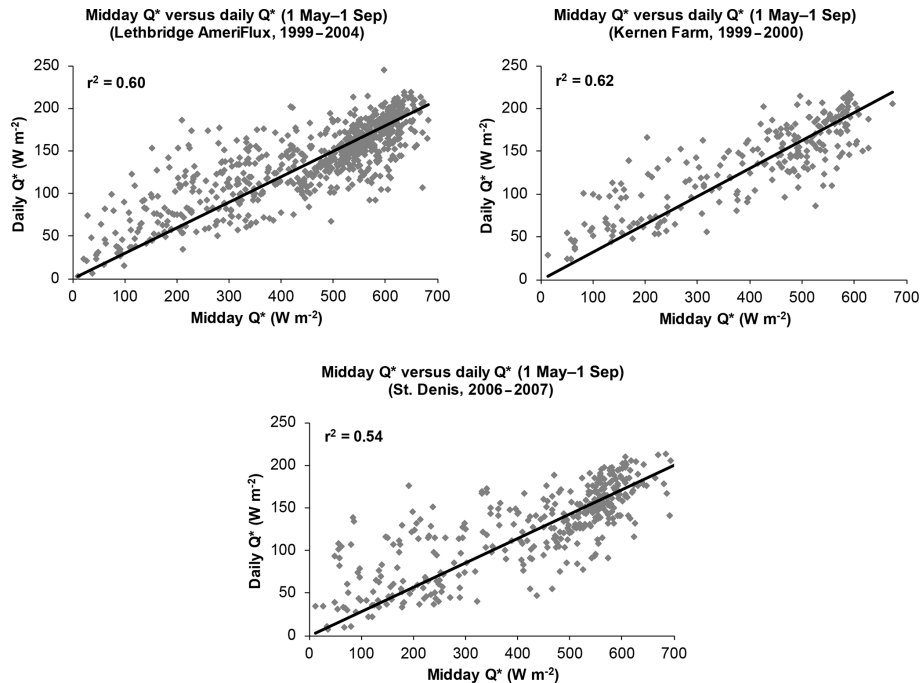
Historical records were examined for a period from 1 May to 1 September at three Canadian Prairie locations at similar latitudes (49–52.2°). The analysis included two field seasons at the SDNWA study site (2006–2007). Archived data were also obtained at two short grass prairie locations, an AmeriFlux network site at Lethbridge, Alberta, Canada (1999–2004), and Kernen Farm located at Saskatoon, Saskatchewan, Canada (1999–2000). Figure 7 shows a moderately strong relationship at each location even with the  $y$  intercept set to 0, and  $r^2$  is equal to 0.54–0.62.

This result confirms that a general proportionality exists and suggests that daily net radiation,  $Q_d^*$ , could be scaled to all pixels across an image from a single measured reference value,  $Q_{dref}^*$ , as a function of the normalised ratio index for  $Q_R^*$  at midday, stated here as

