



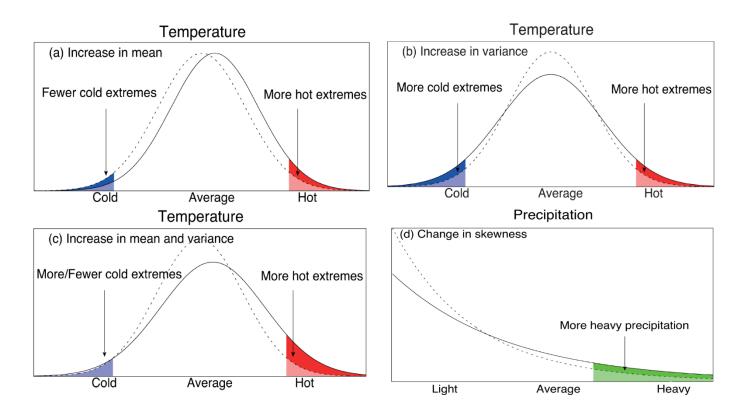
# Supplement of

# Does nonstationarity in rainfall require nonstationary intensity-duration-frequency curves?

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**Figure S1**. IPCC AR5 conceptual representation of changes in probability density functions of daily temperature  $(\mathbf{a} - \mathbf{c})$  and precipitation. The previous and the new distributions are marked by the solid and the dashed lines respectively. The frequency (probability of occurrence) of extremes is denoted by the shaded areas (Source: IPCC AR5 Working Group I report, Figure 1.8, page no. 134).

# SI 1. Infilling Missing AMP Record: Method and Results

# Multiplicative Random Cascade (MRC) Models for Temporal Disaggregation of Rainfall

Multiplicative Random Cascades were first developed for studies of turbulence (Mandelbrot, 1999; Yaglom, 1966) with a motivation to have mathematical models, which produce time series that have statistically scale-invariant properties. In general, random cascade model for rainfall assumes a division of known rainfall total  $R_L$  occurring over an interval of time among a number of smaller intervals of fixed size, which implies a successive fine graining process that starts from an original, large-scale resolution  $R_L$  and continues till a target small-scale resolution is reached. The approach is based on scaling laws, which describe the scale-invariant properties or relationships that connect the statistical properties of rainfall for different timescales (Willems, 2012). The number of subintervals is defined by the branching number b, is set to 2, which is a redistribution of total rainfall in period i at a resolution r,  $R_{i,r}$ , between the amount associated with the first and last half respectively.

Here we implement a micro-canonical (exact conservation of mass in each cascade branching) cascadebased temporal disaggregation model as proposed by (Olsson, 1998), in which daily rainfall is disaggregated using a uniformly distributed generator, dependent on rainfall intensity and position of the rain sequence. The technique was later successfully implemented by (Güntner et al., 2001; Jebari et al., 2012; Rana et al., 2013) for temporal disaggregation of point rainfall and the development of IDF-curves from short-duration rainfall extremes. In the disaggregation process, each time interval (box) at a given resolution (for example 1 day) is split into two half of the original length (1/2 day). The procedure is continued as a cascade until the desired time resolution is reached, i.e., to <sup>1</sup>/4 day, then to 1/8 of a day and so on. Each step is termed as a cascade step, with cascade step 0 as the longest time period with only one box (*i.e.*, a day). The distribution of the volume between two sub-intervals (or smaller boxes) is computed by multiplication with the cascade weights ( $W_{i,r}$ ),  $0 \le W_{i,r} \le 1$ that assigns  $W_{i,r} \bullet R_{i,r}$  to the first half of the period and  $(1 - W_{i,r}) \bullet R_{i,r}$  to the next half. In each branching two possibilities exist: (1)  $W_1 = 0$ ,  $W_1 = 1$  (2)  $0 < W_1 < 1$ . The occurrence of (1) and (2) may be expressed in terms of probabilities,  $P_{01} = P_{(1/0)}$  or  $P_{(0/1)} = P(W_1 = 0$  or  $W_1 = 1$ ) and  $P_{xx} = P_{(x/x)} = P(0 < W_1 < 1) = 1 - P_{01}$ .

Depending on the range of resolution involve,  $P_{01}$  either be assumed as resolution independent or parameterized as a scaling law:  $Pr_{01}(r) = c_1 r^{c_2}$  where  $c_1$  and  $c_2$  are constants. The distribution of  $W_{i,r}$  is termed as cascade generator, assumed to follow 1-parameter beta distribution (Olsson, 2012). Following (Olsson, 1998), the probabilities P, the probability distribution of cascade generator are assumed to be related to (1) position in rainfall sequence, and (2) rainfall volume. The wet boxes, with a rainfall volume V > 0, can be characterized by their position in the rainfall series: (1) the starting box, box preceded by a dry box (V = 0) and succeeded by a wet box (V > 0); (2) the enclosed box, box preceded and succeeded by wet boxes; (3) the ending box, box preceded by a wet box and succeeded by a dry box, and (4) the isolated box, box preceded and succeeded by dry boxes. On the other hand, based on volume dependence, if the volume is large then it is more likely that both halves of the subintervals contribute to nonzero volume than if the volume is small. Following (Olsson, 1998), a partition into three volume classes ( $v_c = 1, 2, 3$ ) was used, separated by percentiles  $33^{rd}$  and  $67^{th}$  of the values at the cascade step. Next, the variation of  $P_{(x/x)}$  with volume is parameterised as,  $P_{(x/x)} = a + b_m \cdot v_c$ , where *a* is the intercept at  $v_c = 0$ ,  $b_m$  is the mean slope of linear regression obtained from all cascade steps and  $v_c$  is volume class. For details about theory and implementation issues of MRC-based disaggregation tool, interested readers are requested to refer (Olsson, 1998).

For calibration and application of the disaggregated model from an original resolution  $R_l$ , two situations are considered: (1) when representative data at target resolution  $R_s$  is available; such as in this case, disaggregation from daily to hourly time steps, in which hourly data were available. Hence, parameters are calibrated over the actual resolution interval  $R_l < r < R_s$  using 5 cascade steps. This implies, 5 successive "halving" from one day to generate 45-minute (2700 seconds) data. (2) When no representative high-resolution data are available, then parameters are estimated by coarse graining from lower resolution  $R_l$  to a higher resolution  $R_s$  by successive disaggregation steps. In this study, it is the disaggregation from daily to minute scales (or sub-hourly time steps), in which no sub-hourly data were available for any of the representative sites. In such case, parameters are calibrated from daily rainfall data using 7 cascade steps. This implies disaggregating by halving from 1-day to 11-minute 15 seconds (675 seconds) data. After calibration, Monte Carlo simulation is performed to gradually fine-grain the data and generate realizations at desired resolution,  $R_s$ . Since  $R_s$  in these cases are not directly achieved by exact resolution doubling from  $R_l$ , the target resolutions are obtained by geometric interpolation of the disaggregation tool using two different sets of observations.

## S 1.1 Performance Evaluation of MRC-based disaggregation Tools for McMaster Weather Station Data

McMaster weather station is situated on a rooftop of McMaster University campus (43.26° N latitude and 79.92° W longitude, 114 m above sea level). We obtain daily, hourly and sub-hourly (15-min) rainfall information from the year 2010 to 2013, archived at McMaster Weather Station (MUWS; <u>http://geomedia.mcmaster.ca/muws/weatherstation.html</u>) website. The time slice was chosen based on data completeness and quality of available records.

We investigate two cases: (1) First, we calibrate the model using 1-year (2012 - 2013) hourly data, estimated model parameters, and then assess the performance of disaggregated model output using 2010 - 2013 observed data (2) Next, the observed 15-min time series was first aggregated to an hourly time step and then calibrated the model using aggregated hourly data. Then we compare disaggregated versus observed data at a 15-min temporal resolution for validation. Since we do not have 15-min daily rainfall information available for any of rain gauge locations, in both cases we calibrate the model using hourly data, which in turn gives us the opportunity to evaluate the performance of the disaggregation algorithm. In all cases, disaggregation was performed from daily time scales. Table S1 shows results of disaggregation experiments. We find a satisfactory performance between

observed and simulated model output, especially for the simulation of the percentage of zero values. However, we find a slight underestimation for simulated standard deviations of event volume and duration, whereas variance of mean inter-arrival time is overestimated.

Time scale	Metrics	Observed	Simulated
Hourly (1-hr)	Zero values (%)	92	91.5
	Individual Rainfall volume (mean $\pm$ SD) mm	$1.60\pm2.95$	$1.45\pm2.89$
	Event volume (mean $\pm$ SD) mm	$4.52 \pm 10.40$	$4.50\pm8.82$
	Event duration (mean $\pm$ SD) hour	$2.83 \pm 3.51$	$3.09 \pm 2.69$
	Mean inter-arrival time between event, hour	$36.82\pm64.70$	$37.33 \pm 65.10$
	Mean annual maxima (mean $\pm$ SD) mm	$39.97 \pm 21.42$	$32.97 \pm 12.33$
Minute	Zero values (%)	94.63	95.35
(15-min)	Individual Rainfall volume (mean $\pm$ SD) mm	$0.032 \pm 1.20$	$0.031 \pm 1.28$
	Event volume (mean $\pm$ SD) mm	$1.87 \pm 6.28$	$1.96 \pm 4.64$
	Event duration (mean $\pm$ SD) hour	$3.15\pm5.77$	$2.94 \pm 3.47$
	Mean inter-arrival time between event, hour	$59.54 \pm 177.33$	$64.12\pm182.01$
	Mean annual maxima (mean ± SD) mm	$20.4\pm10.22$	$23.4 \pm 12.70$

 Table S1. Comparison between observed and disaggregated 15-min and 1-hour time series for McMaster Weather

 Station Data

# S 1.2 Performance Evaluation of MRC-based disaggregation Tools for the Nine Locations in Southern Ontario

Figures S2 – S8 display disaggregation fit of the MRC-based tools for Toronto International Airport. Figure S2 presents variations of probability with volume classes, which often show substantial differences between the classes. The figure shows a linear relationship between precipitation, *P* and volume class, v<sub>c</sub> changes with cascade steps. The mean regression line  $a_p + b_m^*vc$ , (where  $a_p$  is the intercept and  $b_m$  is the slope) is shown as a dashed line with squares (Figure S2). Figures S3 and S4 show variations of intercepts with cascade steps. The probabilities P(x/x) and P(0/1) for daily to minute-scale disaggregation of four different type of boxes are shown in Tables S2 and S3. P(x/x) can be modelled assuming linear dependence on the cascade step, which is given as, P(x/x)= $a_p + b_m^*vc$  with  $a_p$  is estimated as,  $a_p = c_1 + c_2^*C_s$ , where  $c_1$  and  $c_2$  are the slopes and the intercept of the linear regression. Since P(0/1) [or P(1/0)] is relatively independent of cascade step, it can be modeled using  $a_p + b_m^*vc$ . Finally, P(0/1) [or P(1/0)] can be estimated as, P(0/1)=1-(P(x/x)+P(1/0) [or P(1/0)=1-(P(x/x)+P(0/1)]]. The empirical histograms (the observed, shown in bars) and the fitted beta distributions (shown in lines) [Figures S5 and S6] show a good agreement in the overall fit. However, at higher cascade steps, i.e. finer time scales, the number of bins in the histogram is small, and the fits appear naturally uncertain.

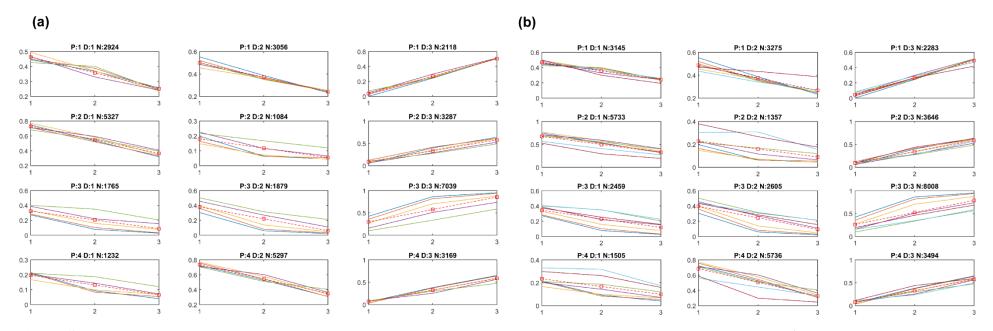
Figure S7 shows time series of disaggregated versus observed annual maxima (the 15-min and 1-hour) for Toronto International Airport. The Quantile Mapping (QM) is employed to adjust occasional overestimation due to disaggregation. Except for a few extremes, we find a close agreement between the observed versus bias-corrected disaggregated annual maxima time series. For example, the algorithm overestimates the wettest event in Toronto (137.4 mm of rainfall) during Hurricane Hazel (1954) at hourly disaggregation time steps. However, due to lack of observation, we could not validate 15-min disaggregation model performance. Figure S8 shows 1-hour disaggregated model performance for the nine sites. Although we find evidence of occasional overestimations in disaggregated model output, the adjustment of extremes by QM could correct biases to some extent. However, the algorithm fails to correct extreme wet biases for London International Airport (during 1954), Trenton Airport (2000), Stratford WWTP (2002) and Fergus Shand Dam (2004 and 2006).

