



How good are hydrological models for gap-filling streamflow data?

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Abstract. Gap-filling streamflow data is a critical step for most hydrological studies, such as streamflow trend, flood, and drought analysis and hydrological response variable estimates and predictions. However, there is a lack of quantitative evaluation of the gap-filled data accuracy in most hydrological studies. Here we show that when the missing data rate is less than 10 %, the gap-filled streamflow data obtained using calibrated hydrological models perform almost the same as the benchmark data (less than 1 % missing) when estimating annual trends for 217 unregulated catchments widely spread across Australia. Furthermore, the relative streamflow trend bias caused by the gap filling is not very large in very dry catchments where the hydrological model calibration is normally poor. Our results clearly demonstrate that the gap filling using hydrological modelling has little impact on the estimation of annual streamflow and its trends.

1 Introduction

Streamflow is channel runoff, i.e. the flow of water in streams and rivers and water accumulated from surface runoff from the land surface and groundwater recharge. It is one of the major water balance components in a catchment, where precipitation is partially stored in surface water, soil, and groundwater stores, and the rest is partitioned into two fluxes: evapotranspiration and streamflow. It is almost impossible to measure evapotranspiration dynamics at a catchment scale. In contrast, streamflow time series can be easily measured at a catchment outlet. Therefore, streamflow data become a fundamental dataset underpinning hydrological studies. Without such a dataset, it is hard to understand catchment hydrological processes under climate change and non-stationarity (Dai et al., 2009; Gedney et al., 2006a; Ukkola et al., 2015; Zhang et al., 2016b).

Unfortunately, streamflow data are not always continuously available and most gauges suffer from missing streamflow data issues (Dai et al., 2009). Often, the missing data rate is important when selecting streamflow gauges, especially when the data are used for annual trend analysis. To choose qualified catchments, researchers often set up a threshold for the missing data ratio, for instance 1 % (Petrone et al., 2010), 5 % (Ukkola et al., 2015), 10 % (Déry et al., 2009), 15 % (Liu and Zhang, 2017), and 20 % (Lopes et al., 2016). Only those gauges with a missing data rate less than a particular threshold are selected, and the rest are excluded for further analysis because of high missing data rates.

There are many methods used for gap-filling the missing data, including interpolation from nearby gauges (Hannaford and Buy, 2012; Lavers et al., 2010; Lopes et al., 2016), statistical methods (Gedney et al., 2006b), hydrological modelling (Dai et al., 2009; Sanderson et al., 2012), and multiple infilling methods (Harvey et al., 2012). Among them, the hydrological modelling method is widely used since it fully considers the spatial heterogeneity and temporal variability of climate forcing data, and can achieve sufficient simulations when it is calibrated against a small number of observations (Peña-Arancibia et al., 2015; Rojas-Serna et al., 2016; Seibert and Beven, 2009; Liu and Zhang, 2017). This is particularly important in Australia, where hydrological modelling is a major tool for simulating continuous streamflow at a catchment scale. More recently, the Australian Bureau of Meteorology used a hydrological model – GR4J – to infill missing daily streamflow data for 222 Hydrologic Reference Stations (<http://www.bom.gov.au/water/hrs/about.shtml>, last access on 8 August 2018). The gap-filled streamflow data are then used for trend analysis, which provides hydrological information to all users.

One major concern for the hydrology community is to understand how reliable the gap-filled data are. Unfortunately

there are no studies in the literature to comprehensively evaluate the reliability and accuracy of the gap-filled data that are influenced by different thresholds and by patterns of missing data. Our study aims to provide a framework to evaluate the annual trends and annual variables obtained from gap-filled streamflow data using two hydrological models (GR4J and SIMHYD), together with a large streamflow dataset available across the Australian continent (Zhang et al., 2013). This can guide researchers to more sensibly define a threshold for catchment selection and hydrological analysis.

2 Data and methods

2.1 Data

We obtained a daily streamflow dataset from 780 unregulated catchments widely spread across Australia (Zhang et al., 2013). The dataset has undergone strict quality assurance and quality control, including quality code check and spike (i.e. outlier points) control, and covered the period from 1975 to 2012. This dataset has been used by modellers for various hydrological modelling and studies of extreme events (Li and Zhang, 2017; Liu and Zhang, 2017; Ukkola et al., 2016; Yang et al., 2017). The missing data rates for the pre-1980 and post-2010 periods were high. To meet our study requirements, we selected 217 catchments with a missing data rate of less than 1 % for the period 1981–2010, and the streamflow data for the 217 catchments are regarded as benchmark data (Fig. 1). Out of the 780 catchments there are 146, 91, and 61 with a missing data rate of 1 %–5 %, 5 %–10 %, and 10 %–20 % during 1981–2010, respectively (Fig. 1), and these catchments account for 38 % of total available catchments. Table 1 summarises major catchment attributes for the 217 selected catchments. The data gaps for Australian streamflow gauges mainly include the following issues: (i) non-sensible records; (ii) broken sensors; (iii) no recorded data (instrumentation removed); (iv) no existing data, and (v) no records or records lost.

Out of the 217 catchments, about half of the catchments showed a significant decreasing trend, 37 % showed a non-significant decreasing trend, and 13 % showed a non-significant increasing trend (Fig. 2), detected using Mann–Kendall trend analysis (see Sect. 2.3). This is because Australia experienced the millennium drought over the period 2001–2009, which caused a dramatic streamflow reduction in this period (van Dijk et al., 2013). Trend analysis for the 217 catchments is explained in Sect. 2.3 and trend results are summarised in Sect. 3.

Out of the 217 catchments, about 46 % of catchments have no missing data in 1981–2010, 12 % with a missing data rate of < 0.1 %, 22 % with a missing data rate of 0.1 %–0.5 %, and 20 % with a missing data rate of 0.5 %–1 % (Fig. 2).

To drive the two hydrological models, we obtained daily meteorological time series (including minimum tempera-

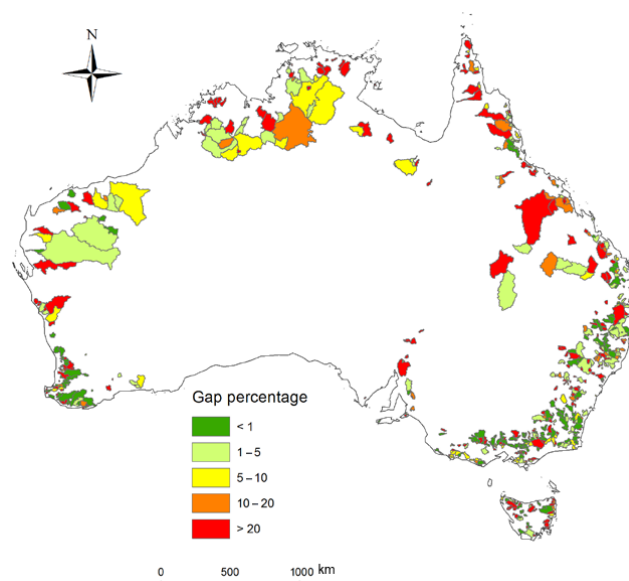


Figure 1. The 780 unregulated catchments grouped by different streamflow data gaps for the period of 1981–2010.