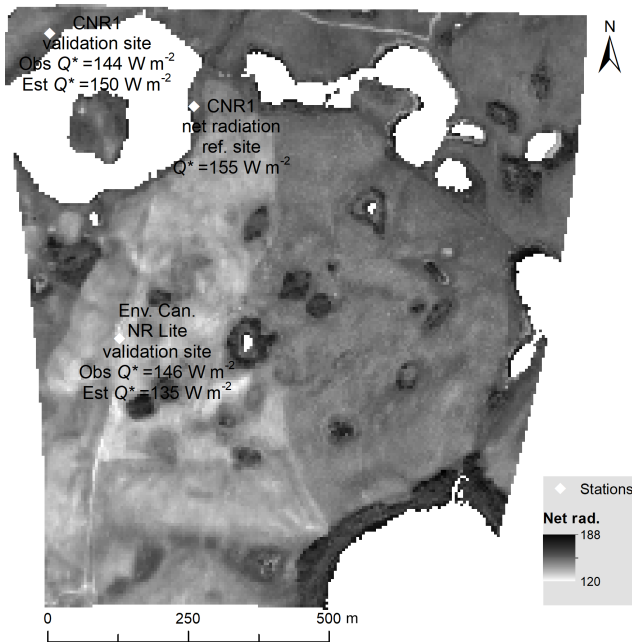
$$Q_d^* = Q_{dref}^* Q_R^* \quad (12)$$

$Q_{dref}^*$  was assigned a daily measured reference value of  $155 \text{ W m}^{-2}$ , which was obtained from the CNR1 at the reference station.  $Q_R^*$  was derived from Eq. (10) using the measured reference values of incoming shortwave and longwave radiation components, and albedo and emitted longwave maps are used as inputs. The resulting mean daily net radiation map and a comparison of estimated and measured  $Q_d^*$  at two validation locations are shown in Fig. 8. The main validation site was equipped with a CNR1 and a second independent site maintained by Environment Canada was equipped with an NR Lite radiometer (Kipp & Zonen, Delft, the Netherlands).

The distributed estimates of daily net radiation ranged from approximately 120 to  $190 \text{ W m}^{-2}$ . The  $Q_d^*$  estimates at the validation sites were  $6 \text{ W m}^{-2}$  higher (4 % error) compared to the CNR1 measurement and  $11 \text{ W m}^{-2}$  lower (8 %



**Figure 7.** Relationship between the midday and mean daily net radiation for a range of years at two Canadian Prairie sites and one Parkland site for the period 1 May through 1 September.  $R^2$  values shown for fitted line with the  $y$  intercept set to 0.



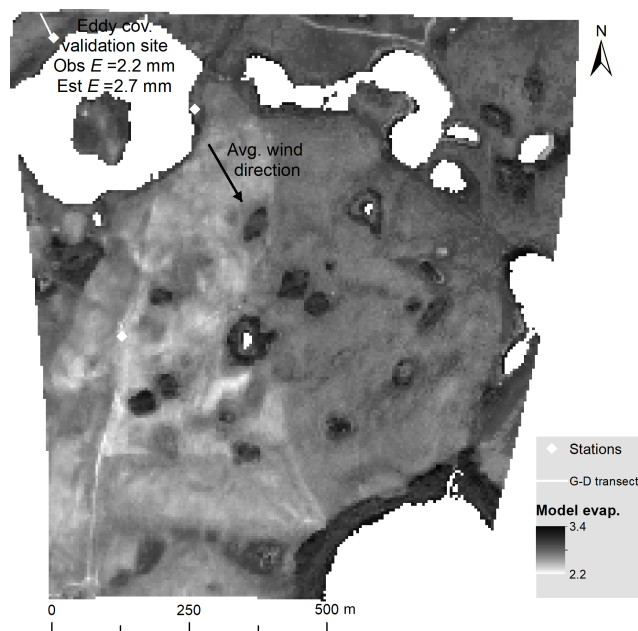
**Figure 8.** Resulting input map of mean daily net radiation derived from the normalised index of midday net radiation and a single reference value of mean daily net radiation ( $155 \text{ W m}^{-2}$ ). Also shown are the location of validation sites for comparing measured and estimated values of mean daily net radiation.

error) compared to the NR Lite observation. These results indicate that accurate estimates of net radiation can be scaled across detailed midday images from a single measured value of mean daily net radiation. More importantly, detailed accurate estimates of net radiation would be valuable for improving point-scale evaporation estimates.

#### 4.6 Calculating direct estimates of actual evaporation with the G–D model

The mean daily net radiation map derived from Eq. (12) was supplied as input to the G–D model to estimate the mean daily actual evaporation at every land surface pixel. The reference humidity and wind speed values (discussed earlier) and the surface roughness length map were used for calculating the aerodynamic terms in Eqs. (2) and (3). An estimate of mean daily evaporation was then calculated at every pixel location based on Eq. (1).