					1 21	•		00 0						
			1. Isol	ated Box $(b_m = 0)$	0.223)									
Volume	1	2	3	4	5	6	7	Mean						
Class/Cascade Step	р													
1	0.001	0.030	0.051	0.048	0.073	0.082	0.031	0.045						
2	0.244	0.254	0.266	0.299	0.249	0.289	0.267	0.27						
3	0.509	0.505	0.510	0.513	0.512	0.470	0.420	0.49						
2. Starting Box $(b_m = 0.244)$														
2. Starting Box (b <sub>m</sub> = 0.244)         1       0.054       0.122       0.081       0.064       0.101       0.130       0.095       0.092														
2	0.399	0.415	0.345	0.290	0.275	0.283	0.437	0.349						
3	0.635	0.612	0.610	0.527	0.487	0.570	0.628	0.581						
			3. Enc	losed Box $(b_m =$	0.263)									
1	0.423	0.357	0.272	0.157	0.097	0.156	0.194	0.236						
2	0.862	0.817	0.703	0.510	0.335	0.345	0.463	0.576						
3	0.951	0.938	0.875	0.736	0.585	0.562	0.685	0.762						
			<b>4.</b> En	ding Box $(b_m = 0)$	).247)									
1	0.063	0.033	0.064	0.087	0.084	0.109	0.114	0.079						
2	0.381	0.372	0.323	0.253	0.303	0.237	0.439	0.330						
3	0.651	0.639	0.591	0.564	0.474	0.496	0.593	0.572						

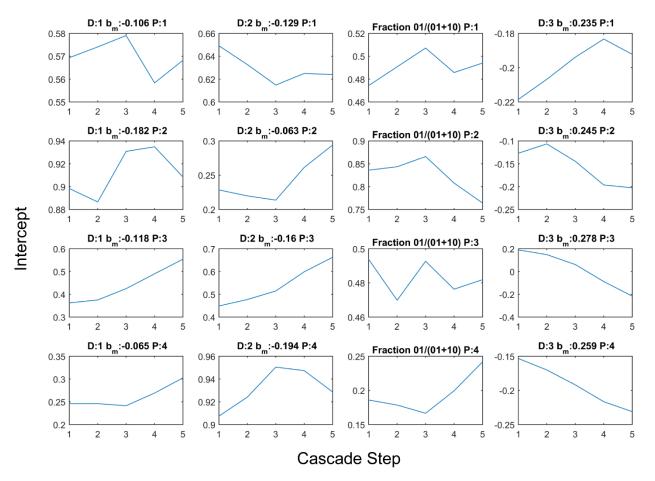
**Table S2.** Probabilities P(x/x) as function of volume class, cascade step and type of box for daily to minute scale disaggregation

		1. Isolated	<b>d Box</b> $(b_m = -0.11)$	13)			
1	2	3	4	5	6	7	Mean
0.446	0.449	0.494	0.466	0.427	0.482	0.50	0.466
0.369	0.388	0.370	0.330	0.400	0.369	0.30	0.361
0.257	0.248	0.236	0.242	0.241	0.259	0.193	0.239
		2. Starting	$g \operatorname{Box} (b_m = -0.1')$	75)			
0.747	0.713	0.771	0.711	0.681	0.565	0.526	0.673
0.535	0.521	0.583	0.593	0.558	0.409	0.295	0.499
0.320	0.333	0.347	0.408	0.394	0.274	0.195	0.324
		3. Enclose	$\mathbf{d} \operatorname{Box} (b_m = -0.1$	13)			
0.272	0.283	0.330	0.387	0.400	0.405	0.374	0.350
0.078	0.103	0.159	0.220	0.350	0.348	0.253	0.216
0.027	0.031	0.077	0.154	0.204	0.224	0.158	0.125
		4. Ending	$a_{m} = -0.06$	(8)			
0.215	0.211	0.167	0.202	0.210	0.330	0.298	0.233
0.093	0.083	0.098	0.144	0.187	0.318	0.263	0.169
0.040	0.054	0.068	0.072	0.120	0.174	0.159	0.098
	0.369 0.257 0.747 0.535 0.320 0.272 0.078 0.027 0.215 0.093	0.446       0.449         0.369       0.388         0.257       0.248         0.747       0.713         0.535       0.521         0.320       0.333         0.078       0.103         0.027       0.031         0.215       0.211         0.093       0.083	1       2       3         0.446       0.449       0.494         0.369       0.388       0.370         0.257       0.248       0.236 <b>2. Starting</b> 0.747       0.713       0.771         0.535       0.521       0.583         0.320       0.333       0.347 <b>3. Enclose</b> 0.272       0.283       0.330         0.078       0.103       0.159         0.027       0.031       0.077 <b>4. Ending</b> 0.215       0.211       0.167         0.093       0.083       0.098	1         2         3         4 $0.446$ $0.449$ $0.494$ $0.466$ $0.369$ $0.388$ $0.370$ $0.330$ $0.257$ $0.248$ $0.236$ $0.242$ <b>2. Starting Box</b> ( $b_m = -0.1^{\prime}$ $0.747$ $0.713$ $0.771$ $0.711$ $0.535$ $0.521$ $0.583$ $0.593$ $0.320$ $0.333$ $0.347$ $0.408$ <b>3. Enclosed Box</b> ( $b_m = -0.1^{\prime}$ $0.272$ $0.283$ $0.330$ $0.387$ $0.078$ $0.103$ $0.159$ $0.220$ $0.027$ $0.031$ $0.077$ $0.154$ <b>4 4 4 6 6 6 6 6 6 6 6 6 6</b>	$0.446$ $0.449$ $0.494$ $0.466$ $0.427$ $0.369$ $0.388$ $0.370$ $0.330$ $0.400$ $0.257$ $0.248$ $0.236$ $0.242$ $0.241$ <b>2. Starting Box (<math>b_m</math> = -0.175</b> ) $0.747$ $0.713$ $0.771$ $0.711$ $0.681$ $0.535$ $0.521$ $0.583$ $0.593$ $0.558$ $0.320$ $0.333$ $0.347$ $0.408$ $0.394$ <b>Box (<math>b_m</math> = -0.113</b> ) $0.272$ $0.283$ $0.330$ $0.387$ $0.400$ $0.078$ $0.103$ $0.159$ $0.220$ $0.350$ $0.027$ $0.031$ $0.077$ $0.154$ $0.204$ <b>Lending Box (<math>b_m</math> = -0.068)</b> $0.215$ $0.211$ $0.167$ $0.202$ $0.210$ $0.093$ $0.083$ $0.098$ $0.144$ $0.187$	123456 $0.446$ $0.449$ $0.494$ $0.466$ $0.427$ $0.482$ $0.369$ $0.388$ $0.370$ $0.330$ $0.400$ $0.369$ $0.257$ $0.248$ $0.236$ $0.242$ $0.241$ $0.259$ <b>2. Starting Box</b> ( $b_m = -0.175$ ) $0.747$ $0.713$ $0.771$ $0.711$ $0.681$ $0.565$ $0.535$ $0.521$ $0.583$ $0.593$ $0.558$ $0.409$ $0.320$ $0.333$ $0.347$ $0.408$ $0.394$ $0.274$ <b>3. Enclosed Box</b> ( $b_m = -0.113$ ) $0.272$ $0.283$ $0.330$ $0.387$ $0.400$ $0.405$ $0.078$ $0.103$ $0.159$ $0.220$ $0.350$ $0.348$ $0.027$ $0.031$ $0.077$ $0.154$ $0.204$ $0.224$ <b>4. Ending Box</b> ( $b_m = -0.068$ ) $0.215$ $0.211$ $0.167$ $0.202$ $0.210$ $0.330$ $0.093$ $0.083$ $0.098$ $0.144$ $0.187$ $0.318$	1234567 $0.446$ $0.449$ $0.494$ $0.466$ $0.427$ $0.482$ $0.50$ $0.369$ $0.388$ $0.370$ $0.330$ $0.400$ $0.369$ $0.30$ $0.257$ $0.248$ $0.236$ $0.242$ $0.241$ $0.259$ $0.193$ <b>2. Starting Box</b> ( $b_m = -0.175$ ) $0.747$ $0.713$ $0.771$ $0.711$ $0.681$ $0.565$ $0.526$ $0.535$ $0.521$ $0.583$ $0.593$ $0.558$ $0.409$ $0.295$ $0.320$ $0.333$ $0.347$ $0.408$ $0.394$ $0.274$ $0.195$ <b>3. Enclosed Box</b> ( $b_m = -0.113$ ) <b>4. Ending Box</b> ( $b_m = -0.068$ ) <b>4. Ending Box</b> ( $b_m = -0.068$ ) <b>4. Ending Box</b> ( $b_m = -0.068$ ) $0.215$ $0.211$ $0.167$ $0.202$ $0.210$ $0.330$ $0.298$ $0.093$ $0.083$ $0.098$ $0.144$ $0.187$ $0.318$ $0.263$

**Table S3.** Probabilities P(0/1) as function of volume class, cascade step and type of box for daily to minute scale disaggregation



**Figure S2**. Variation of probabilities with volume class,  $v_c$  for Toronto International Airport at (*a*) daily to hourly-, and (*b*) daily to minutetime step disaggregation. X-axes show,  $v_c$ : 1 – small, 2 – medium, and 3 – large; Y-axes show, probabilities. *P* – denotes position type, 1: Isolated, 2: Starting, 3: Enclosed, and 4: Ending, *D* denotes division type (1: 0/1, 2: 1/0, 3: x/x), and N denotes the total number of periods for associated position and division type. The solid lines marked with different colors indicate different cascade steps. The dashed line with squares represents the mean of all cascade levels.



**Figure S3**. Variations of intercept,  $a_p$  with cascade steps for daily to hourly- time step disaggregation at Toronto International Airport. *P*-denotes position types, 1: Isolated, 2: Starting, 3: Enclosed and 4: Ending. *D* denotes division type (1: 0/1, 2: 1/0, 3: x/x), and  $b_m$  indicates the mean slope for corresponding position and division type, estimated from the fitted mean lines as in Figure S3. The third column indicates the fraction of 0/1-divisions of all "non-x/x-divisions" summed over volume classes.

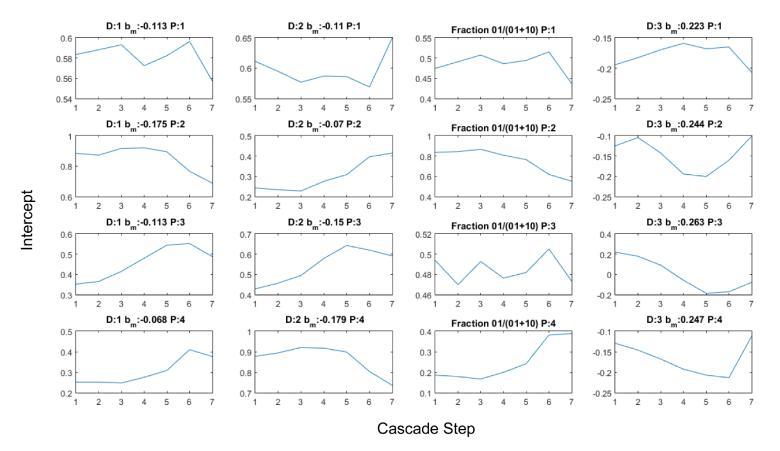
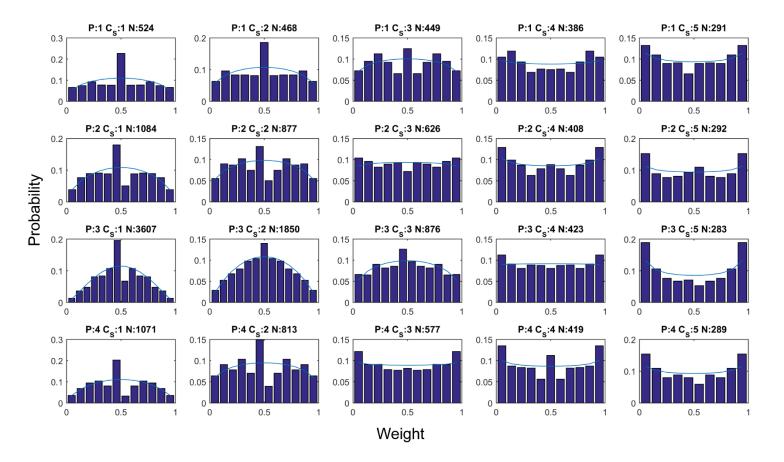


Figure S4. Same as in Figure S3 but for daily to minute- time step disaggregation.



**Figure S5**. Variations of empirical x/x-distributions with cascade steps (bars) and fitted beta distributions (lines) for daily to hourly- time step disaggregation at Toronto International Airport. *P*-denotes position types, 1: Isolated, 2: Starting, 3: Enclosed and 4: Ending; *C*<sub>s</sub> denotes cascade steps, for example, step 1 shows cascading from 32 to 16 minute, step 2 indicates from 16 to minute and so on. *N* indicates the total number of x/x- divisions for this position type and cascade level.