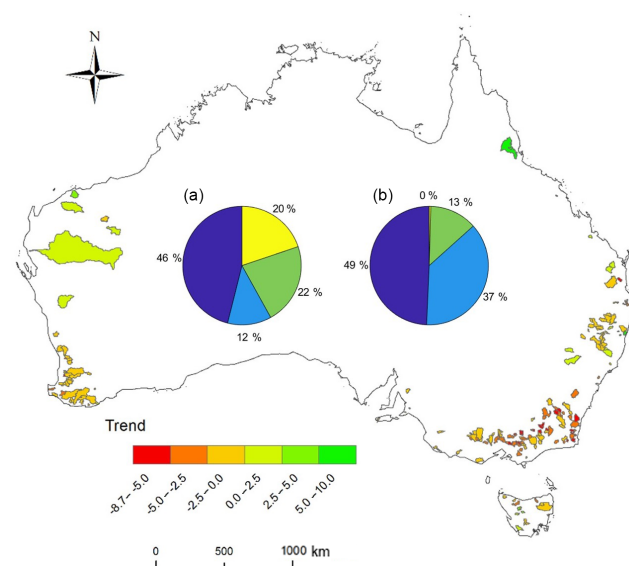
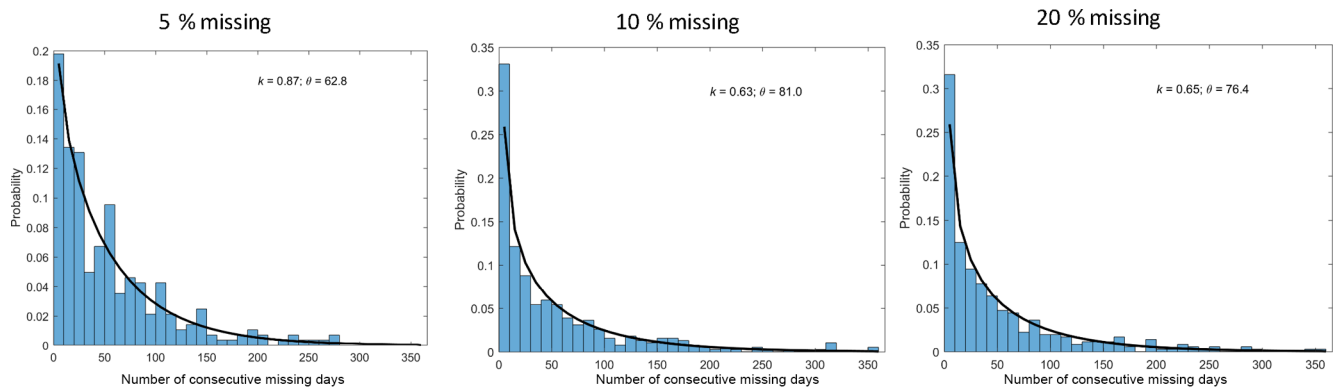


Figure 2. Trends and streamflow data summary for the 217 catchments used in this study. The trend in annual streamflow is shown in units of $\text{mm year}^{-1} \text{ year}^{-1}$. The chart in (a) indicates the catchment percentage with different missing data rates (dark blue with a missing data rate of 0 %, navy blue with a missing data rate of 0 %–0.1 %, green with a missing data rate of 0.1 %–0.5 %, and yellow with a missing data rate of 0.5 %–1.0 %). The chart in (b) indicates the catchment percentage with different trends (dark blue with a significant ($p \leq 0.05$) decreasing trend, navy blue with a non-significant ($p > 0.05$) decreasing trend, green with a non-significant ($p > 0.05$) increasing trend, and yellow with a significant ($p \leq 0.05$) increasing trend).

Table 1. Major catchment attributes for the 217 catchments.

Attribute	Definition	Unit	Min	2.5th	25th	Median	75th	97.5th	Max
Area	Catchment area	km ²	53	70	180	392	844	4562	72 902
Elevation	Catchment average elevation above sea level	m	46	100	278	449	753	1194	1351
Slope	Catchment mean slope	°	0.3	0.6	2.0	3.9	7.7	12.0	13.6
P	Mean annual precipitation	mm year ⁻¹	256	371	703	853	1107	1966	2473
ET _p	Mean annual potential evapotranspiration	mm year ⁻¹	906	968	1149	1235	1408	1791	1892
AI	Aridity index	–	0.38	0.55	1.11	1.44	1.89	4.75	6.47
Forest ratio	Ratio of forest to all land cover types	–	0.02	0.06	0.39	0.55	0.67	0.83	0.90

**Figure 3.** Missing data patterns for three groups of catchments with missing data rates of 4 %–6 %, 8 %–12 %, and 18 %–22 %, which are represented by 5 %, 10 %, and 20 % missing data rates, respectively.

ture, maximum temperature, incoming solar radiation, actual vapour pressure, and precipitation) from 1975 to 2012 at 0.05° (~ 5 km) grid resolution from the SILO Data Drill of the Queensland Department of Natural Resources and Water (<https://silo.longpaddock.qld.gov.au/>, last access on 8 August 2018). The data quality is reasonably good, indicated by the mean absolute error for maximum daily air temperature, minimum daily air temperature, vapour pressure, and precipitation at 1.0 °C, 1.4 °C, 0.15 kPa, and 0.40 mm day⁻¹ (Jeffrey et al., 2001).

2.2 Gap-filling experiments

For thoroughly investigating the potential impacts of infilled streamflow data on annual trend accuracy, we conducted three groups of experiments to test how the missing data rates at 5 %, 10 %, and 20 % impact streamflow trends. We followed three steps for each missing data rate of the experiments.