The resulting map of distributed actual evaporation estimates is shown in Fig. 9. Due to the level of detail captured in the net radiation map of Fig. 8, the map shows a physically realistic pattern of evaporation for the range of land cover types. For example, areas where vegetation was less dense (e.g. fallowed/cropped) and soil surface conditions were drier showed lower rates of mean daily evaporation, and higher rates were associated with the more-densely grassed areas. The highest evaporation estimates were obtained where water availability is expected to be higher, e.g. among wetland fringes and depressions where albedo and surface tempera-



**Figure 9.** Map of distributed estimates of mean daily evaporation at a 5 m pixel resolution.

tures were lower, which can be attributed to increased water availability and evaporative cooling.

The prevailing wind direction for the day ( $U_{\text{dir}}$ ) was from a north-northwest direction. A mean evaporation estimate of 2.7 mm was obtained along a linear transect for pixels containing a brome grass surface immediately upwind of the EC station (Fig. 9). The estimate of 2.7 mm was 0.5 mm or 23 % higher than the EC-measured mean evaporative flux of 2.2 mm d<sup>-1</sup>. Based on the cumulative flux model of Schuepp et al. (1990), it is expected that 80 % of the cumulative flux would come from within an upwind distance of 100 m from the EC station along a similar path to the linear transect. The estimate of 2.7 mm d<sup>-1</sup> might be lower if ground heat flux was found to be a factor for reducing the available energy. However this would need to be reliably accounted for at every 5 m pixel.

On the study day the mean daily energy fluxes in W m<sup>-2</sup> (including latent (LE) and sensible heat (HE)), and the ratio of the energy balance closure at the validation site was  $(LE + HE)/(Q^* - Q_g) = (63 + 55)/(144 - 2)$ . This results in an energy balance closure of approximately 83 %. The resulting Bowen ratio of 0.87 was reasonable for the drying conditions and later timing in the growing season for the grasses in this semi-arid region. In this case it is expected there will be uncertainty in both estimated and measured EC fluxes due to modelling and measurement errors and different footprint scales. For instance, it is possible that LE and HE could be under-measured or the ground heat flux could be more variable upwind of the EC station than estimated.

Measured evaporation rates were not available for trees (dominated by aspen) in 2007, but the G–D estimates were compared against archived values from Boreal Ecosystem–Atmosphere Study (BOREAS) data for an old-aspen site from August 1996. The G–D mean daily values in the order of 3 mm were reasonable compared to evaporation from similar trees reported by Hogg et al. (2001).

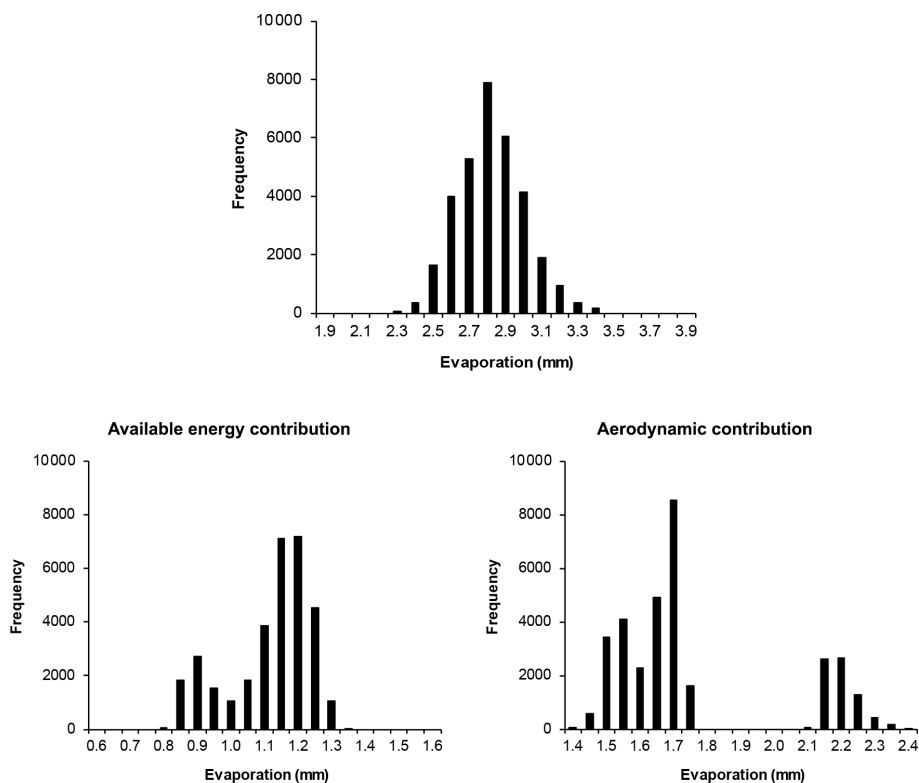
In general, the results are instructive because the G–D method has been demonstrated to provide a reasonable estimate of evaporation from the remote-sensing images taken over a complex landscape. Armstrong et al. (2008) have also shown similar accuracy for daily and multi-day periods from meteorological data alone during the 2006 field season at the same study area. More importantly, the radiometric-index method of scaling may be valid for distributing surface radiation components across remote-sensing imagery obtained from satellites, planes, or near-surface aerial platforms such as UAVs.