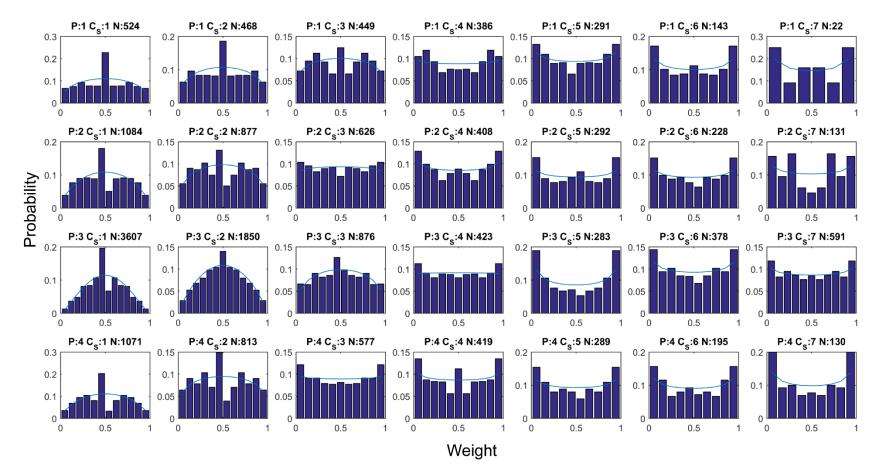
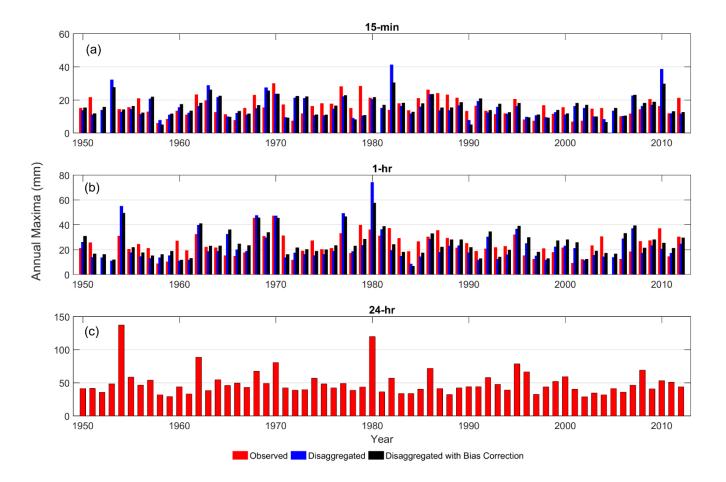


Figure S6. Same as in Figure S5 but for daily to minute- time step disaggregation.



**Figure S7**. Comparison of observed versus disaggregated (**a**) sub-hourly and (**b**) hourly Annual Maximum (AM) rainfall values (Observed – red, disaggregated – blue and disaggregated and bias corrected - black) for Toronto International Airport. (**c**) The bottom panel shows AM daily rainfall values. A multiplicative random cascade-based disaggregation tool is used to disaggregate daily rainfall time series into a sub-hourly and hourly time step.

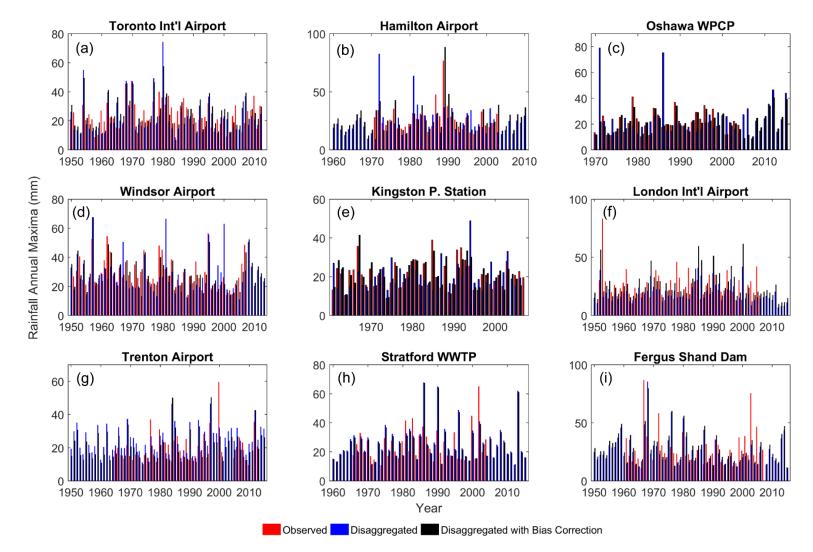


Figure S8. Comparison of observed versus disaggregated time series for 1-hour AMP across nine locations (a-g)

# SI 2 Trend and Change point, Autocorrelation: Methods and Results SI 2.1 Detection of Monotonic trend: Mann-Kendall Test Statistics

The null hypothesis  $H_0$  of the test assumes that no temporal trend exists in the data and the alternate hypothesis  $H_1$  assumes that a significant temporal trend (upward or downward) exists. The test statistic  $Z_{MK}$  is computed as (Hirsch et al., 1982)

$$Z_{MK} = \begin{cases} \frac{S-1}{\sqrt{Var(S)}} & \text{if } S > 0; \\ 0, & \text{if } S = 0; \\ \frac{S+1}{\sqrt{Var(S)}} & \text{if } S < 0 \end{cases}$$
(2.1)

where S is defined by,

$$S = \sum_{k=1}^{n-1} \sum_{j=k+1}^{n} \operatorname{sgn}(x_j - x_k) = \begin{cases} 1, & \text{if } (x_j - x_k) > 0\\ 0, & \text{if } (x_j - x_k) = 0\\ -1, & \text{if } (x_j - x_k) < 0 \end{cases}$$
(2.2)

where  $x_j$  and  $x_k$  are the data points in time periods j and k (j > k) respectively, and n is number of observed data points. For  $n \ge 10$ , the test statistic S is approximately normally distributed with the mean of E(S) = 0, and the variance of,

$$Var(S) = \frac{1}{18} \left[ n(n-1)(2n+5) - \sum_{i=1}^{g} t_i . (i) . (i-1) . (2i+5) \right]$$
(2.3)

where g is the number of tied groups and  $t_i$  is the number of data points in the  $i^{th}$  group.

# SI 2.2 Detection of Abrupt or Step Change

#### SI 2.2.1 General Formulation of Sequential Change Point Test

When a sequence of random variables is divided into two segments represented by  $x_1, ..., x_{t_0}$  and  $x_{t_0+1}, x_{t_0+2}, ..., x_{t_0}$ , if each segment has distribution functions,  $F_1(x)$  and  $F_2(x)$ , where  $F_1(x) \neq F_2(x)$ , then change point is identified at  $t_0$ . Thus the null hypothesis of the test is "no change",  $H_0: \tau = T$  against the alternative of "change"  $H_1: 1 \le \tau < T$ . Suppose *t* points in the sequence of observations and we wish to test whether a change point has occurred at some point in the historical observation. For any fixed k < t the hypothesis that a change point occurs at the  $k^{th}$  observation can be written as (Ross et al., 2011)

$$H_{o} \forall i \quad X_{i} \sim F_{0}, \quad H_{1} \colon X_{i} \sim \begin{cases} F_{0} & \text{if } i < k \\ F_{1} & \text{if } i \geq k \end{cases}$$

$$(2.4)$$

Now a two-sample hypothesis test can be used to test for a change point at a location k using a test statistic  $N_{k,t}$ . The test statistic  $N_{k,t}$  can be evaluated for all values of 1 < k < t, and then using the maximum value, *i.e.*,

$$N_{\max,t} = \max_{k} N_{k,t} \tag{2.5}$$

Then, the hypothesis that no change has occurred before the  $t^{th}$  observation is rejected if  $N_{\max,t} > h_t$  at a threshold  $h_t$ . The value  $\tau$  of the change point is then the value of k which maximizes  $N_{\max,t}$ 

## Change Point in Location

#### Pettitt Change Point Test

The test is based on following statistic (Serinaldi and Kilsby, 2016; Xie et al., 2014)

$$K_T = \max_{1 \le t \le T} \left| U_{t,T} \right| \tag{2.6}$$

Where  $U_{t,T}$  the ranked sample as is defined in Eq. 2.2. The statistical significance of Pettitt test quantified by *p*-value is approximately evaluated as (Xie et al., 2014),  $p = 2\exp\left(\frac{-6K_T^2}{T^2 + T^3}\right)$ . Given a certain significance level  $\alpha$ , if  $p < \alpha$ , we reject the null hypothesis and conclude that  $x_\tau$  is a significant change point at level  $\alpha$ . The analysis was performed using R statistical software with add-on package "trend".

#### Mann-Whitney Change Point Test

Mann-Whitney (MW) test statistics detect shifts in location parameter in the time series. The test is based on the following observation: if there are *n* points spread over two samples *S* and *T*, containing  $n_s$  and  $n_t$  points respectively,  $n = n_s + n_t$ . The MW U statistic is then defined as (Ross, 2013)

$$U' = r_s - \frac{n_s \left(n_s + 1\right)}{2}$$
(2.7)

Where  $r_s$  is the sum of the ranks of the points in sample *S*. Under the null hypothesis that *S* and *T* have equal location parameter, the distribution of of *U* is independent of the distribution of the observations in two samples and its first two moments are

$$\mu_{U'} = n_s n_t / 2, \ \sigma_{U'}^2 = n_s n_t \left( 1 + n_s + n_t \right) / 12 \tag{2.8}$$

The standardized MW statistic,  $U = |(U' - \mu_{U'})/\sigma_{U'}|$  (2.9)

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A nonparametric change point for location shifts is then defined as by replacing  $N_{\text{max},t}$  with this U statistic.

# Change Point in Scale: Mood Test

The Mood Test uses a test statistic which measures the extent to which the rank of each point deviates from its expected value (Ross et al., 2011)

$$M' = \sum_{x_i \in S} \left( r(x_i) - (n+1)/2 \right)^2$$
(2.10)

Where  $r(x_i)$  denotes the rank of  $x_i$  in the pooled sample. Similar to MW statistic, the distribution of Mood statistic is independent of the underlying random variables. The mean and variance of the Mood statistic is given as

$$\mu_{M'} = n_s \left( n^2 - 1 \right) / 12, \ \sigma_{M'}^2 = n_s n_T \left( n + 1 \right) \left( n^2 - 4 \right) / 180$$
(2.11)

Then the standardized statistic is given as (Ross et al., 2011)

$$M = \left| \left( M' - \mu_{M'} \right) / \sigma_{M'} \right| \tag{2.12}$$

Similar to MW statistic, a nonparametric change point for scale shifts is defined as by replacing  $N_{\max,t}$  with this *M* statistic. Both Mann-Whitney and Mood tests were performed using R statistical software with add-on package "cpm".

# SI 2.3 Non-parametric Trend Free Pre-Whitening (TPFW) for Correction of Autocorrelation

To correct the autocorrelation present in the data, we followed the non-parametric procedure of trend-free prewhitening (TPFW) as suggested by the (Petrow and Merz, 2009):

• At first, the trend of annual maxima time series of a particular duration is estimated by the nonparametric trend slope estimator,  $\beta$  as suggested by (Sen, 1968), which is the median of all pair wise slopes ( $b_i$ ) in the time series of length (N):

$$\beta = \begin{cases} b_{(N+1)/2} & \text{if } N \text{ is odd} \\ \frac{1}{2} \left( b_{N/2} + b_{(N+1)/2} \right) & \text{if } N \text{ is even} \end{cases}$$
(2.13)

Where,  $b_i = \frac{(x_j - x_k)}{j - k}$ , i = 1, 2, ..., N and j > k, and  $x_j$  and  $x_k$  are the data points in time periods j and k (j

> k) respectively. Hence, if there are n values of data in the time series, it results into as many as  $N = {}^{n}C_{2}$  number of  $b_{i}$  values.

• Secondly, the computed trend is removed from the original series:

$$Y_t = X_t - \beta \times t \tag{2.14}$$

Where,  $X_t$  is the original time series and t is the time.

• Next, the lag1- autocorrelation [ $\rho$ , using MATLAB function 'autocorr ()'], is computed from  $Y_t$ . If no statistically significant (significance is checked at 5 and 10% significance level) autocorrelation is found, the trend and change-point detection algorithms are directly applied to the original time series. Otherwise, the lag-1 autocorrelation is removed from the time series:

$$Y_t' = Y_t - \rho \times Y_{t-1} \tag{2.15}$$

• Finally, the removed trend in the first step is added back into the time series free from trend and autocorrelation.

$$Y_t'' = Y_t' + \beta \times t \tag{2.16}$$

The resulting time series Y'' includes the original trend but free from autocorrelation.

Time Slice	Ljung- Box Test	Augme Dickey- Tes	Fuller	KPSS	Test	Mann-Ken	dall Tren	d Test	Priestley- Subbarao Test		M	ann-Whitn Point 7	• 0	Мос	od Change	Point Test
	p-value	Test statistics	p- value	Test statistics	p- value	MK <sub>Z</sub>	β	p- value	p-value	p-value	Year	Test statistics	Threshold	Year	Test statistics	Threshold
15-min	0.014**	-0.326	0.53**	0.120	$0.098^{*}$	-0.71	-0.23	0.48	0.383	0.141	Х	Х	Х	Х	Х	Х
30-min	$0.027^{**}$	-0.177	$0.58^{**}$	0.123	$0.092^{*}$	-0.52	-0.25	0.61	0.283	0.179	х	х	Х	х	х	Х
1-hr	0.805	-0.077	0.62**	0.138	$0.064^{*}$	0.39	0.22	0.69	0.409	0.368	х	х	Х	Х	х	Х
2-hr	0.920	0.043	0.66**	0.129	$0.081^{*}$	-0.07	-0.05	0.94	0.143	0.564	х	х	х	Х	Х	Х
6-hr	0.959	0.051	$0.67^{**}$	0.060	> 0.10	-0.61	-0.48	0.54	0.025	0.733	х	х	х	Х	х	Х
12-hr	0.965	0.106	$0.67^{**}$	0.065	> 0.10	-0.55	-0.49	0.58	2.0e <sup>-4**</sup>	0.659	х	х	х	Х	х	Х
24-hr	0.885	0.106	0.69**	0.046	> 0.10	-0.06	-0.06	0.95	0.046**	-†	х	Х	х	х	Х	Х

Table S4. Detection of trends and nonstationarity in Toronto Pearson International Airport

<sup>\*\*</sup> and <sup>\*</sup> indicate statistically significant at 5% and 10% significance levels, 'x' denotes no change point is detected using Mann-Whitney and Mood tests respectively.  $\beta$  indicates slope per decade calculated using Theil-Sen method. *P-values* larger than 0.1 in KPSS test indicates test statistics are non-significant, whereas *p-values* smaller than 0.01 are considered to be highly significant. The standardized Mann-Kendall test statistic (MK<sub>Z</sub>) is positive (negative) with an increasing (decreasing) trend, and statistically significant at 5% and 10% significance levels when  $|MK_Z| > 1.96$  and  $|MK_Z| > 1.64$  respectively. Change point tests are performed at 10% significance level. †*p*-values are not reported due to analytical intractability.