1. *Missing data patterns were obtained using actual streamflow data.*

We selected patterns of consecutive missing days from actual data from the 780 catchments. For the 5 % group of missing data rate experiments, we selected 44 catchments with missing rates of 4 %–6 %; for the 10 % group of missing data rate experiments, we selected 39 catchments with missing

data rates of 8 %–12 %; and for the 20 % group of missing data rate experiments, we selected 22 catchments with missing data rates of 18 %–22 %. Figure 3 shows the probability distribution of consecutive missing days from each group of catchments, which is skewed toward the low end. We therefore used the two-parameter Gamma distribution to simulate probability distribution of consecutive missing days (Fig. 3). The Γ distribution is expressed as

$$X \sim \Gamma(k, \theta) = \Gamma(k, \theta), \quad (1)$$

where X is the number of consecutive missing days, k is the shape parameter, and θ is the scale parameter. The corresponding probability density function in the shape-scale parameterisation is

$$f(x; k, \theta) = \frac{1}{\Gamma(k)\theta^k} x^{k-1} e^{-\frac{x}{\theta}}, \quad (2)$$

where $\Gamma(k)$ is the gamma function.

As seen from Fig. 3, the two parameters are stable under the three groups of catchments. The k parameter varies from 0.63 to 0.87 and the θ parameter changes from 62 to 81. It is noted that we removed all times when the number of consecutive missing days was > 365. We did that for a number of reasons. Firstly, gap-filling an entire year of missing data would likely impact annual trends. Secondly, the focus of this paper is on gap-filling short periods of missing data to be able

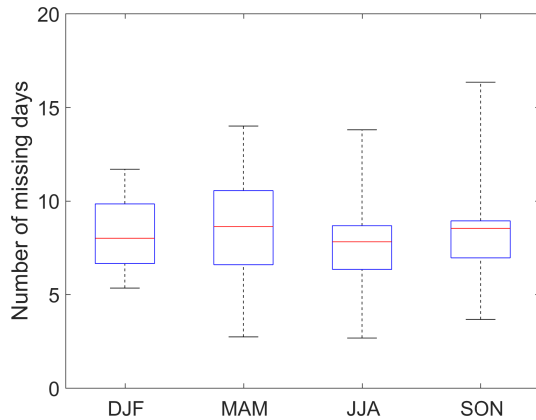


Figure 4. Distribution of number of missing days across different seasons, summarised from 39 catchments with a missing data rate ranging from 8 % to 12 % (i.e. 10 % missing data group).

to include more catchments in streamflow analyses. Thirdly, removing all periods of greater than 365 days allowed us to better fit a gamma distribution to the number of missing days.

We also checked the seasonality of missing data to see if one season were more likely to have missing data than another. As seen from Fig. 4, the missing data are more or less evenly distributed through different seasons across all the 39 catchments (with a missing data rate of 8 % to 12 %) within the 10 % missing data group. This indicates that the data gaps were not skewed toward a particular season and they occurred randomly through the year.

2. *Numbers of random consecutive missing days were generated using a random number generator (sampling without replacement) based on the gamma distribution.*

The random number generation was repeated 100 times to ensure the selected samples covered a wide range of streamflow time series.

3. *Streamflow data were gap-filled.*

The selected days were treated as missing data and the unselected data were used for hydrological model calibration. The missing data were then gap-filled using the simulated streamflow from the calibrated GR4J and SIMHYD models.

For consistent interpretation hereafter, the benchmark streamflow data are regarded as “observed” and the experiment data as “filled”. For each of the three experiments, there are 100×217 (21 700) missing data time series, with 100 representing sample times using the random number generator and 217 representing the number of catchments.

2.3 Trend analysis

We used the Mann–Kendall Tau-b non-parametric test including Sen’s slope method (Burn and Elnur, 2002) for annual streamflow trend analysis and significance testing for all three groups of experiments and benchmark data.

We used the following equation to quantify the trend bias:

$$B_t = T_{\text{filled}} - T_{\text{obs}}, \quad (3)$$

where B_t is the bias in the annual streamflow trend ($\text{mm year}^{-1} \text{ year}^{-1}$), T_{filled} is the annual trend for gap-filled streamflow ($\text{mm year}^{-1} \text{ year}^{-1}$), and T_{obs} is the annual trend in observed streamflow ($\text{mm year}^{-1} \text{ year}^{-1}$). It measures the trend error between the infilled and observed runoff trends with $B_t \approx 0$, which indicates that the trend in observed annual runoff is almost the same as that in the infilled annual runoff.

We also defined relative trend bias (P_{B_t}) as

$$P_{B_t} = \frac{T_{\text{filled}} - T_{\text{obs}}}{T_{\text{obs}}} \times 100. \quad (4)$$

2.4 Hydrological models

Two widely used hydrological models, SIMHYD and GR4J (Chiew et al., 2002, 2010; Li et al., 2014; Oudin et al., 2008; Perrin et al., 2003; Zhang and Chiew, 2009; Zhang et al., 2016a), were used to infill daily missing streamflow data. Both models require daily precipitation and daily potential evaporation (Priestley and Taylor, 1972) as model inputs, and model outputs are daily streamflow at each gauge. The daily inputs of the maximum and minimum temperatures, incoming solar radiation, and vapour pressure data were used to calculate the Priestley–Taylor daily potential evaporation.

The two models were calibrated using a global optimiser, consisting of a genetic algorithm (The MathWorks, 2006), at each catchment, with the first 6 years (i.e. 1975–1980) for spin-up and the remainder (1981–2010) for modelling experiments. Since this study mainly evaluates the trends obtained using the gap-filled streamflow from hydrological modelling, it is crucial to predict high flow and mean flow as accurately as possible. To this end, the model calibration was to minimise the following objective function (F) (Viney et al., 2009; Zhang et al., 2016b):

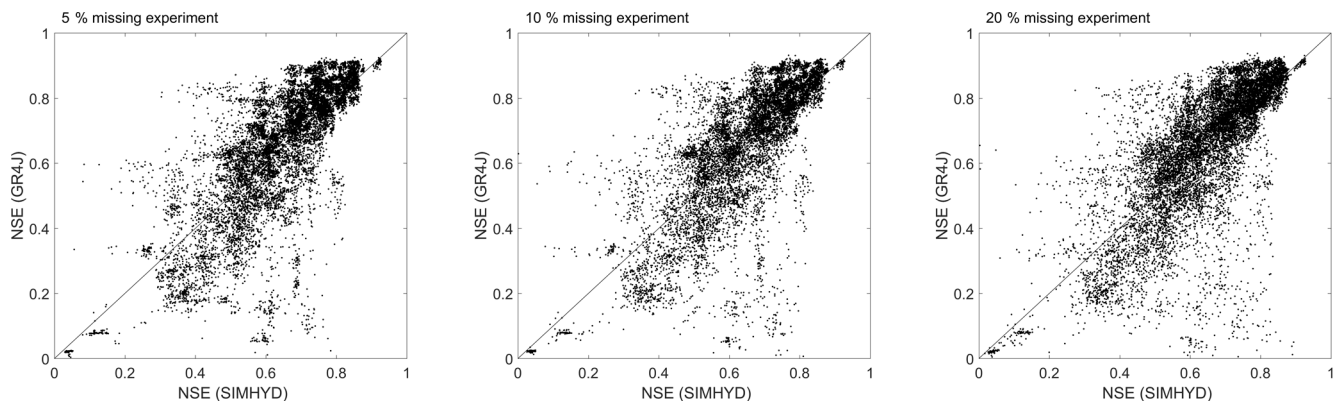
$$F = (1 - \text{NSE}) + 5|\ln(1 + B)|^{2.5}, \quad (5)$$