#### 4.7 Distributions of evaporation and driving surface variables

The following sections briefly discuss the statistical distributions of the driving variables obtained from the images used for estimating evaporation and their impacts on the resulting evaporation estimates. The benefit here is the statistical distributions of evaporation and key driving factors are considered to be physically meaningful.

Figure 10 shows the frequency distributions of evaporation estimates and relative contributions for the energy balance and aerodynamic components. G–D model evaporation estimates appear normally distributed with a mean of 2.8 mm d<sup>-1</sup> and a relatively low coefficient of variation (cv of 0.07). Distributions for the energy and aerodynamic terms were notably different due to interactions among the driving variables and different roughness classes. For the energy component, the distribution was continuous with a mean of 1.1 mm and a cv of 0.11. The distribution mean for the aerodynamic term was 1.7 mm and was bimodal due to the differences in magnitude of the discrete roughness classes used.

Figure 11 shows boxplot summaries of distributions for albedo ( $\alpha$ ), surface temperature ( $T_s$ ), net radiation ( $Q^*$ ), relative evaporation ( $G$ ), mean daily evaporation ( $E$ ), and  $G$  plotted against net radiation. In the case of  $\alpha$ , values below approximately 0.10 and lower “outliers” can be attributed to uncertainty associated with the wetland vegetation and likely where surface water was not completely masked out near the edges of ponds. In general, the distributions for  $\alpha$  and  $T_s$  which drive the net radiation appear to show more notable variability compared to  $Q^*$  and the resulting estimates of  $E$ . For example, the distributions of  $\alpha$  and  $T_s$  showed opposite skewness,  $-0.83$  and  $0.36$ , respectively. The variability for  $\alpha$  (cv of 0.19) was larger than  $T_s$  (cv of 0.14), which is also much larger than apparent variability of both  $Q^*$  (cv of 0.65) and  $E$  (cv of 0.66). Mean values of the distributions for  $\alpha$ ,



**Figure 10.** Distribution of daily evaporation estimates over the field area and relative contributions of evaporation for the energy and aerodynamic terms.

$T_s$ ,  $Q^*$ , and  $E$  were close to the median values shown within the boxes depicting the interquartile ranges.

The resulting boxplot for  $G$  and the plot of  $G$  against net radiation reflects the interaction across the discrete roughness length classes. The statistical distribution of  $G$  was not continuous due to the larger step change in roughness length from 10 to 40 cm. Plots of  $G$  against net radiation resulted in three distinct linear relationships which can be attributed to using a uniform mean daily wind speed and humidity deficit for calculating the drying power of the air,  $E_A$ . In this case, the potential variability of  $G$  associated with the relative drying power,  $D$ , is limited to variations in roughness length, but this may vary more with changes in wind speed and the humidity deficit.