Table S4.1 Detection of trends and nonstationarit	v after	performing	TFPW in	Toronto	Pearson	International A	virport

Time Slice	Ljung- Box Test	Augme Dickey-l Tes	Fuller	KPSS	Test	Mann-H	Kendall T Test	Frend	Priestley- Subbarao Test	Pettitt Test	Mar	nn-Whitne Point T		Mood	l Change I	Point Test
	p-value	Test statistics	p- value	Test statistics	1		β	p- value	p-value	p-value	Year	Test statistics	Threshold	Year	Test statistics	Threshold
15-min	0.258	-0.60**	0.43	0.089	>0.10	-0.17	-0.04	0.87	0.504	0.531	Х	Х	Х	х	Х	Х
30-min	0.243	-0.35**	0.52	0.098	>0.10	0.07	0.05	0.94	0.498	0.777	Х	Х	Х	Х	Х	Х

Time Slice	Ljung- Box Test	Augmo Dickey- Tes	Fuller	KPSS	Test	Mann-F	Kendall 7 Test	Frend	Priestley- Subbarao Test	Pettitt Test	Ma	nn-Whitney Point Te	0	Мо	od Change Test	Point
	p-value	Test statistics	p- value	Test statistics	p- value	MK <sub>Z</sub>	β	p- value	p-value	p-value	Year	Test statistics	Threshold	Year	Test statistics	Threshold
15-min	0.173	-0.454	$0.48^{**}$	0.033	>0.10	-0.65	-0.24	0.516	0.406	0.438	Х	Х	Х	Х	Х	Х
30-min	0.911	-0.428	0.49**	0.047	>0.10	-1.186	-0.45	0.236	2.56e <sup>-5**</sup>	0.402	Х	Х	Х	Х	Х	Х
1-hr	0.918	-0.170	$0.58^{**}$	0.082	>0.10	0.244	0.28	0.807	$0.002^{**}$	0.870	Х	Х	Х	Х	Х	Х
2-hr	0.735	-0.176	0.58**	0.154	0.043**	1.023	0.75	0.306	8.03e <sup>-6**</sup>	0.300	Х	Х	Х	Х	Х	Х
6-hr	$0.099^{*}$	-0.138	0.60**	0.193	0.019**	-0.097	-0.11	0.922	3.49e <sup>-9**</sup>	0.216	Х	Х	Х	Х	Х	Х
12-hr	0.150	-0.055	0.63**	0.183	0.023**	-0.122	-0.14	0.903	2.78e <sup>-10**</sup>	0.506	Х	Х	Х	Х	Х	Х
24-hr	$0.059^{*}$	-0.035	0.63**	0.307	0.010**	0.309	0.39	0.758	1.82e <sup>-7**</sup>	0.199	Х	Х	Х	Х	Х	Х

Table S5. Detection of trends and nonstationarity in Hamilton Airport

Table S5.1 Detection of trends and nonstationarity after performing TFPW in Hamilton Airport

Time Slice	Ljung -Box Test	Augme Dickey- Tes	Fuller	KPSS Te	st	Mann-K	endall T Test	rend	Priestley- Subbarao Test	Pettitt Test	Mai	nn-Whitney Point To	0	Моо	d Change	Point Test
	p- value	Test statistics	p-value	Test statistics	p- value	MK <sub>Z</sub>	β	p- value	p-value	p-value	Year	Test statistics	Threshold	Year	Test statistics	Threshold
6-hr	0.108	-0.211	$0.570^{**}$	0.197	0.02**	-0.02	-0.03	0.981	2.83e <sup>-6**</sup>	0.227	Х	Х	Х	Х	Х	X
24-hr	0.282	-0.202	0.573**	0.282	0.01**	0.318	0.41	0.751	9.78e <sup>-4**</sup>	0.316	Х	х	Х	Х	Х	Х

Time Slice	Ljung -Box Test	Augme Dickey-l Tes	Fuller	KPSS T	lest	Mann-	Kendall Test	Trend	Priestley- Subbarao Test	Pettitt T	est Ma	nn-Whitne Point Te		Mood	Change Po	int Test
	p- value	Test statistics	p- value	Test statistics	p- value	MK <sub>Z</sub>	β	p-value	p-value	p-value	Year	Test statistics	Threshold	Year	Test statistics	Threshold
15-min	0.986	-0.152	0.59**	0.044	>0.10	0.93	2.12	0.35	0.18	0.89	Х	Х	Х	Х	X	Х
30-min	0.620	-0.251	0.55**	0.045	>0.10	0.73	1.02	0.47	0.92	-	Х	Х	Х	1974	$2.62^{*}$	2.59
1-hr	0.994	-0.065	0.62**	0.081	>0.10	1.29	1.5	0.20	0.57	0.562	Х	Х	Х	Х	Х	Х
2-hr	0.938	-0.116	0.61**	0.08	>0.10	1.68	0.82	$0.09^{*}$	0.005**	0.259	2009	2.64*	2.58	Х	Х	Х
6-hr	0.924	-0.311	0.53**	0.075	>0.10	1.49	0.3	0.14	0.027**	0.248	Х	Х	Х	Х	Х	Х
12-hr	0.998	-0.928	0.31**	0.048	>0.10	1.73	0.13	$0.08^*$	2.4e <sup>-4**</sup>	0.321	1975	$2.59^{*}$	2.67	Х	Х	Х
24-hr	0.990	-1.716	$0.08^{*}$	0.040	>0.10	2.20	0.14	0.03**	$2.4e^{-3**}$	$0.056^{*}$	1983	$2.90^{*}$	2.58	Х	Х	Х

Table S6. Detection of trends and nonstationarity in Oshawa WPCP

Time Slice	Ljung- Box Test	Augme Dickey- Tes	Fuller	KPSS '	Test		Kendall T Test	rend	Priestley- Subbarao Test	Pettitt Test	Mann	n-Whitney Point Test	0	Mood	Change Poi	int Test
	p- value	Test statistics	p- value	Test statistics	p- value	MK <sub>Z</sub>	β	p-value	p-value	p-value	Year	Test statistics	Threshold	Year	Test statistics	Threshold
15-min	0.595	-0.237	0.56**	0.108	>0.10	-1.29	-0.42	0.198	0.156	0.141	Х	Х	Х	Х	Х	х
30-min	0.749	-0.363	0.51**	0.074	>0.10	-1.59	-0.77	0.111	0.845	0.093*	Х	Х	Х	Х	Х	Х
1-hr	0.462	-0.366	0.51**	0.083	>0.10	-1.52	-0.9	0.129	0.851	0.103	Х	Х	Х	Х	Х	Х
2-hr	0.614	-0.222	0.56**	0.127	$0.085^{*}$	-0.82	-0.74	0.414	0.529	0.281	2005	2.99*	2.63	Х	Х	Х
6-hr	0.504	-0.098	0.61**	0.128	$0.084^{*}$	-0.47	-0.45	0.656	0.256	0.300	2005	2.95*	2.63	Х	Х	Х
12-hr	0.969	-0.238	0.56**	0.065	>0.10	-1.48	-1.4	0.138	0.296	0.141	Х	Х	Х	Х	Х	Х
24-hr	0.414	-0.177	$0.58^{**}$	0.041	>0.10	-0.035	-0.01	0.972	0.976	0.940	Х	Х	Х	Х	Х	Х

Table S7. Detection of trends and nonstationarity in Windsor Airport

Time Slice	Ljung -Box Test	Augmen Dickey-F Test	uller	KPSS 7	ſest	Mann-K	endall T Test		Priestley- Subbarao Test	Pettitt T	`est		tney Change t Test	Мо	od Change	Point Test
	p- value	Test statistics	p- value	Test statistics	p-value	MKz	β	p- value	p-value	p-value	Year	Test statistics	Threshold	Year	Test statistics	Threshold
15-min	0.257	-0.502	0.46**	0.024	>0.10	0.63	0.2	0.53	0.040	-	X	Х	Х	X	Х	Х
30-min	0.094	-0.485	0.47**	0.027	>0.10	0.18	0.12	0.85	0.322	-	Х	Х	Х	Х	Х	Х
1-hr	0.371	-0.316	0.53**	0.039	>0.10	0.16	0.12	0.88	$0.094^{*}$	-	Х	Х	Х	1996	2.73*	2.6
2-hr	0.124	-0.306	0.53**	0.084	>0.10	0.05	0.03	0.96	0.333	-	Х	Х	Х	Х	Х	Х
6-hr	0.273	-0.330	0.53**	0.168	0.032**	-0.22	-0.36	0.83	$0.0009^{**}$	0.397	Х	Х	Х	Х	Х	Х
12-hr	0.886	-0.298	0.54**	0.102	>0.10	0.56	0.39	0.58	5.53e <sup>-6**</sup>	0.347	Х	Х	Х	Х	Х	Х
24-hr	0.346	-0.258	0.55**	0.131	$0.078^*$	0.68	0.75	0.50	1.06e <sup>-5**</sup>	0.514	1965	$2.62^{*}$	2.60	Х	Х	Х

Table S8. Detection of trends and nonstationarity in Kingston P. Station

Time Slice	Ljung -Box Test	Augme Dickey- Tes	Fuller	KPSS	Test	Mann-Ke	ndall Tr	end Test	Priestley- Subbarao Test	Pettitt Test	Mann	-Whitney C Point Test	U	Mood	l Change P	oint Test
	p- value	Test statistics	p- value	Test statistics	p-value	MK <sub>Z</sub>	β	p-value	p-value	p-value	Year	Test statistics	Thres hold	Year	Test statistics	Threshold
15-min	0.344	-0.662	0.41**	0.179	0.024**	-0.549	-0.23	0.583	$0.092^{*}$	0.253	2006	$2.94^{*}$	2.63	2006	3.09*	2.66
30-min	0.288	-0.598	0.43**	0.106	>0.10	-1.422	-0.64	0.155	0.019**	0.240	2005	$2.87^{*}$	2.63	Х	Х	Х
1-hr	0.783	-0.487	$0.47^{**}$	0.117	>0.10	-1.173	-0.66	0.241	0.031**	0.359	2011	3.06*	2.63	2011	$2.96^{*}$	2.66
2-hr	0.845	-0.552	0.45**	0.135	$0.070^{*}$	-1.566	-1.03	0.117	0.224	0.216	2011	3.14*	2.63	2011	3.15*	2.66
6-hr	0.700	-0.418	0.49**	0.071	>0.10	-1.893	-1.11	$0.058^{*}$	0.199	0.161	2011	3.01*	2.63	2011	$2.80^{*}$	2.66
12-hr	0.587	-0.347	0.52**	0.090	>0.10	-2.142	-1.47	0.032**	0.755	0.093*	2011	$2.98^{*}$	2.63	Х	Х	Х
24-hr	0.733	-0.414	$0.50^{**}$	0.223	$0.010^{**}$	-2.297	-2.45	0.022**	0.909	0.024**	2005	3.46*	2.63	Х	Х	Х

Table S9. Detection of trends and nonstationarity in London International Airport

Table S10. Detection of trends and nonstationarity in Trenton Airport

Time Slice	Ljung Augmented KPSS Test -Box Dickey-Fuller Test Test		est	Mann-Ken	-Kendall Trend Test		Priestley- Subbarao Test	Pettitt Test	Mann-Whitney Change Point Test			Mood Change Point Test				
	p- value	Test statistics	p- value	Test statistics	p-value	MKz	β	p-value	p-value	p-value	Year	Test statistics	Threshold	Year	Test statistics	Threshold
15-min	0.263	-0.398	$0.50^{**}$	0.051	>0.10	0.708	0.16	0.479	2.65e <sup>-6**</sup>	0.893	Х	Х	Х	1979	3.66*	2.66
30-min	0.161	-0.325	0.53**	0.034	>0.10	1.732	0.68	0.083*	0.0033**	0.264	Х	Х	Х	1978	3.16*	2.66
1-hr	0.373	-0.328	0.53**	0.061	>0.10	1.776	0.87	$0.076^{*}$	0.0013**	$0.098^{*}$	Х	Х	Х	Х	Х	Х
2-hr	0.423	-0.341	0.52**	0.063	>0.10	2.313	1.27	0.021**	5.1e <sup>-5**</sup>	$0.053^{*}$	1994	$2.81^{*}$	2.63	Х	Х	Х
6-hr	0.638	-0.244	0.56**	0.078	>0.10	2.031	1.12	0.042**	0.005**	$0.092^{*}$	1994	$2.66^{*}$	2.63	Х	Х	Х
12-hr	0.295	-0.105	0.61**	0.204	0.014**	2.009	1.64	0.045**	0.044**	0.022**	1996	3.25*	2.63	Х	Х	Х
24-hr	0.321	-0.131	0.60**	0.238	0.010**	2.031	1.82	0.042**	0.39	0.014**	1994	3.37*	2.63	Х	Х	Х