$$B = \frac{\sum_{i=1}^N Q_{\text{sim},i} - \sum_{i=1}^N Q_{\text{obs},i}}{\sum_{i=1}^N Q_{\text{obs},i}}, \quad (6)$$

where NSE is the Nash–Sutcliffe efficiency of daily streamflow, B is the model bias, Q_{sim} and Q_{obs} are the simulated and observed daily runoff, i is the i th day, and N is the total number of days sampled. The NSE gives higher streamflow more weight, and varies between $-\infty$ and 1, with $\text{NSE} > 0.6$ indicating a good agreement (Zhang and Chiew, 2009). The B measures water balance error between the observed and

Table 2. Summary of model calibration number carried out for benchmark data and missing data experiments.

Model	Benchmark	5 % missing	10 % missing	20 % missing	Sum
GR4J	217	21 700	21 700	21 700	65 317
SIMHYD	217	21 700	21 700	21 700	65 317
Sum	434	43 400	43 400	43 400	130 634

**Figure 5.** Comparisons between calibrated GR4J and calibrated SIMHYD for 44 catchments of the 5 % missing data experiment, 39 catchments of the 10 % missing data experiment, and 22 catchments of the 20 % missing data experiment. In each catchment, there were 100 replicates carried out.

modelled daily streamflow, with $B = 0$ indicating that the average of modelled daily streamflow is the same as the average of observed daily streamflow.

For each catchment, GR4J and SIMHYD were calibrated using benchmark data and 100 time series of streamflow data with missing data (see Sect. 2.2), respectively. For benchmark data without any missing data (46 % catchments), no gap filling is required; for the benchmark data with missing data rates less than 1 %, the calibrated continuous streamflow data were used to fill the gaps. For the missing data experiments, the calibrated continuous streamflow data for each missing replicate were used to infill the artificially made missing data. Table 2 summarises the model calibrations carried out for the benchmark and for each experiment. Finally, 130 634 model calibrations and 130 200 times of gap filling were carried out. Finally, the trends estimated from the benchmark were used to evaluate those obtained from the missing data experiments.

3 Results

The gap-filled data from the two hydrological models were evaluated against the benchmark data. Overall, the two models perform well and neither significantly outperforms the other (Fig. 5). For the three groups of gap-filling experiments, these two models perform similarly (i.e. the difference of NSE of daily runoff between the two is less than 0.02) in 18 %–19 % catchments; the SIMHYD model outperforms

the GR4J model (NSE difference between the two is larger than 0.02) in 30 %–31 % catchments; and the GR4J model outperforms the SIMHYD model in 50 %–51 % catchments.

Figures 6 and 7 summarise the performance of the gap-filled data for estimating annual trends, annual streamflow, monthly streamflow, and daily streamflow, respectively. The three missing data rate experiments (5 %, 10 %, and 20 %) perform almost the same as the benchmark (Figs. 6 and 7). The coefficient of determination (r^2) between the gap-filled trends and observed trends is more than 0.98 for the three experiments and two hydrological models.

Since errors in gap-filled trends are likely to be different and time steps are different when daily infilled streamflow data are used, we further investigate how gap-filled errors are propagated from daily to monthly and to annual scales in the three gap-filling cases (5 %, 10 %, and 20 %) (Figs. 6 and 7). It is expected that daily gap-filled streamflow has a larger standard deviation from the benchmark than monthly and annual streamflow since the streamflow was gap-filled at a daily scale. This indicates that the temporal aggregation smooths the gap-filled error strongly, and it generates very reasonable monthly and annual streamflow estimates with less standard deviation. It is interesting to note that both models tend to underestimate very high flows, though they are calibrated against the NSE of daily streamflow, which gives larger weight to the correct representation of higher flows.

Figure 8 further summarises the catchments with trend direction mismatch between the benchmark and gap-filled data (i.e. change from negative to positive or change from pos-