Generally, despite the larger variability of key factors driving the energy component the complex interactions within the G–D model appear to reduce the overall variability of evaporation estimates.

#### Spatial variations within roughness length classes

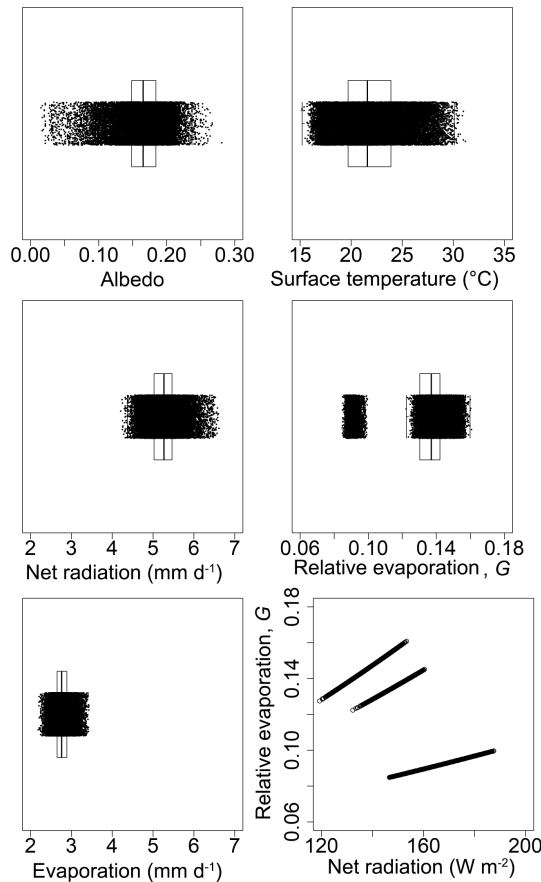
Boxplots shown in Fig. 12 further characterise the spatial variability of  $\alpha$ ,  $T_s$ ,  $Q^*$ ,  $G$ , and  $E$  within the three roughness length classes. In general, the plots depict notable shifts in the interquartile ranges of the distributions across the classes. Results of paired Kolmogorov–Smirnov tests for

each variable showed statistical differences among the distributions for each roughness class were highly significant ( $p$  value < 0.001). General increases in albedo and surface temperature are clearly shown across the 20 to 40 cm and 10 cm roughness length classes.

Consequently, there was a notable reduction in net radiation and similar reduction in evaporation estimates moving from the higher to lower roughness length classes. Figure 12 also clearly shows evidence of a non-linear, inverse relationship between  $G$  and net radiation across the roughness length classes. In this case, the interaction between  $G$  and  $Q^*$  appears to offset the potential increase in mean estimates of  $E$  associated with increases in available energy. As a result, a large reduction in the variability of the evaporation estimates is clearly evident when compared to the same plot for net radiation.

#### 4.8 Scaling implications

There is a potential for areal estimates of evaporation to vary depending on how upscaled estimates are calculated from the underlying driving factors or the smaller point-scale estimates. For example, a mean areal estimate of evaporation calculated from all image pixels was  $2.8 \text{ mm d}^{-1}$ , which accounts for all of the variability available from 5 m pixels. An areal estimate may also be calculated as a weighted mean