Time Slice			-Fuller	KPSS '	Test	Mann-F	Kendall T Test	rend	Priestley- Subbarao Test	Pettitt Test	Mai	nn-Whitney Point Te	. 0	Моо	od Change F	'oint Test
	p- value	Test statistics	p- value	Test statistics	p- value	MKz	β	p- value	p-value	p-value	Year	Test statistics	Threshold	Year	Test statistics	Threshold
15-min	0.070	-0.321	0.53**	0.068	>0.10	-0.233	-0.07	0.816	0.143	_	1994	3.37*	2.63	Х	Х	Х
30-min	0.473	-0.375	0.51**	0.039	>0.10	-0.297	-0.13	0.767	0.004**	-	Х	Х	Х	2011	3.23*	2.63
1-hr	0.857	-0.230	$0.56^{**}$	0.077	>0.10	0.417	0.26	0.677	0.013**	-	Х	Х	Х	Х	Х	Х
2-hr	0.149	-0.263	$0.55^{**}$	0.055	>0.10	0.389	0.3	0.697	0.016**	-	Х	Х	Х	1967	2.73*	2.63
6-hr	0.375	-0.134	$0.60^{**}$	0.062	>0.10	-0.459	-0.51	0.646	3.9e <sup>-4**</sup>	0.802	Х	Х	Х	Х	Х	Х
12-hr	0.336	-0.186	$0.58^{**}$	0.058	>0.10	0.82	-0.67	0.412	8.9e <sup>-5**</sup>	0.254	Х	Х	Х	Х	Х	Х
24-hr	0.789	-0.208	0.57**	0.056	>0.10	-1.442	-1.43	0.149	8.7e <sup>-4**</sup>	0.360	Х	Х	Х	Х	Х	Х

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Table S11. Detectio	on of trends and no	instationarity in	Stratford WWTP

Time Slice	Ljung- Box Test	- Augment Dickey-Fu Test	uller	KPSS Test Mann-Kendall Trend Test		Priestley- Subbarao Test	Pettitt Test	Mann-Whitney Change Point Test			Mood Change Point Test					
	p-value	Test statistics	p- value	Test statistics	p-value	MKz	β	p- value	p-value	p- value	Year	Test statistics	Threshold	Year	Test statistics	Threshold
15-min	0.955	-0.267	0.55**	0.184	0.022**	-0.99	-0.43	0.322	0.049**	0.25	Х	Х	Х	X	X	X
30-min	0.935	-0.204	0.57**	0.172	0.028**	-0.44	-0.27	0.658	0.015**	0.33	Х	Х	Х	Х	Х	Х
1-hr	0.879	-0.494	0.47**	0.068	>0.10	-1.00	-0.72	0.317	0.004**	0.57	Х	Х	Х	Х	Х	Х
2-hr	0.849	-0.540	0.45**	0.055	>0.10	-0.92	-0.69	0.358	0.002**	0.67	Х	Х	Х	Х	Х	Х
6-hr	0.967	-0.318	0.53**	0.104	>0.10	-0.26	-0.29	0.795	0.053**	0.77	Х	Х	Х	Х	Х	Х
12-hr	0.018 <sup>**</sup> (0.033 <sup>**</sup> )	-0.116	0.61**	0.035	>0.10	-0.45	-0.28	0.652	0.255	-	Х	Х	Х	Х	Х	Х
24-hr	1.5e <sup>-4**</sup> (0.011 <sup>**</sup> )	-0.218	0.57**	0.035	>0.10	-1.34	-1.2	0.180	0.216	0.53	Х	Х	х	Х	Х	Х

Table S12. Detection	of trends and nons	stationarity in	Fergus Shand Dam
10010 81212 0000000	01 1100 1100 110110	,	1 01 800 0110110 2 0111

<sup>1</sup>Values within first Brackets indicate p-values of Ljung-Box Test after performing two-successive TFPWs.

# SI 3 GEV Fitting: Methods and Results

# SI 3.1 Estimation of GEV Parameters

GEV parameters are estimated using Bayesian Inference. For this, a Bayesian analysis is performed by imposing a prior distribution on the parameters. We estimated parameters using Bayesian Inference (BI) coupled with Differential Evaluation Markov Chain (DE-MC) simulation as in (Cheng and AghaKouchak, 2014; Cheng et al., 2014). This approach combines knowledge from a prior distribution and the observation vector  $\boldsymbol{y} = \{\boldsymbol{y}_t\}_{t=1:N}$  (*i.e.*, annual maxima rainfall, where *N* denotes the number of annual maxima in the observation vector  $\boldsymbol{Y}$  ) into the posterior distribution of parameters  $\boldsymbol{\omega} = \{\mu, \sigma, \zeta\}$  and  $\boldsymbol{\lambda} = \{\mu_1, \mu_0, \sigma_1, \sigma_0, \zeta\}$  assuming stationary and nonstationary conditions respectively. The priors for the location and scale parameters are noninformative normal distributions, whereas prior for the shape parameter is a normal distribution with a standard deviation of 0.3 (Renard et al., 2013) as used in the default option in the NEVA package. The Bayes theorem for estimation of GEV parameters under stationarity assumption can be expressed as (Cheng et al., 2014; Renard et al., 2013)

$$p(\boldsymbol{\omega}|\boldsymbol{y}) \propto p(\boldsymbol{y}|\boldsymbol{\omega})p(\boldsymbol{\omega}) = \prod_{t=1}^{N} p(\boldsymbol{y}|\boldsymbol{\omega})p(\boldsymbol{\omega})$$
(3.1)

Under the assumption of nonstationarity, the equation (3.1) is given as (Cheng et al., 2014; Renard et al., 2013),

$$p(\boldsymbol{\lambda}|\boldsymbol{y},\boldsymbol{x}) \propto p(\boldsymbol{y}|\boldsymbol{\lambda},\boldsymbol{x})p(\boldsymbol{\lambda}|\boldsymbol{x})$$
(3.2)

$$p(\mathbf{y}|\boldsymbol{\lambda}, \mathbf{x}) = \prod_{t=1}^{N} p(\mathbf{y}_t | \boldsymbol{\lambda}, \mathbf{x}(t)) = \prod_{t=1}^{N} p(\mathbf{y}_t | \boldsymbol{\mu}(t), \sigma(t), \boldsymbol{\zeta})$$
(3.3)

Where,  $\mathbf{x}(t)$  denote covariates under nonstationarity. The  $p(\boldsymbol{\omega}|\mathbf{y})$  and  $p(\boldsymbol{\lambda}|\mathbf{y},\mathbf{x})$  in Eqns. 3.1 and 3.2 indicate resulting posterior distributions whereas  $p(\mathbf{y}|\boldsymbol{\omega})$  and  $p(\mathbf{y}_t|\boldsymbol{\lambda},\mathbf{x}(t))$  denote likelihood functions. Since the posterior distributions of model parameters are, in general, analytically intractable, the DE-MC is integrated with BI to generate a large number of realizations (*Cheng et al.*, 2014). DE-MC is an adaptive Monte Carlo Markov Chain (MCMC) algorithm (Ter Braak and Vrugt, 2008; Ter Braak, 2006), in which multiple chains (here, we fix chain length 'n' as 5) are run in parallel. The resulting MC simulations are then run to an equilibrium. It is a standard practice to discard the initial iterations (often referred to as the *burn-in* period) of simulated samples since they are strongly influenced by starting values and do not provide usable information of the target distribution. Here we run DE-MC simulations for 3000 iterations and kept the 2001-3000<sup>th</sup> iterations of each chain. The convergence of MC simulation is checked by the "potential scale reduction

factor  $(\widehat{R})$ " as in (Gelman et al., 2011), which suggests the value of  $\widehat{R}$  should remain below the threshold value of 1.1. The post burn-in random draws from posterior distribution are then used to construct predictive distributions. For annual maxima time series of each duration, the mean and associated 95% credibility interval of parameters ( $\mu(t), \sigma(t)$ ) are derived by computing 50<sup>th</sup> (the median), 2.5<sup>th</sup> and 97.5<sup>th</sup> (bounds) percentiles of post *burn-in* random draw (for example, 50<sup>th</sup> percentile of  $\mu(t_1), \dots, \mu(t_{100})$ ). The derived model parameters are then used to compute corresponding design rainfall quantiles at *T*-year return period. For more details of BI and parameter estimation by DE-MC simulation, interested readers are requested to refer (Gelman et al., 2014; Renard et al., 2013).

#### SI 3.2 Model Selection

## SI 3.2.1 Bayes Factor

To evaluate the fit of the stationary model (null model, M1) relative to the nonstationary model (alternative model, M2) Bayes factor is computed based on the posterior distributions of sampled parameters, which is given as (Cheng et al., 2014)

$$\gamma = \frac{\Pr(\boldsymbol{X} \mid \boldsymbol{M}_{1})}{\Pr(\boldsymbol{X} \mid \boldsymbol{M}_{2})} = \frac{\int \Pr(\boldsymbol{\omega} \mid \boldsymbol{M}_{1}) \Pr(\boldsymbol{X} \mid \boldsymbol{\omega}, \boldsymbol{M}_{1}) d\boldsymbol{\omega}}{\int \Pr(\boldsymbol{\lambda} \mid \boldsymbol{M}_{2}) \Pr(\boldsymbol{X} \mid \boldsymbol{\lambda}, \boldsymbol{M}_{2}) d\boldsymbol{\lambda}}$$
(3.4)

Where X denotes input data,  $\omega$  and  $\lambda$  denote model parameters as described in the previous section. The term Pr(X | M) can be expressed using Monte Carlo integration estimation as described in (Kass and Raftery, 1995). A value of  $\gamma < 1$  indicates nonstationary model, the nonstationary model, M2 fits the data better than the stationary model, M1.

#### SI 3.2.2 Akaike Information Criterion (AIC) for Small Samples

The AIC (Anderson et al., 1994; Bozdogan, 2000) is defined as follows:

$$AIC(m) = n\log(MSE) + 2m \tag{3.5}$$

Where *n* is the number of observations, *m* denotes the number of fitted model parameters. *MSE* is the Mean Square Error of the fitted distribution against empirical distribution, which is expressed as (Dawson et al., 2007; Hu, 2007; Karmakar and Simonovic, 2007, 2007),

$$MSE = \frac{1}{n-m} \sum_{i=1}^{n} \left( O_i - F_i \right)^2$$
(3.6)

Where  $O_i$  and  $F_i$  are empirical (observed) and estimated distributions. The observed distribution ( $O_X$ ) is computed using rank-based Gringorten's plotting position formula (Yue, 2001)

$$O_X \left( X \le x_i \right) = \frac{i - 0.44}{n + 0.12} \quad \forall i = 1, 2, ..., n$$
(3.7)

Where, *i* is the rank in ascending order and  $x_i$  is the *i*<sup>th</sup> largest variate in a data series of size *n*.

The AIC for small sample sizes  $(n/m < \sim 40)$  is given by (Hurvich and Tsai, 1995),

$$AIC_{c}(m) = AIC + \frac{2m(m+1)}{n-m-1}$$
(3.8)

As sample size increases, the last term of the second-order AIC statistics ( $AIC_c$ ) approaches zero, and the AICc tends to give the same conclusion as the traditional AIC (Burnham and Anderson, 2003). Since in the present study, length of data series varies from 46 to 66 years, we used AICc instead of traditional AIC, which is also a widely used method for model selection in hydrology (Caroni and Panagoulia, 2016; Gu et al., 2017; Panagoulia et al., 2014).

Time Slice	Model	Location parameter	Scale parameter	Shape parameter	AIC <sub>c</sub>	Bayes- factor	LB (100yr)	UB (100yr)	UB/LB
15-min	GEV <sub>t</sub> -0	48.33	15.71	-0.075	-332.55	-	81.65	156.01	1.91
	GEV <sub>t</sub> -I	47.22+0.095 <i>t</i>	17.95	-0.202	-304.31	7736.97	86.91	134.98	1.55
	GEV <sub>t</sub> -II	51.03-0.074 <i>t</i>	$\exp(3.06 - 0.007t)$	-0.108	-290.55	5.44	91.48	156.69	1.71
30-min	GEV <sub>t</sub> -0	31.67	11.21	-0.21	-306.10	-	47.64	107.8	2.26
	GEV <sub>t</sub> -I	27.66+0.135 <i>t</i>	10.73	-0.098	-287.17	0.15	51.74	74.03	1.43
	GEV <sub>t</sub> -II	28.55+0.104 <i>t</i>	$\exp(2.47 - 0.005t)$	-0.155	-279.13	2.13	51.03	94.42	1.85
1-hr	GEV <sub>t</sub> -0	18.10	7.33	-0.03	-317.73	-	31.82	104.55	3.28
	GEV <sub>t</sub> -I	16.62+0.082 <i>t</i>	7.28	-0.05	-320.87	0.47	39.59	59.46	1.50
	GEV <sub>t</sub> -II	16.44+0.07 <i>t</i>	$\exp(1.97+0.002t)$	-0.002	-319.36	0.42	38.23	77.35	2.02
2-hr	GEV <sub>t</sub> -0	11.09	3.81	0.13	-333.15	-	21.21	73.71	3.47
	GEV <sub>t</sub> -I	10.04+0.05 <i>t</i>	3.72	0.095	-316.87	0.16	23.03	48.89	2.12
	GEV <sub>t</sub> -II	9.61+0.07 <i>t</i>	exp(1.41+0.0034 <i>t</i> )	0.007	-304.53	0.54	24.97	47.67	1.91
6-hr	GEV <sub>t</sub> -0	5.02	1.42	0.094	-315.85	-	9.49	22.66	2.39
	GEV <sub>t</sub> -I	4.5+0.02 <i>t</i>	1.44	0.062	-302.12	0.51	10.8	15.46	1.43
	GEV <sub>t</sub> -II	4.6+0.02 <i>t</i>	$\exp(0.52 - 0.004t)$	0.032	-291.60	0.67	10.34	15.94	1.54
12-hr	GEV <sub>t</sub> -0	2.83	0.78	0.28	-310.34	-	6.36	20.48	3.22
	GEV <sub>t</sub> -I	2.65+0.0073t	0.78	0.36	-319.6	0.46	9.3	15.85	1.70
	GEV <sub>t</sub> -II	2.68+0.0092t	exp(-0.24+0.0017 <i>t</i> )	0.29	-304.38	3.83	8.2	14.16	1.72
24-hr	GEV <sub>t</sub> -0	1.65	0.51	0.17	-318.65	-	3.3	10.1	3.06
	GEV <sub>t</sub> -I	1.51+0.0056t	0.50	0.17	-316.24	0.46	3.8	7.63	2.00
	GEV <sub>t</sub> -II	1.51+0.0072 <i>t</i>	$\exp(-0.68+0.00135t)$	0.14	-305.97	1.98	3.94	7.18	1.82

Table S13. Performance of stationary and nonstationary models for Oshawa WPCP

<sup>\*</sup>GEV<sub>t</sub>-0 is stationary model whereas GEV<sub>t</sub>-I and GEV<sub>t</sub>-II are nonstationary models with time-variant mean, and both time-variant mean and standard deviation respectively. The selected best fitted nonstationary model is marked in bold letters. Bayes factor,  $\gamma < 1$  indicates that the nonstationary model fits better than the stationary model. However, in cases  $\gamma > 1$ , to compare with stationary model, the nonstationary model is selected following minimum *AICc* criteria. LB and UB indicate lower and upper bounds of DSI at 100-year return period.