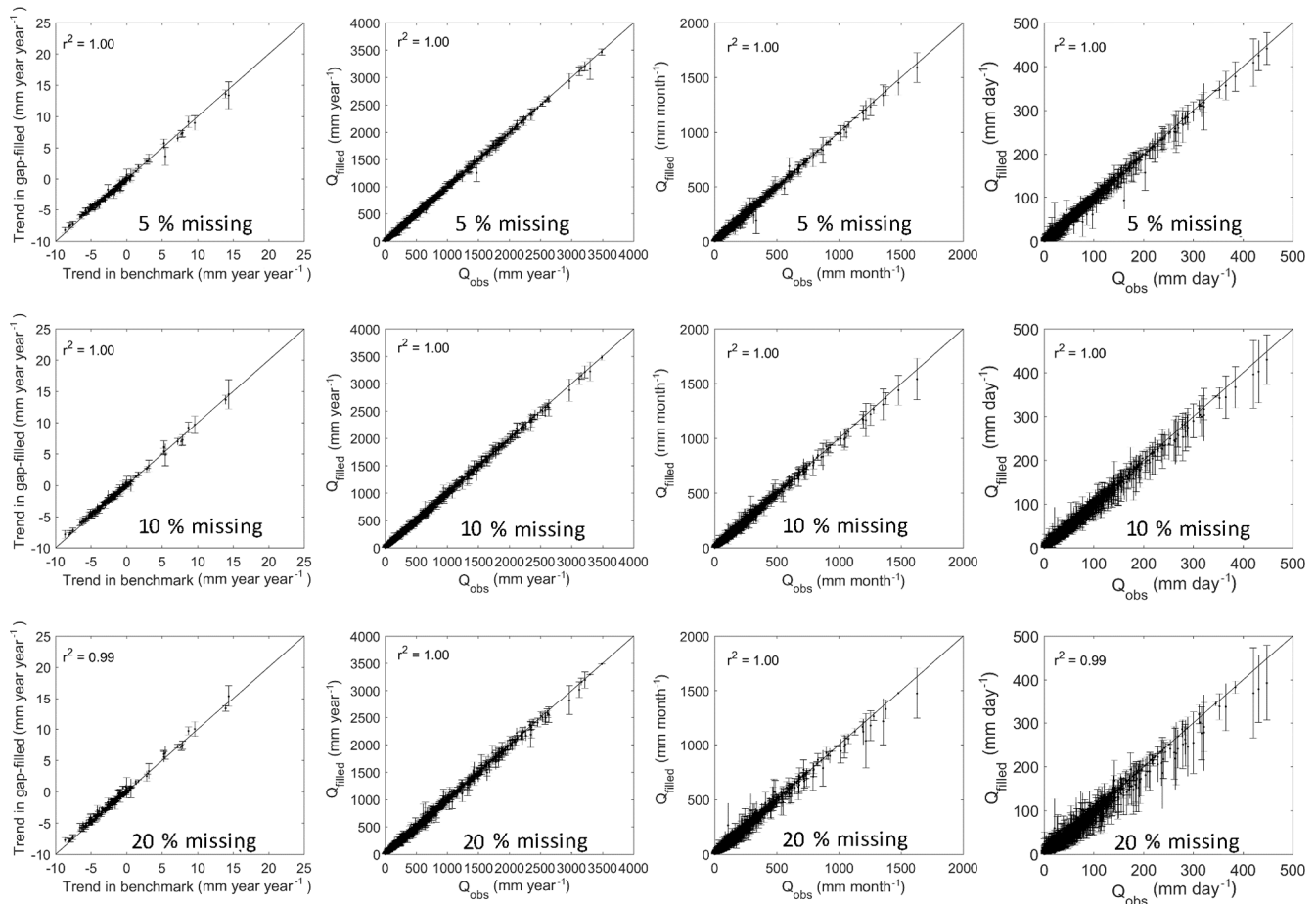


Figure 6. Comparisons between the observed streamflow (x axis) and gap-filled ones (y axis) for streamflow trend (mm year⁻¹ year⁻¹, left panels), annual streamflow (mm year⁻¹, second left panels), monthly streamflow (mm month⁻¹, second right panels), and daily streamflow (mm day⁻¹, right panels). The gaps were filled using GR4J. The error bar represents standard deviation of the 100 replicates for each group of missing data experiments.

itive to negative). For the experiments with 5 % and 10 % missing data rates and for GR4J, fewer than 8 out of the 217 catchments show a trend mismatch, and almost all of them show non-significant trends ($p > 0.05$). For the experiments with a 20 % missing data rate for GR4J, fewer than 10 out of the 217 catchments show a trend mismatch, and all of them show non-significant trends. SIMHYD results are almost the same as GR4J results. All these indicate that there is very marginal influence on annual streamflow trend directions when the missing data rate is less than 20 %.

Though the three groups of experiments show small trend direction changes (Fig. 8), it is not clear how the trend bias (Eq. 3) looks. To this end, Fig. 9 further compares the trend bias between the experiments. It is clear that the trend biases between 5 % and 10 % missing data experiments are similar. For GR4J, both have a trend bias varying from -1 to 1 mm year⁻¹ year⁻¹. For SIMHYD, the trend bias between the two is similar when it varies from -0.5 to 1 mm year⁻¹ year⁻¹, and the trend bias of the 5 % missing

data experiment is even larger than that of the 10 % missing data experiment. The trend bias of the 20 % missing data experiment is noticeably larger than that of the 10 % and 5 % missing data experiments for both models, and the underperformance is more noticeable in the SIMHYD gap-filled data than in the GR4J gap-filled data. This result suggests that the trend bias is reasonable when the missing data rate is less than 10 %, and can be large for a small number of catchments when the missing data rate is up to 20 %.

4 Discussion and conclusions

Researchers are keen to have a comprehensive understanding of rules for excluding catchments with gaps in the streamflow record. Our results indicate that when the streamflow data gaps are up to 10 %, the gap-filled data obtained using hydrological modelling are very reasonable for annual trend analysis and annual streamflow estimates. Choosing the threshold of the 10 % missing data rate will allow the use of