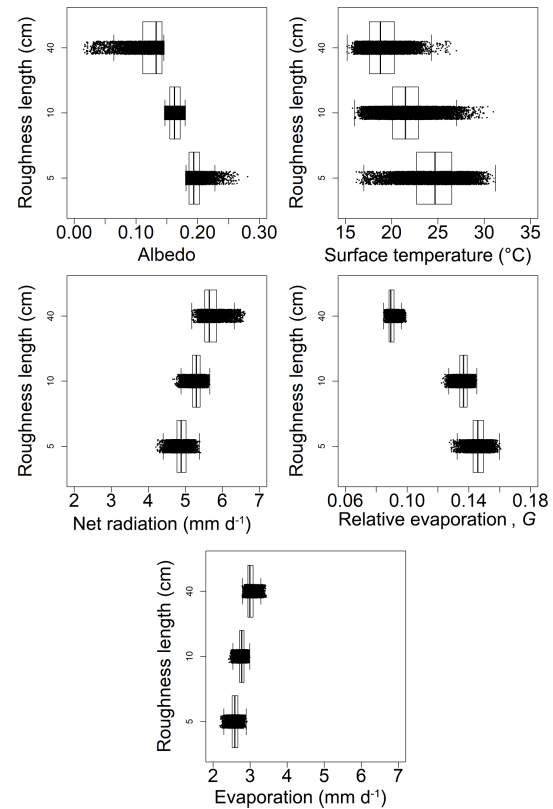


**Figure 11.** Distribution of key surface variables, mean daily evaporation estimates, and relative evaporation over the field area and the relationship between  $G$  and net radiation within the roughness classes.

of evaporation estimates obtained for each roughness length class. This is similar to the mosaic approach used within land surface schemes based on fractional land cover areas. The mean daily evaporation rates for the 5, 10, and 40 cm roughness length classes increased with each step change in roughness class as 2.6, 2.8, and 3.0 mm d<sup>-1</sup>, respectively. The distribution of land area associated with each roughness class was 48 % (10 cm roughness), 30 % (5 cm roughness), and 22 % (40 cm roughness). The weighted areal evaporation ( $E_{\text{areal}}$ ) can be obtained as

$$E_{\text{areal}} = (0.30 \cdot 2.6) + (0.48 \cdot 2.8) + (0.22 \cdot 3.0) = 2.78 \text{ mm d}^{-1}. \quad (13)$$

In this case there was only a small difference in areal estimates obtained based on the distribution mean or a weighted mean based on fractional areas of each roughness class. This may be partly due to the relatively small variation in evaporation rates across the roughness length classes and the level of detailed variability captured by the 5 m pixel resolution.  $E_{\text{areal}}$  was recalculated using Eq. (13) with different combinations of the fractional areas, which only produced a minor difference of  $\pm 0.1$  mm. In other words, in order for there to



**Figure 12.** Distributions of albedo, surface temperature, net radiation, evaporation, and relative evaporation within each roughness class.

be a larger difference between the areal estimates, greater variability may either be required in the evaporation estimates distributed over the field or among the mean rates for each roughness class.

The mean areal estimate,  $E_{\text{areal}}$  of 2.8 mm d<sup>-1</sup> for all pixels, was also 0.3 mm higher than a G–D model estimate of 2.5 mm d<sup>-1</sup> obtained from station meteorological observations of net radiation, air temperature, humidity, and wind speed. Variations among the estimates and measurements vary by approximately 22 % to 27 %, which is not surprising given the differences in calculation techniques and potential mismatches in associated footprint scales.

An upscaled areal mean estimate of evaporation can also be obtained from mean values of the key factors driving the energy and aerodynamic terms. The general form of Eq. (1) can be restated to derive the individual components more directly as

$$E = \frac{\Delta G Q^*}{\Delta G + \gamma} + \frac{\gamma G E_A}{\Delta G + \gamma}. \quad (14)$$

For the entire area and also each roughness length class, mean values of the driving factors were derived and evaporation estimates were recalculated using Eq. (14). The relative evaporative contributions attributed to the energy and

**Table 2.** Areal evaporation estimates within each roughness class from the G–D model and for the entire area based on mean values.  $E_{\text{energy}}$  and  $E_{\text{aero}}$  are the contributions from the energy and aerodynamic components, and  $E_{\text{total}}$  is the combined total. The mean value of the distributed estimates is given in the column “Expected”, and the difference between the total and expected is given in the column “Diff”.