Time Slice	Model	Location parameter	Scale parameter	Shape parameter	AIC <sub>c</sub>	Bayes- factor	LB (100yr)	UB (100yr)	UB/LB
15-min	GEV <sub>t</sub> -0	44.59	12.70	-0.04	-315.08	-	76	140.88	1.85
	GEV <sub>t</sub> -I	41.36+0.13 <i>t</i>	12.83	-0.04	-311.53	1.93	85.2	118.76	1.40
	GEV <sub>t</sub> -II	40.83+0.19 <i>t</i>	exp(2.92-0.013 <i>t</i> )	-0.07	-317.65	5.19	78.8	142.36	1.81
30-min	GEV <sub>t</sub> -0	28.40	9.04	-0.05	-345.71	-	48.1	97.36	2.02
	GEV <sub>t</sub> -I	27.61+0.042 <i>t</i>	9.01	-0.04	-348.92	0.91	53.41	98.27	1.84
	GEV <sub>t</sub> -II	27.57+0.035 <i>t</i>	exp(2.11+0.0026 <i>t</i> )	-0.07	-331.17	37.31	53.12	73.41	1.38
1-hr	GEV <sub>t</sub> -0	18.35	5.87	-0.11	-318.56	-	29.45	56.19	1.91
	GEV <sub>t</sub> -I	18.4+0.008 <i>t</i>	6.02	-0.12	-326.50	3.76	31.21	61.45	1.97
	GEV <sub>t</sub> -II	16.77+0.046 <i>t</i>	exp(1.84-0.0059 <i>t</i> )	0.02	-291.35	1.84	37.8	52.93	1.40
2-hr	GEV <sub>t</sub> -0	11.32	3.16	0.06	-330.11	-	19.36	49.78	2.57
	GEV <sub>t</sub> -I	11.09+0.009 <i>t</i>	3.19	0.05	-321.46	1.27	23.74	33.6	1.41
	GEV <sub>t</sub> -II	11.12+0.0055 <i>t</i>	exp(1.10+0.0004 <i>t</i> )	0.15	-325.34	4.47	22.89	46.26	2.02
6-hr	GEV <sub>t</sub> -0	5.21	1.44	0.10	-327.18	-	10.1	23.64	2.34
	GEV <sub>t</sub> -I	5.07+0.0073 <i>t</i>	1.41	0.13	-329.47	0.23	11.17	17.79	1.59
	GEV <sub>t</sub> -II	4.88+0.0093 <i>t</i>	exp(0.38-0.00335t)	0.21	-326.79	0.77	12.91	19.57	1.51
12-hr	GEV <sub>t</sub> -0	3.13	0.83	0.11	-312.19	-	6.09	13.04	2.14
	GEV <sub>t</sub> -I	2.85+0.009t	0.78	0.14	-321.61	0.57	6.36	10.59	1.66
	GEV <sub>t</sub> -II	2.84+0.009 <i>t</i>	exp(-0.126-0.006 <i>t</i> )	0.14	-317.09	0.16	6.78	9.5	1.40
24-hr	GEV <sub>t</sub> -0	1.77	0.46	0.07	-297.12	-	3.18	6.43	2.02
	GEV <sub>t</sub> -I	1.59+0.0071 <i>t</i>	0.44	0.08	-299.78	0.54	6.36	10.59	1.66
	GEV <sub>t</sub> -II	1.64 + 0.005t	exp(-0.81-0.0006 <i>t</i> )	0.07	-296.75	0.97	3.42	5.57	1.63

Table S14. Performance of stationary and nonstationary models for Kingston Airport

Time Slice	Model	Location parameter	Scale parameter	Shape parameter	AIC <sub>c</sub>	Bayes- factor	LB (100yr)	UB (100yr)	UB/LB
15-min	GEV <sub>t</sub> -0	43.08	12.41	0.24	-485.30	-	95.12	250.55	2.63
	GEV <sub>t</sub> -I	43.96-0.05 <i>t</i>	11.87	0.19	-474.35	4.18	98.79	173.25	1.75
	GEV <sub>t</sub> -II	40.37+0.16 <i>t</i>	exp(1.65+0.04 <i>t</i> )	-0.20	-472.29	7075420	86.12	120.33	1.40
30-min	GEV <sub>t</sub> -0	26.94	8.50	0.13	-495.06	-	55.05	133.25	2.42
	GEV <sub>t</sub> -I	26.71+0.014 <i>t</i>	8.28	0.09	-477.87	13.50	55.16	111.31	2.02
	GEV <sub>t</sub> -II	22.39+0.16t	exp(2.34+0.0024)	-0.07	-418.98	77.76	56.23	96.9	1.72
1-hr	GEV <sub>t</sub> -0	16.25	5.022	0.15	-448.76	-	34.7	88.1	2.54
	GEV <sub>t</sub> -I	15.40 + 0.032t	5.44	0.17	-476.72	0.73	39.3	73.74	1.88
	GEV <sub>t</sub> -II	14.62+0.057 <i>t</i>	exp(1.31+0.010)	0.13	-463.04	0.06	37.0	81.02	2.19
2-hr	GEV <sub>t</sub> -0	10.13	3.32	0.17	-524.45	-	21.72	59.53	2.74
	GEV <sub>t</sub> -I	9.03 + 0.03t	3.38	0.09	-481.72	0.99	20.46	51.05	2.49
	GEV <sub>t</sub> -II	8.63 + 0.05t	$\exp(1.02 + 0.007t)$	0.09	-493.82	0.16	24.76	36.64	1.48
6-hr	GEV <sub>t</sub> -0	5.100	1.31	0.14	-419.26	-	10.24	22.05	2.15
	GEV <sub>t</sub> -I	4.72 + 0.0124t	1.37	0.16	-429.78	1.83	12.56	17.14	1.36
	GEV <sub>t</sub> -II	4.75 + 0.014t	$\exp(0.33 + 0.0012t)$	0.15	-415.55	1.11	12.65	17.03	1.35
12-hr	GEV <sub>t</sub> -0	3.19	0.94	0.14	-480.19	-	6.09	14.86	2.44
	GEV <sub>t</sub> -I	2.85 + 0.0114t	0.87	0.09	-491.15	0.93	6.74	10.26	1.52
	GEV <sub>t</sub> -II	2.84 + 0.0113t	exp(-0.16+0.0014 <i>t</i> )	0.15	-488.52	0.15	7.95	10.58	1.33
24-hr	GEV <sub>t</sub> -0	1.90	0.52	-0.04	-499.41	-	3.38	4.99	1.48
	GEV <sub>t</sub> -I	1.51 + 0.011t	0.50	0.02	-467.34	0.26	3.19	5.84	1.83
	GEV <sub>t</sub> -II	1.57 + 0.0096t	$\exp(-0.80 + 0.0033t)$	-0.02	-475.74	0.14	3.38	4.99	1.48

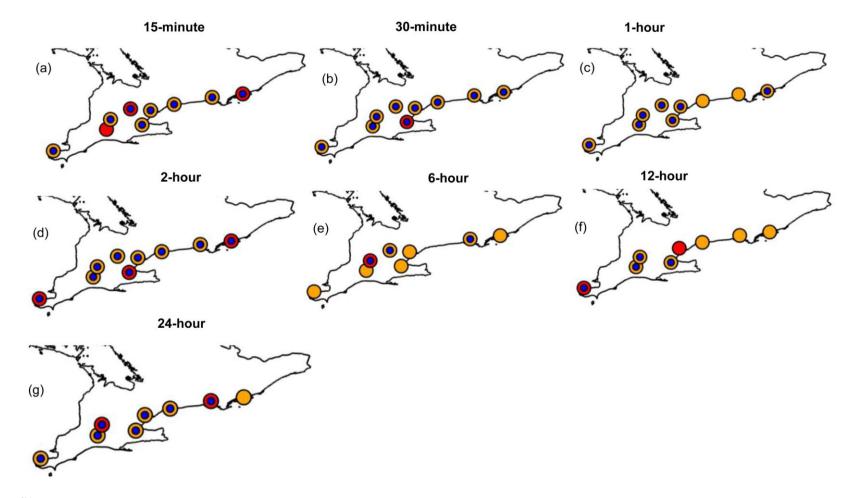
Table S15. Performance of stationary and nonstationary models for Trenton Airport

Time Slice	Model	Location parameter	Scale parameter	Shape parameter	AICc	Bayes- factor	LB (100yr)	UB (100yr)	UB/LB
15-min	GEV <sub>t</sub> -0	56.30	15.70	0.04	-423.32	-	100.59	216.41	2.15
	GEV <sub>t</sub> -I	57.31-0.05 <i>t</i>	15.06	0.18	-414.85	5.26	105.08	144.59	1.38
	GEV <sub>t</sub> -II	60.72-0.13 <i>t</i>	exp(3.04-0.009 <i>t</i> )	0.12	-384.65	54.70	134.37	184.4	1.37
30-min	GEV <sub>t</sub> -0	33.83	10.81	0.17	-413.45	-	73.35	205.5	2.80
	GEV <sub>t</sub> -I	34.76-0.023 <i>t</i>	11.16	0.28	-419.35	6.24	110.13	177.76	1.61
	GEV <sub>t</sub> -II	38.75-0.164 <i>t</i>	exp(2.97-0.015 <i>t</i> )	0.45	-314.14	68.72	311.05	163.32	1.90
1-hr	GEV <sub>t</sub> -0	19.03	6.31	0.21	-388.39	-	44.6	149.69	3.36
	GEV <sub>t</sub> -I	18.62-0.0045 <i>t</i>	6.42	0.36	-398.93	3.93	74.66	125.4	1.68
	GEV <sub>t</sub> -II	17.43+0.0552 <i>t</i>	exp(1.5+0.0125 <i>t</i> )	0.17	-372.02	2.79	49.84	84.84	1.70
2-hr	GEV <sub>t</sub> -0	11.71	4.37	0.26	-390.44	-	28.84	118.37	4.10
	GEV <sub>t</sub> -I	11.49+0.023 <i>t</i>	4.99	0.34	-371.43	3.77	33.97	158.15	4.65
	GEV <sub>t</sub> -II	11.82-0.027 <i>t</i>	exp(1.70-0.008 <i>t</i> )	0.53	-342.82	3.35	70.43	147.35	2.09
6-hr	GEV <sub>t</sub> -0	5.32	1.80	0.24	-400.01	-	13.34	38.24	2.87
	GEV <sub>t</sub> -I	5.76-0.012 <i>t</i>	1.78	0.21	-392.41	3.97	13.2	31.6	2.40
	GEV <sub>t</sub> -II	5.52-0.007 <i>t</i>	exp(0.59+0.0002 <i>t</i> )	0.28	-400.2	29.5	18.2	28.63	1.57
12-hr	GEV <sub>t</sub> -0	3.11	0.89	0.26	-365.66	-	7.45	19.5	2.62
	GEV <sub>t</sub> -I	3.38-0.01 <i>t</i>	0.89	0.34	-377.72	0.96	9.75	17.42	1.79
	GEV <sub>t</sub> -II	3.44-0.0097 <i>t</i>	$\exp(-0.11-6e^{-5}t)$	0.29	-367.39	0.25	9.88	14.77	1.50
24-hr	GEV <sub>t</sub> -0	1.68	0.45	0.26	-376.96	-	3.75	9.93	2.65
	GEV <sub>t</sub> -I	1.77-0.004 <i>t</i>	0.45	0.29	-377.32	0.71	9.75	17.42	1.79
	GEV <sub>t</sub> -II	1.82-0.005 <i>t</i>	exp(-0.80-0.0008 <i>t</i> )	0.30	-378.44	0.41	4.56	8.69	1.90