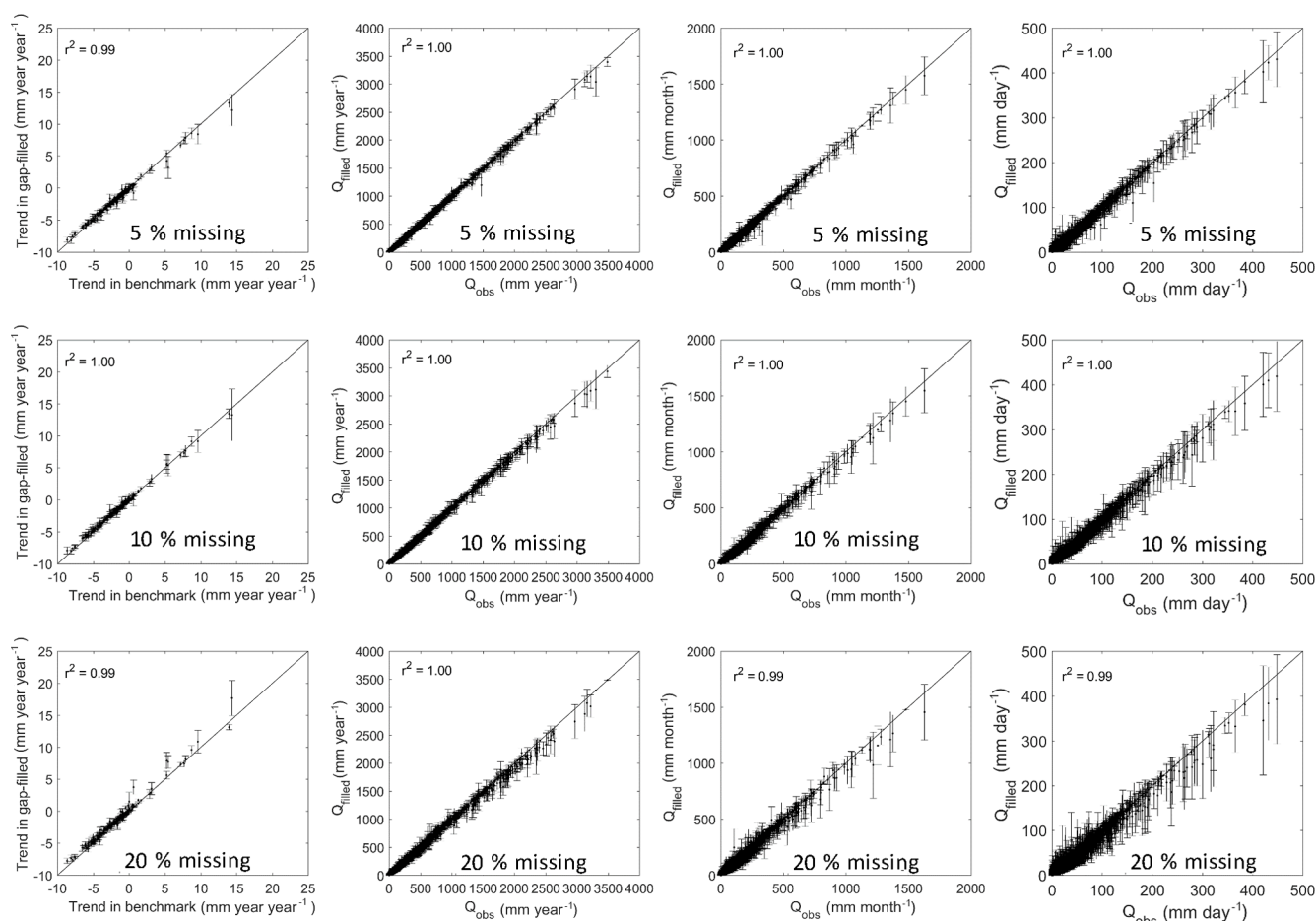


Figure 7. Same as Fig. 6 but using SIMHYD.

many more catchments in modelling and data analysis studies. For example, of the 780 unregulated Australian catchments available for modelling studies (Zhang et al., 2013), there are 237 catchments with a missing data rate of 1%–10% during 1981–2010, accounting for 38% of total available catchments (Fig. 1). Of these 237, 67 (~28%) also have gaps lasting more than 1 year (which we did not consider in this analysis), and therefore these may not be suitable for use. With an increased number of catchments, more reliable large-scale hydrological modelling studies can be carried out (Beck et al., 2016; Parajka et al., 2013; Zhang et al., 2016a).

The missing rate experiments designed in this study are based on the actual missing data patterns obtained from the 780 catchments. In most cases, the number of consecutive missing days is less than 10, as indicated by Fig. 3, indicating brief periods of gauge malfunctions. It is, however, interesting to note that there are streamflow gaps lasting much longer than this in many catchments, with gaps of many months in some cases, noting that we excluded gaps lasting 1 year or more. It is highly likely that filling a gap of 1 year or more will result in biases larger than those presented here.

Furthermore, we also tested the quality of random gap-filled daily streamflow. In that case, the missing data patterns were randomly selected using a random number generator. The results obtained from the random gap filling (not shown) are similar to the results presented here. Thus, it is likely that the length of the gaps (as long as it is less than 1 year) is unlikely to impact the results of the gap-filling experiment. We conclude from this that the use of hydrologic modelling for filling the substantially gapped data (up to a 10% missing data rate) described here for Australia will not impact annual trends of streamflow. Impacts on other streamflow characteristics also need to be examined, as well as seeing if the results obtained in Australia are comparable with those in other parts of the world, where the length of observational gaps may be quite different to those shown in Fig. 3.

It is possible that data gaps may only exist during high flow or low flow conditions, although that is not what we observed here, with the majority of missing data being more or less evenly distributed throughout the year (Fig. 4). We did, however, test the impact of filling streamflow data in high flow or low flow conditions (results not shown here). In these cases, the missing data patterns were selected using only high

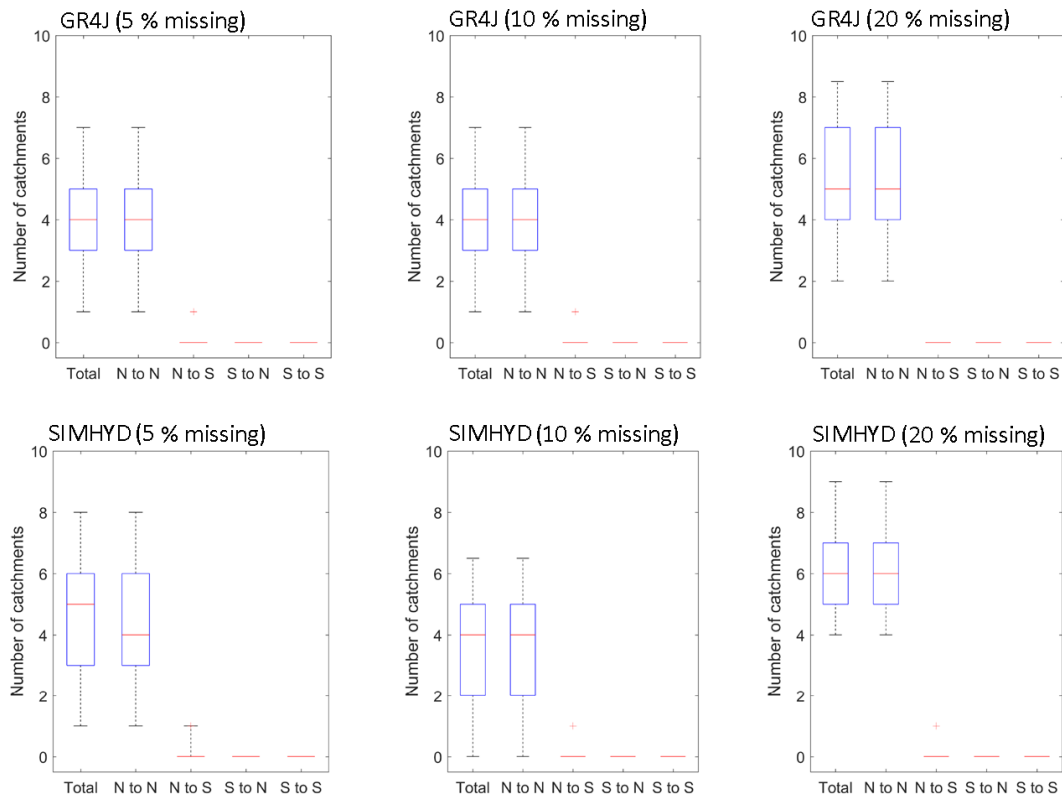


Figure 8. Trend mismatch analysis between the gap-filled and benchmark data. “Total” refers to all the mismatch catchments, “N” denotes non-significant trends ($p > 0.05$), and “S” denotes significant trends ($p \leq 0.05$). The bottom, middle, and top of each box show the 25th, 50th, and 75th percentiles, and the bottom and top whiskers are the 5th and 95th percentiles.

flow (> 95 th percentile) or low flow (< 50 th percentile) data. The results obtained from the low flow gap filling indicates that there is only a negligible influence on annual streamflow trend estimates when the missing data rate is less than 50 %. In contrast, the high flow gap-filled data show a noticeable change in annual streamflow trend when the missing data rate is 5 %. This is understandable since high flow is usually several orders of magnitude higher than low flow, and errors in filling high flow could have large impacts on annual flow and its trends (Slater and Villarini, 2017).