$Z_0$ cm	$\Delta$ kPa	$G$	$Q^*$ mm d <sup>−1</sup>	$\gamma$ kPa	$E_A$ mm d <sup>−1</sup>	$D$	$E_{\text{energy}}$ mm d <sup>−1</sup>	$E_{\text{aero}}$ mm d <sup>−1</sup>	$E_{\text{total}}$ mm d <sup>−1</sup>	Expected mm d <sup>−1</sup>	Diff mm
5	0.134	0.132	4.88	0.063	12.99	0.73	1.07	1.34	2.40	2.59	−0.18
10	0.134	0.124	5.27	0.063	15.13	0.74	1.10	1.48	2.58	2.77	−0.19
40	0.134	0.085	5.69	0.063	27.97	0.83	0.87	2.01	2.88	3.02	−0.14
$E_{\text{areal}}$	0.134	0.113	5.28	0.063	18.70	0.77	1.03	1.71	2.73	2.77	−0.03

aerodynamic terms are provided in Table 2. For the different roughness length classes, the range of evaporation estimates attributed to  $E_{\text{energy}}$  was only 0.2 mm d<sup>−1</sup> and nearly 0.7 mm d<sup>−1</sup> for  $E_{\text{aero}}$ , and the difference in total evaporation,  $E_{\text{total}}$  was 0.5 mm d<sup>−1</sup>. A bias toward larger evaporation estimates might be expected given the increase in energy availability and enhanced turbulence with an increase in roughness. However, the potential bias was offset by the interaction of  $G$  and  $Q^*$  and also  $G$  and  $E_A$ .

Table 2 also compares evaporation estimates calculated from only mean values of  $G$  and  $Q^*$ , and  $E_A$  to the “expected” rates for each roughness length class. Expected rates were calculated from the mean values for all pixels assigned within each roughness length class. Evaporation rates derived from the mean input values alone were only between 0.14 and 0.2 mm less than the expected mean rates for each roughness length class. Upscaling the driving factors to the entire area also had no impact on the resulting estimate as the difference was just 0.1 mm.

#### 4.9 Examining spatial covariance among key variables

Whether evaporation estimates might be influenced by a spatial covariance between driving factors was also examined. The Pearson correlation coefficient,  $r$ , was used to evaluate correlations among the driving factors distributed over the field area. By definition, Pearson’s correlation is the ratio of the covariance (the numerator) between two variables normalised by the product of their standard deviations as follows:

$$r = \frac{\sum \frac{(X_i - \bar{X})(Y_i - \bar{Y})}{n}}{\sqrt{\sum \frac{(X_i - \bar{X})^2}{n}} \sqrt{\sum \frac{(Y_i - \bar{Y})^2}{n}}}, \quad (15)$$

where  $X_i$  and  $Y_i$  are the respective values of the variables, the overbar denotes the mean value, and  $n$  is the number of pairs. A strong correlation between two variables might suggest the existence of covariance that could influence upscaled estimates of evaporation. Given that the roughness classes used represent discrete data and there is a lack of more detailed meteorological data to parameterise the aerodynamic term, further evaluation related to climate factors would not

be meaningful. Therefore only an examination of the factors driving the energy term are considered here.

In this case, a potential covariance between  $G$  (dimensionless) and  $Q^*$  (expressed in mm d<sup>−1</sup>) can be considered directly. By rearranging Eq. (15) the covariance can be obtained by multiplying the correlation coefficient and the product of the standard deviations of  $Q^*$  (0.34 mm d<sup>−1</sup>) and  $G$  (0.021 mm d<sup>−1</sup>). The correlation between  $Q^*$  and  $G$  over the field area produced a coefficient,  $r = -0.67$ .