Table S16. Performance of stationary and nonstationary models for Stratford WWTP

Time Slice	Model	Location parameter	Scale parameter	Shape parameter	AIC <sub>c</sub>	Bayes- factor	LB (100yr)	UB (100yr)	UB/LB
15-min	GEV <sub>t</sub> -0	54.92	15.4	0.13	-538.02	-	116.76	224.08	1.92
	GEV <sub>t</sub> -I	61.55-0.09 <i>t</i>	20.77	0.047	-516.45	3.40	119.9	255.47	2.13
	GEV <sub>t</sub> -II	65.49-0.19t	exp(2.99-0.00064 <i>t</i> )	0.03	-529.81	1.22	117.27	230.15	1.96
30-min	GEV <sub>t</sub> -0	37.63	13.2	0.11	-469.76	-	86.68	185.36	2.14
	GEV <sub>t</sub> -I	38.27-0.024 <i>t</i>	13.6	0.11	-462.14	2.98	85.51	200.77	2.35
	GEV <sub>t</sub> -II	34.08+0.074 <i>t</i>	exp(2.12+0.0115 <i>t</i> )	0.14	-444.82	105.23	93.66	150.24	1.60
1-hr	GEV <sub>t</sub> -0	22.10	8.57	0.16	-532.24	-	52.91	137.9	2.61
	GEV <sub>t</sub> -I	25.35-0.096t	8.58	0.17	-526.26	0.12	60.42	115.43	1.91
	GEV <sub>t</sub> -II	19.54 + 0.04t	exp(1.59+0.013 <i>t</i> )	0.28	-476.74	11.4	74.7	112.48	1.50
2-hr	GEV <sub>t</sub> -0	12.54	5.26	0.12	-542.06	-	30.02	76.43	2.55
	GEV <sub>t</sub> -I	13.75-0.049t	5.02	0.23	-487.49	1.17	41.93	69.76	1.66
	GEV <sub>t</sub> -II	12.89-0.026t	exp(1.64-0.00013 <i>t</i> )	0.32	-462.93	1.95	49.89	89.83	1.80
6-hr	GEV <sub>t</sub> -0	5.34	2.31	0.055	-558.5	-	12.11	28.94	2.39
	GEV <sub>t</sub> -I	5.30-0.0026t	2.35	0.064	-537.24	1.35	14.66	21.69	1.48
	GEV <sub>t</sub> -II	5.15+0.0011 <i>t</i>	exp(0.88-0.00035 <i>t</i> )	0.046	-524.53	1.25	14.86	20.51	1.38

Table S17. Performance of stationary and nonstationary models for Fergas Shand Dam



**Figure S9**. The performance of stationary (Blue) versus nonstationary (Orange - nonstationary with time variant mean; red - nonstationary with time variant mean and standard deviation) GEV models with durations ranging between 15-minute and 24-hour (**a-g**) in nine urbanized sites. Sites with double circles indicate either better or comparable performance of stationary model relative to the nonstationary model. The shades denote the type of distribution.

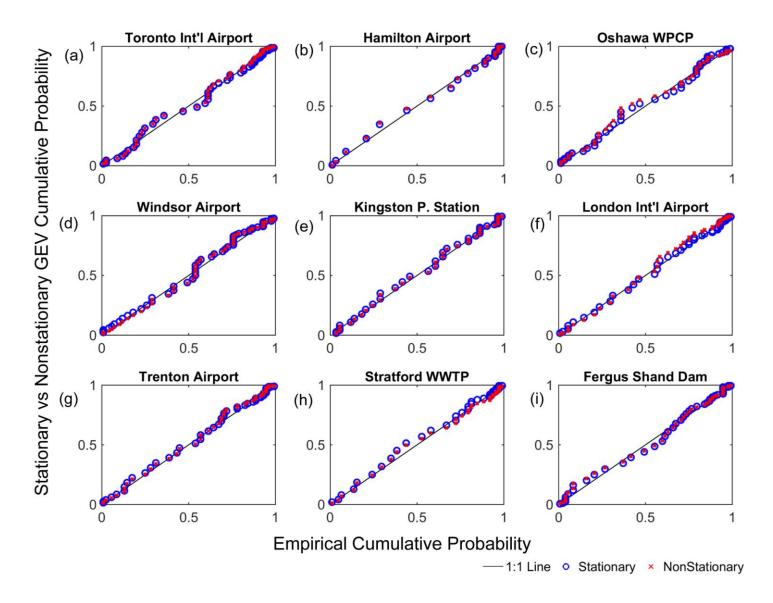


Figure S10. PP plots of nonstationary versus stationary GEV distributions for 30-min storm duration in nine sites (a - i)

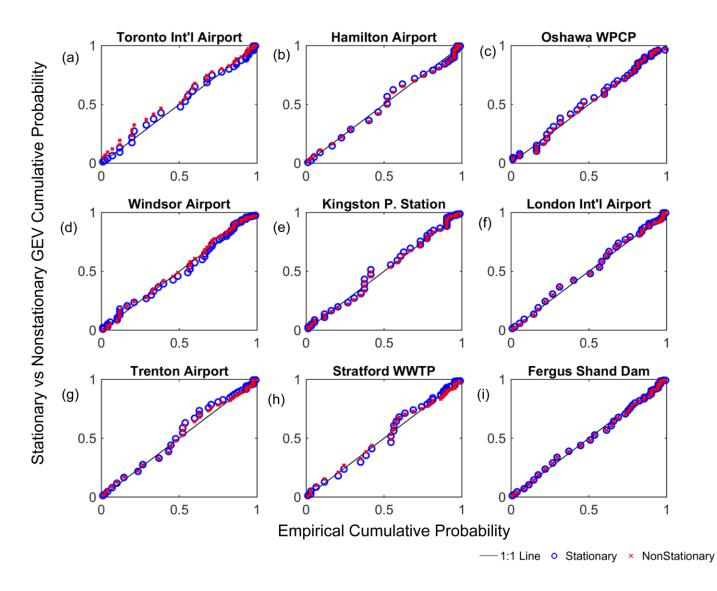


Figure S11. PP plots of nonstationary versus stationary GEV distributions for 1-hour storm duration in nine sites (a - i).

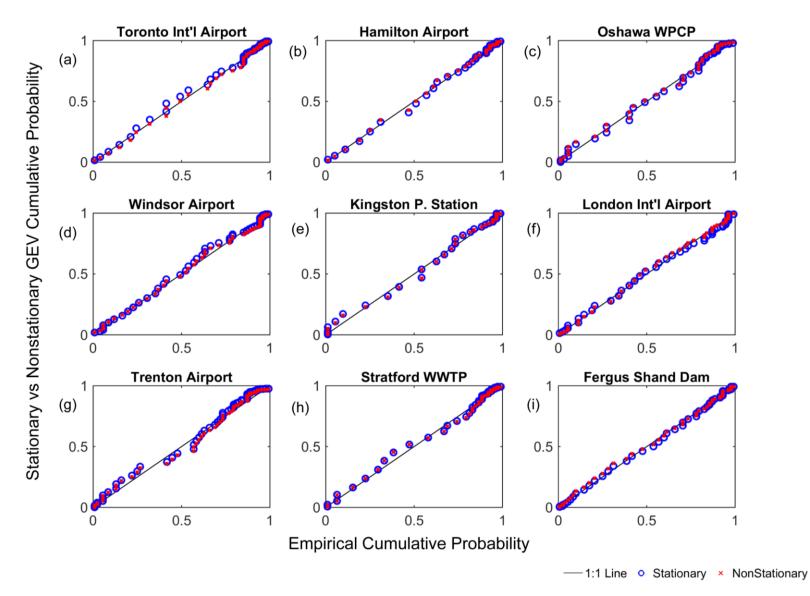


Figure S12. PP plots of nonstationary versus stationary GEV distributions for 6-hour duration in nine sites (a - i)

## **4** Estimation of Design Storm Intensity (DSI)

The DSI  $q_p$ , often referred as *return level* in the literature is the value which is expected to be exceeded on an average once in every 1/p periods, where 1-p is the specific probability associated with the quantile (Gilleland and Katz, 2014). We obtain the 1-p (*i.e.*, non-exceedance probability of occurrence) quantile of the annual maximum rainfall fitted with stationary GEV distribution using following expression (Coles and Tawn, 1996):

$$q_{p} = \mu + \frac{\sigma}{\zeta} \left[ \left\{ -\ln\left(1 - p\right) \right\}^{-\zeta} - 1 \right] \quad \forall \zeta \neq 0$$

$$(4.1)$$

Where,  $q_p$  is the DSI, associated with a  $T = \frac{1}{(1-p)}$  - year return period. The nonstationary design intensity is analogous to the standard stationary precipitation intensity with the exception of inclusion of time variant parameters (Cheng et al., 2014)

$$q_{p} = \overline{\mu} + \frac{\overline{\sigma}}{\zeta} \left[ \left\{ -\ln\left(1 - p\right) \right\}^{-\zeta} - 1 \right] \quad \forall \zeta \neq 0$$
(4.2)

Where time-variant parameters,  $\overline{\mu}$  and  $\overline{\sigma}$  are derived by computing 0.50, 0.025 and 0.975 quantiles of DE-MC sampled  $\mu(t)$  and  $\sigma(t)$  ({ $\mu(t_1), ..., \mu(t_n)$ } and { $\sigma(t_1), ..., \sigma(t_n)$ }) respectively. In Eq. 4.1, when  $\zeta \to 0$ , the GEV distribution reduces to Gumbel distribution (or Extreme Value Type I). It should be noted that Gumbel Extreme value distribution has been commonly used to estimate design storm by Environment Canada (CSA, 2010). The Gumbel probability distribution has following form (Wang et al., 2015)

$$q_p = \mu + K_p \sigma \tag{4.3}$$

Where  $K_p$  denotes frequency factor depending on the return period *T*, which is obtained using following relationship (Wang et al., 2015)

$$K_{p} = \frac{-\sqrt{6}}{\pi} \left[ 0.5772 + \ln\left(\ln\left(\frac{T}{T-1}\right)\right) \right]$$
(4.4)

Environment Canada uses this method to estimate rainfall frequency at a given duration and obtain nationwide IDF curves.

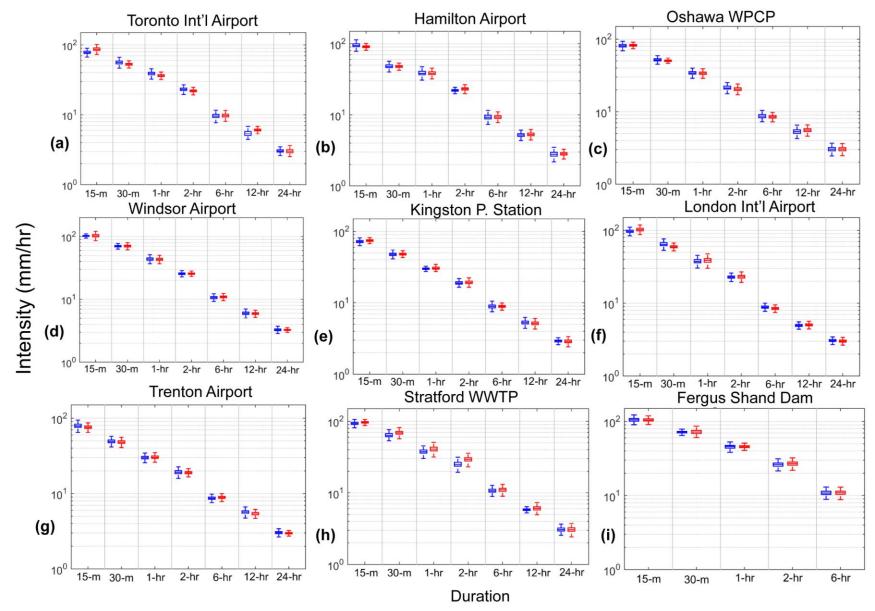


Figure S13. Uncertainty in DSI for 10-year return periods for stationary (blue) versus nonstationary (red) models The boxplots indicate 95% credibility interval in DSI estimate.