To understand if the quality of gap-filled streamflow is related to catchment attributes and calibration accuracy, we conducted further analysis among the trend bias, model calibration efficiency (i.e. NSE), and catchment aridity index (mean annual potential evaporation divided by mean annual precipitation) (Fig. 10). The model calibration results in dry catchments are normally poorer than those in wet catchments. However, the trend bias ($\text{mm year}^{-1} \text{ year}^{-1}$) obtained from dry catchments is usually smaller. The large biases are observed from the catchments with an aridity index less than 2 and with the calibrated NSE being larger than 0.60. In part, this is to be expected since the streamflow is also lower in more arid catchments, meaning that the trend bias is also likely to be lower.

Figure 11 shows the relationship between the relative trend bias (% , Eq. 4) and aridity index. It shows that not only is the actual trend bias lower in drier catchments, but so too is the relative (%) trend. This result suggests that the large bias in annual trends as a result of gap filling is observed in relatively wet catchments, where model calibrations are reasonably good. This result seems counter-intuitive and requires further exploration, which is beyond the scope of the current paper.

This study focuses on evaluating annual streamflow and its trends. Therefore, we used the Nash–Sutcliffe efficiency plus model bias (Eqs. 5 and 6) to calibrate the two hydrological models. If other hydrological response variables such as low flow metrics are required, other model calibration schemes should be used since the NSE model calibration scheme gives more weight to the reproduction of high flows at the expense of low flows (Zhang et al., 2014). Low flow metrics have important ecological implications (Mackay et al., 2014; Smakhtin, 2001). In general, however, it is challenging to use hydrological modelling for low flow simulations and predictions (Pushpalatha et al., 2012; Staudinger et al., 2011). To obtain credible low flow gap filling, model calibrations should use an objective function that gives more weight to low flows, such as the NSE of daily inverse streamflow and

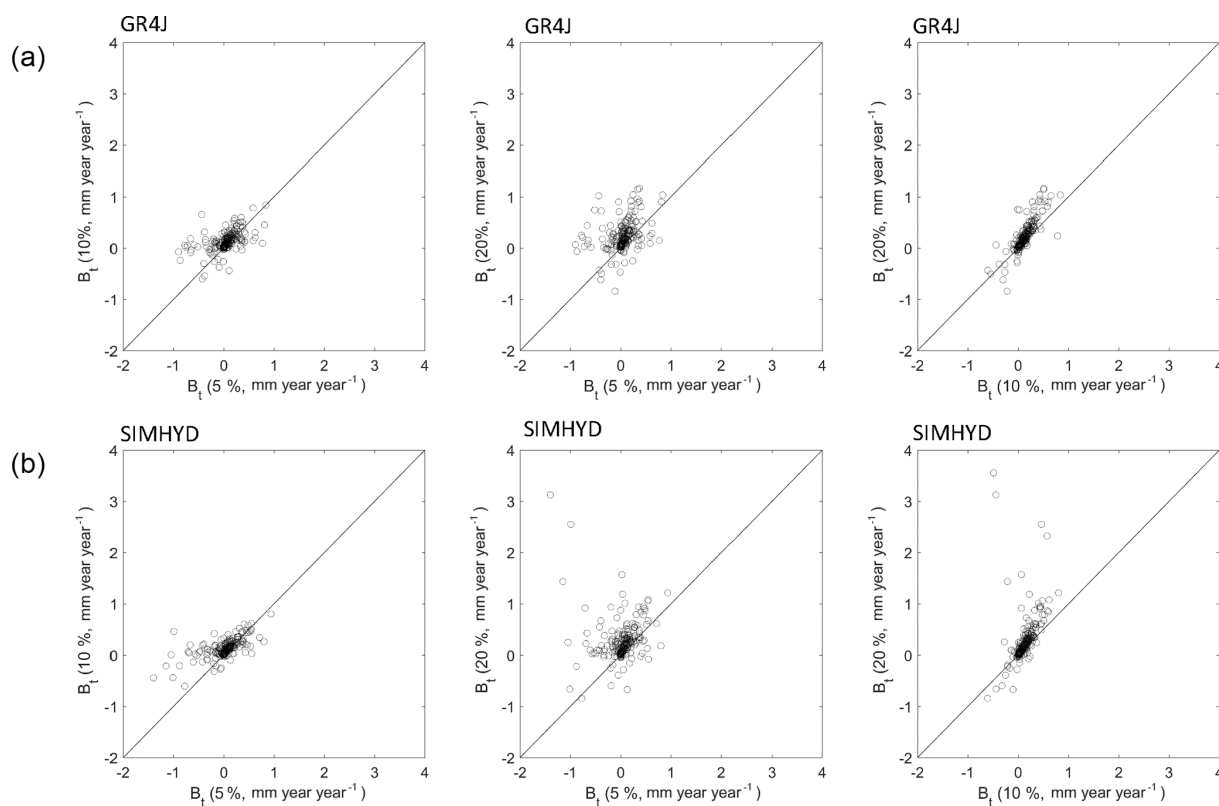


Figure 9. Trend biases comparison between the three groups of gap-filling experiments (5 %, 10 % and 20 %). (a) is for GR4J and (b) is for SIMHYD.

the direct low flow metrics. Another possible method is to combine hydrological modelling with other methods of gap filling, such as using nearby gauges (Lopes et al., 2016) and statistical methods (Gedney et al., 2006b).

It is noted that the infilled data purely refer to the missing data. All streamflow gauges only measure to a certain flow. Once the flow exceeds that level during flooding, the results are interpolated using stage–discharge relationships (Peña-Arancibia et al., 2015). These interpolations could be a major source of observation error. However, investigating high flow interpolation and data quality is beyond the scope of this study.