When multiplied in series ( $r = -0.67$ ) · 0.34 · 0.02 this results in a covariance of approximately −0.0049 mm d<sup>−1</sup>. This suggests interactions between  $Q^*$  and  $G$  for the methods applied here would have no further statistical influence on upscaled evaporation estimates. Unfortunately, no comment can be made regarding covariance between  $G$  and the turbulent flux component in the G–D model. Such analysis would require more detailed observations of air temperature, humidity, and wind speed and possibly a more sensitive combination model. Nevertheless, the impact of combined interactions within the G–D model effectively reduced the overall variability of point-scale evaporation estimates and also upscaled estimates derived from different computation methods for parameterising the model.

#### 4.10 General uncertainty of the methods applied

Implications of general modelling assumptions and the uncertainty of the methods applied are briefly discussed here. The daily ground heat flux was considered to be negligible for the study day as the mean daily flux was relatively small at the two stations where there was good canopy coverage. Where local cover properties are similar (e.g. brome grass and mixed-grass areas) the ground heat flux may be of a similar magnitude, but it would be greater where surface cover is less dense or where water availability is limited, due to differences in the surface properties.

Further, the relative evaporation,  $G$ , which is based on the relative drying power,  $D$ , integrates available energy which in this case directly includes the spatial variability of surface temperature. As such, evaporation might be overestimated in areas with more ground exposure and higher surface temperatures, where ground heat flux may be appreciably larger (e.g. fallowed/crop area). This interaction could result in a



further reduction in the energy available for the evaporation estimate.

C<sub>3</sub>-type vegetation was at the study area, but the model behaviour may differ for C<sub>4</sub> plants and may require new vapour transfer equations for surface types and plants other than which the G–D model was developed on. In the current study representative roughness lengths were selected based on reported values for surfaces of a similar type and height. A larger uncertainty in evaporation estimates may be expected for the roughness length class associated with the shrub/tree areas which could result in variable changes in wind speed and enhanced turbulence associated with larger roughness lengths.

## 5 Summary and conclusions

This study examined spatial associations and physical interactions amongst key surface variables driving actual evaporation estimates and impacts of their variations on various methods of upscaling estimates to a larger area. The methods applied demonstrate how measured reference values of albedo and mean daily net radiation can be scaled accurately across a large field area for the purpose of deriving point-scale estimates of evaporation at each pixel. This was achieved by computing a normalised radiometric index of surface radiation from highly detailed midday visible and thermal images. At two validation sites estimates of daily net radiation showed good agreement with measured values to within 4 % and 8 % error.

Estimates of mean daily actual evaporation were calculated at 5 m resolution with the G–D model. The daily evaporation rate estimated for a transect upwind of the EC station was 2.7 mm for 5 August 2007 which was 23 % larger than the EC measured flux of 2.2 mm. Offsetting interactions between the relative evaporation term and key surface variables effectively reduce the spatial variability of evaporation estimates. As a result, differences amongst computed areal evaporation estimates were relatively small regardless of the different methods used to derive representative average values of driving factors to parameterise the model or the average evaporation rate derived from detailed estimates across the field. There was no evidence of a spatial covariance between the spatial distributions of net radiation and *G*, so no correction factor was identified for improving upscaled evaporation estimates.

The scaling methods applied to the energy terms using radiometric indexes derived from detailed images could generate useful diagnostic information at other study locations and potentially over much larger areas. The methods applied here may also be instructive toward improving techniques for upscaling evaporation estimates to larger areas via traditional remote sensing or climate modelling or using a different combination model. It is expected that the methods can be applied to visible and thermal images taken from cameras

and sensors on a variety of sensing platforms (e.g. satellites, planes, and UAVs).

*Data availability.* Data used for this study can be accessed at <https://doi.org/10.20383/101.0192> (Armstrong et al., 2019).

*Author contributions.* RA conducted the field investigation and modelling under the co-supervision of JP and LM. RA prepared the paper with contributions from all co-authors.

*Competing interests.* The authors declare that they have no conflict of interest.

*Special issue statement.* This article is part of the special issue “Understanding and predicting Earth system and hydrological change in cold regions”. It is not associated with a conference.

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