The modelling experiments and findings from this study could have important implications for other parts of the world as well as Australia. First, to develop appropriate gap-filling modelling experiments, it is necessary to evaluate the distribution of consecutive missing data. The probability distribution of consecutive missing data is skewed toward the low end, which can be nicely simulated using the gamma distribution (Eq. 1). This distribution should be very useful for similar missing data patterns in other regions. Second, hydrological modelling is a very good tool for filling gaps since it can fully take advantage of climate forcing and non-gap streamflow data and obtain the best possible daily simulations. Third, the threshold of 10 % identified in this

study should be applicable to regions/catchments with similar missing data patterns. However, if the data gaps continue for seasons or years, the threshold may not hold.

It would also be interesting to compare hydrological modelling to other approaches for filling streamflow data gaps. Hydrological modelling is a most useful method used in Australia for predicting daily streamflow in ungauged catchments (Chiew et al., 2009; Li and Zhang, 2017; Zhang and Chiew, 2009; Viney et al., 2009). It has been used operationally by the Australian Bureau of Meteorology for filling daily streamflow data gaps for many years. In the future, this operational method could further be comprehensively evaluated against other approaches, such as interpolation or correlation with nearby gauging sites.

In summary, our results clearly demonstrate that the gap-filled data are most accurate when examining trends at the annual scale, followed by the monthly scale, and with least satisfaction at the daily scale. This gives researchers confidence in annual trend analysis, a hot topic in hydrological and climate sciences. Our results also clearly indicate that the gap filling of Australian streamflow data using hydrological models is very reasonable when the missing data rate is less than 10 %, with only a small number of catchments showing a large trend bias when the missing data rate is up to 20 %. The results also indicate that gap-filling drier catch-

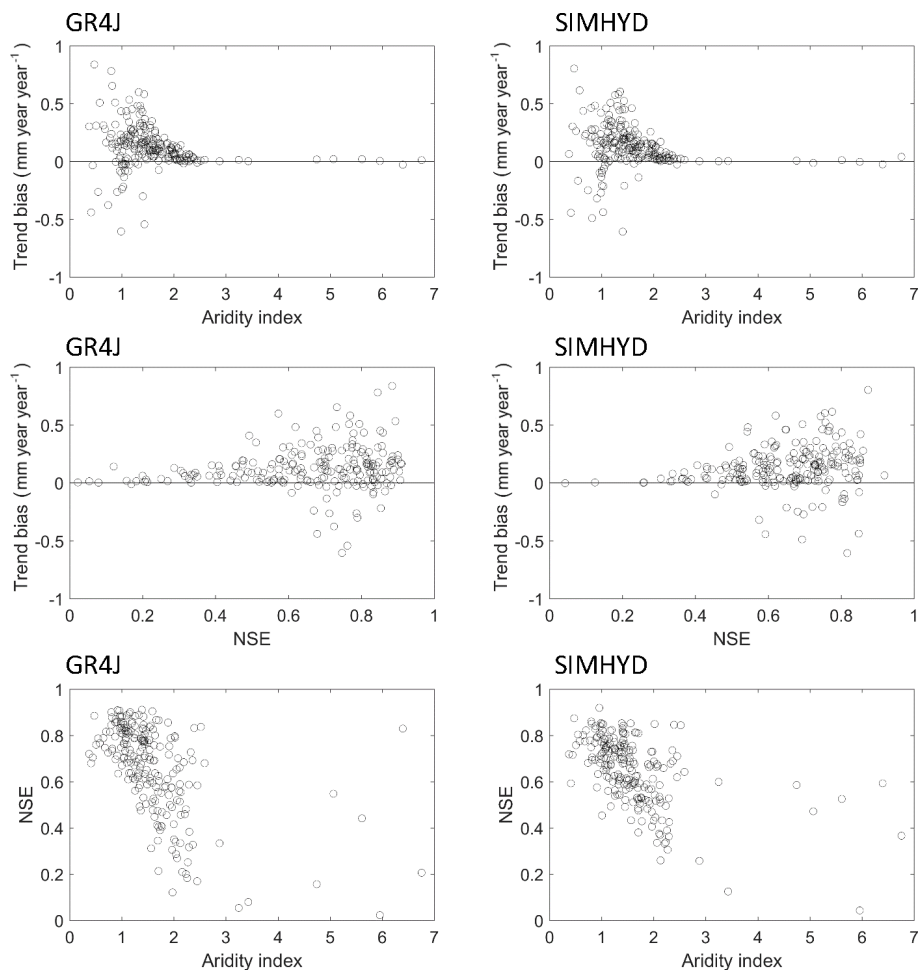


Figure 10. Relationships among trend bias (mm year⁻¹ year⁻¹), model calibration Nash–Sutcliffe efficiency and aridity index for each catchment and for the experiment of the 10 % missing data rate.

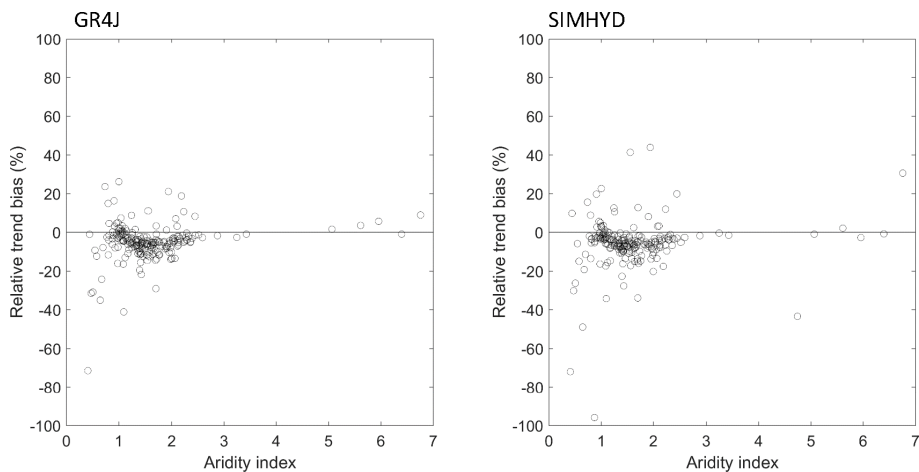


Figure 11. Relationships between relative trend bias (mm year⁻¹ year⁻¹) and aridity index for each catchment and for the experiment of the 10 % missing data rate.

ments appears to be more successful than gap-filling wetter catchments.

Data availability. Streamflow data used in this study are available at <https://doi.org/10.4225/08/58b5baad4fcc2>. The modelling experiment data are freely available upon request from the corresponding author (Yongqiang Zhang, email: yongqiang.zhang2014@gmail.com).

Author contributions. YQZ conceived this study and conducted modelling experiments and data analysis. YQZ finished the first draft and DP modified it. YQZ and DP addressed comments from reviewers.

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