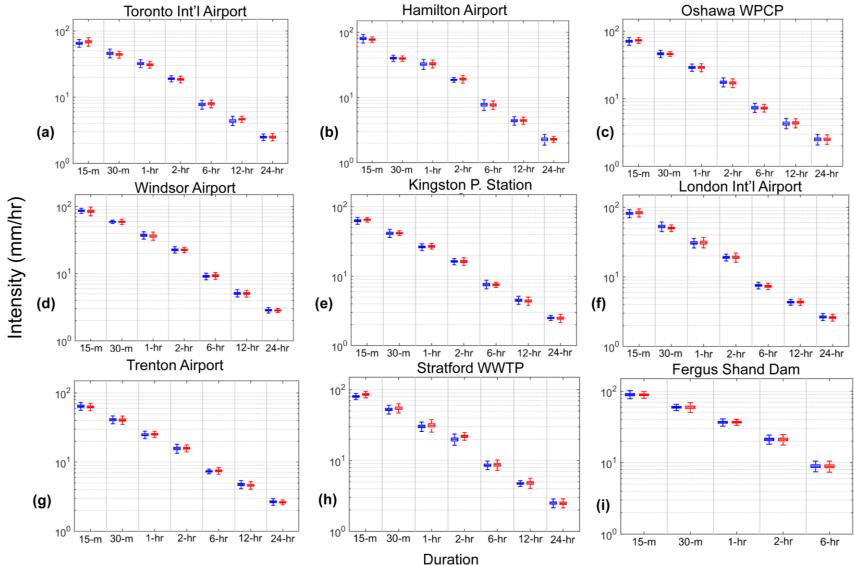


Figure S14. Same as Figure S13 but for 5-year return period.

generated DSI for Toronto International Airport for different durations								
Duration	2-year	5-year	10-year	25-year	50-year	100-year		
15-min	0.72	0.84	0.91	0.99	1.05	1.12		
	[-38.6%]	[-19.1%]	[-10.0%]	[-0.8%]	[5.1%]	[ <b>10.4</b> %]		
30-min	0.75	0.80	0.81	0.82	0.82	0.82		
	[-33.2%]	[-25.1%]	[-22.9%]	[-21.7%]	[-21.6%]	[-21.8%]		
1-hour	0.94	0.93	0.92	0.90	0.88	0.86		
	[-6.7%]	[-7.3%]	[-8.9%]	[-11.7%]	[-14.1%]	[-16.7%]		
2-hour	0.97	0.93	0.91	0.90	0.89	0.88		
	[-3.3%]	[-7.5%]	[-9.4%]	[-11.3%]	[-12.6%]	[-13.7%]		
6-hour	0.96	0.92	0.94	0.99	1.05	1.13		
	[-4.4%]	[-9.17%]	[-6.8%]	[-0.7%]	[5.2%]	[ <i>11.7</i> *%]		
12-hour	0.94	0.94	1.03	1.23	1.47	1.80		
	[-6.4%]	[-6.7%]	[2.5%]	[ <b>18.9%</b> ]	[32.2%]	[44.5%]		
24-hour	0.94	0.89	0.90	0.96	1.03	1.11		
	[-5.9%]	[-12.1%]	[-10.7%]	[-4.18%]	[2.8%]	[ <i>10.1%</i> ]		

Table S18.1 Ratio and percentage changes between updated nonstationary versus ECgenerated DSI for Toronto International Airport for different durations

\*Results within brackets indicate percentage changes between updated versus EC-generated DSI. More than 1% increase in DSI is shown in bold, whereas 10% or more is marked with bold italic letters.

Table S18.2 Ratio and percentage changes between updated stationary versus EC-generated DSI for Toronto International Airport for different durations

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	0.73	0.80	0.82	0.83	0.83	0.83
	[-37.7%]	[-25.3%]	[-22.1%]	[-20.6%]	[-20.5%]	[-25.6%]
30-min	0.76	0.83	0.86	0.89	0.91	0.93
	[-32.3%]	[-21.0%]	[-16.5%]	[-12.4%]	[-10.0%]	[-8.08%]
1-hour	0.97	0.97	0.98	1.01	1.03	1.05
	[-2.9%]	[-2.9%]	[-1.7%]	[0.6%]	[2.5%]	[ <b>4.6</b> %]
2-hour	0.98	0.96	0.97	0.99	1.02	1.05
	[-1.6%]	[-4.35%]	[-3.4%]	[-0.7%]	[1.9%]	[4.9%]
6-hour	0.93	0.89	0.91	0.98	1.05	1.13
	[-7.7%]	[-12.6%]	[-9.7%]	[-2.4%]	[4.4%]	[11.8*%]
12-hour	0.93	0.88	0.91	1.0	1.1	1.25
	[-8.0%]	[-13.5%]	[-9.8%]	[0.3%]	[ <b>9.8%</b> ]	[ <i>19.9%</i> ]
24-hour	0.94	0.90	0.91	0.98	1.06	1.15
	[-5.9%]	[-11.6%]	[-9.6%]	[-2.3%]	[5.3%]	[ <i>13.2%</i> ]

\*More than 10% increase is marked in bold italics.

generated DSI for Hamilton Allport for different durations								
Duration	2-year	5-year	10-year	25-year	50-year	100-year		
15-min	0.96	0.93	0.94	0.97	1.0	1.03		
	[-4.7%]	[-7.1%]	[-6.1%]	[-3.2%]	[-0.3%]	[3.1%]		
30-min	0.71	0.72	0.75	0.80	0.86	0.94		
	[-40.1%]	[-39.5%]	[-34.2%]	[-24.3%]	[-15.7%]	[-6.7%]		
1-hour	0.98	0.93	0.91	0.90	0.90	0.90		
	[-2.1%]	[-7.8%]	[-9.7%]	[-10.9%]	[-11.2%]	[-11.2%]		
2-hour	0.94	0.89	0.90	0.93	0.97	1.02		
	[-6.1%]	[-12.3%]	[-11.7%]	[-7.8%]	[-3.5%]	[1.5%]		
6-hour	0.90	0.85	0.87	0.93	1.0	1.09		
	[-11.6%]	[-17.7%]	[-15.2%]	[-7.8%]	[-0.3%]	[7.9%]		
12-hour	0.91	0.88	0.89	0.94	0.99	1.06		
	[-9.2%]	[-13.8%]	[-	[-6.5%]	[-0.76%]	[5.59%]		
			12.07%]					
24-hour	0.75	0.80	0.84	0.92	0.99	1.07		
	[-32.9%]	[-25.8%]	[-19.0%]	[-8.9%]	[-1.1%]	[6.5%]		

Table S19.1 Ratio and percentage changes between updated nonstationary versus ECgenerated DSI for Hamilton Airport for different durations

Table S19.2 Ratio and percentage changes between updated stationary versus EC-generated DSI for Hamilton Airport for different durations

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	0.98	0.97	0.99	1.02	1.05	1.08
	[-1.7%]	[-2.8%]	[-1.5%]	[1.6%]	[4.5%]	[7.7%]
30-min	0.72	0.72	0.75	0.79	0.83	0.61
	[-38.5%]	[-38.3%]	[-34.2%]	[-26.5%]	[-19.8%]	[-63.9%]
1-hour	0.96	0.92	0.91	0.93	0.95	0.98
	[-3.7%]	[-9.2%]	[-9.5%]	[-7.6%]	[-5.2%]	[-2.1%]
2-hour	0.94	0.87	0.85	0.85	0.86	0.87
	[-6.4%]	[-15.4%]	[-17.5%]	[-17.5%]	[-16.3%]	[-14.4%]
6-hour	0.91	0.86	0.86	0.91	0.96	1.02
	[-10.1%]	[-16.8%]	[-15.6%]	[-10.4%]	[-4.7%]	[1.7%]
12-hour	0.92	0.87	0.87	0.90	0.94	0.99
	[-8.5%]	[-14.5%]	[-14.2%]	[-10.4%]	[-6.3%]	[-1.3%]
24-hour	0.76	0.79	0.83	0.88	0.93	0.99
	[-31.3%]	[-26.3%]	[-21.1%]	[-13.3%]	[-7.2%]	[-1.2%]

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	1.09	1.08	1.06	1.01	0.97	0.94
	[7.8%]	[7.6%]	[5.3%]	[1.06%]	[-2.7%]	[-6.8%]
30-min	1.09	1.05	1.0	0.93	0.88	0.83
	[8.7%]	[4.83%]	[0.1%]	[-7.4%]	[-13.6%]	[-20.3%]
1-hour	1.05	1.07	1.07	1.06	1.05	1.04
	[4.3%]	[6.4%]	[6.5%]	[5.9%]	[5.1%]	[4.2%]
2-hour	1.0	1.02	1.04	1.07	1.10	1.14
	[0.24%]	[1.81%]	[3.7%]	[ <b>6.9</b> %]	[ <b>9.4</b> %]	[ <i>12.0</i> %]
6-hour	1.0	0.99	1.0	1.01	1.03	1.04
	[0%]	[-0.55%]	[-0.11%]	[1.3%]	[2.5%]	[4.0%]
12-hour	0.96	0.90	0.93	1.03	1.15	1.30
	[-4.2%]	[-11.6%]	[-7.56%]	[3.04%]	[ <i>12.8%</i> ]	[23.0%]
24-hour	0.99	0.95	0.96	0.99	1.03	1.08
	[-1.1%]	[-5.6%]	[-4.6%]	[-1.05%]	[2.9%]	[7.3%]

Table S20.1 Ratio and percentage changes between updated nonstationary versus ECgenerated DSI for Oshawa WPCP for different durations

Table S20.2 Ratio and percentage changes between updated stationary versus EC-generated DSI for Oshawa WPCP for different durations

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	1.05	1.05	1.04	1.03	1.01	0.99
	[4.9%]	<b>[4.9%</b> ]	[4.1%]	[2.5%]	[1.0%]	[-0.6%]
30-min	1.07	1.06	1.03	0.99	0.95	0.91
	[6.3%]	[5.6%]	[3.0%]	[-1.5%]	[-5.5%]	[-9.9%]
1-hour	1.03	1.06	1.07	1.08	1.08	1.08
	[2.6%]	[5.9%]	[6.9%]	[7.4%]	[7.5%]	[7.3%]
2-hour	1.0	1.04	1.07	1.13	1.18	1.23
	[0.4%]	[3.5%]	[6.7%]	[ <i>11.4%</i> ]	[15.1%]	[ <b>18.9</b> %]
6-hour	1.01	1.01	1.02	1.04	1.06	1.09
	[0.9%]	[0.5%]	[1.5%]	[3.7%]	[5.9%]	[8.1%]
12-hour	0.96	0.88	0.88	0.93	1.0	1.08
	[-3.8%]	[-14.2%]	[-13.3%]	[-7.0%]	[0%]	[7.8%]
24-hour	0.98	0.95	0.96	0.99	1.03	1.07
	[-1.6%]	[-5.5%]	[-4.6%]	[-1.0%]	[2.7%]	[6.9%]

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	0.94	0.97	1.02	1.11	1.20	1.31
	[-6.1%]	[-3.3%]	[1.6%]	[9.8%]	[ <i>16.5</i> %]	[ <b>23.4</b> %]
30-min	0.99	1.00	1.03	1.07	1.11	1.15
	[-1.5%]	[0.5%]	[2.9%]	[6.8%]	[ <b>9.9</b> %]	[ <i>13.2</i> %]
1-hour	0.98	0.98	1.00	1.04	1.08	1.12
	[-1.7%]	[-1.7%]	[0.21%]	[3.9%]	[7.4%]	[ <i>10.9%</i> ]
2-hour	1.06	1.06	1.04	1.00	0.98	0.95
	[5.8%]	[5.3%]	[3.5%]	[0.27%]	[-2.5%]	[-5.5%]
6-hour	1.04	1.06	1.08	1.10	1.11	1.13
	[3.7%]	[5.9%]	[7.2%]	[8.9%]	[ <i>10.3%</i> ]	[ <i>11.6%</i> ]
12-hour	1.01	1.01	1.03	1.05	1.08	1.11
	[0.5%]	[1.2%]	[2.7%]	[5.2%]	[ <b>7.4</b> %]	[ <b>9.8</b> %]
24-hour	1.00	1.00	1.01	1.02	1.03	1.03
	[-0.45%]	[0%]	[0.9%]	[1.8%]	[2.6%]	[3.2%]

Table S21.1 Ratio and percentage changes between updated nonstationary versus ECgenerated DSI for Windsor Airport for different durations

Table S21.2 Ratio and percentage changes between updated stationary versus EC-generated DSI for Windsor Airport for different durations

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	0.97	0.98	1.00	1.04	1.08	1.12
	[-3.0%]	[-1.94%]	[0.32%]	[4.2%]	[7.5%]	[11.1%]
30-min	0.98	1.01	1.03	1.05	1.07	1.09
	[-1.56%]	[0.79%]	[2.6%]	[4.9%]	[6.7%]	[8.5%]
1-hour	1.01	1.01	1.02	1.03	1.04	1.05
	[1.04%]	[0.99%]	[1.5%]	[2.7%]	[3.7%]	[4.8%]
2-hour	1.07	1.06	1.03	1.0	0.97	0.94
	[6.9%]	[5.5%]	[3.3%]	[-0.3%]	[-3.4%]	[-6.8%]
6-hour	1.03	1.04	1.05	1.07	1.08	1.09
	[2.4%]	[3.7%]	[4.7%]	[6.1%]	[7.2%]	[8.4%]
12-hour	1.00	1.01	1.04	1.07	1.10	1.14
	[-0.26%]	[1.4%]	[3.5%]	[6.8%]	[9.5%]	[ <i>12.3%</i> ]
24-hour	1.00	1.01	1.01	1.02	1.03	1.03
	[0.45%]	[0.7%]	[1.2%]	[2.1%]	[2.6%]	[3.2%]

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	1.00	1.00	1.00	0.99	0.98	0.96
	[-0.2%]	[0.5%]	[-0.03%]	[-1.3%]	[-2.5%]	[-3.9%]
30-min	0.98	0.98	0.97	0.95	0.94	0.93
	[-1.8%]	[-2.5%]	[-3.4%]	[-4.78%]	[-5.93%]	[-7.13%]
1-hour	1.00	0.97	0.95	0.91	0.88	0.86
	[0.1%]	[-2.8%]	[-5.68%]	[-9.8%]	[-13.3%]	[-16.8%]
2-hour	0.96	0.95	0.97	1.01	1.05	1.10
	[-4.5%]	[-4.9%]	[-2.84%]	[1.18%]	[4.9%]	[8.82%]
6-hour	0.99	0.98	0.99	1.03	1.06	1.09
	[-1.04%]	[-1.98%]	[-0.56%]	[2.5%]	[5.4%]	[8.6%]
12-hour	0.98	0.96	0.97	1.00	1.03	1.07
	[-2.08%]	[-4.1%]	[-3.1%]	[-0.3%]	[2.8%]	[6.1%]
24-hour	0.98	0.98	0.99	1.01	1.03	1.05
	[-1.5%]	[-1.6%]	[-0.7%]	[1.2%]	[3.1%]	[4.9%]

Table S22.1 Ratio and percentage changes between updated nonstationary versus ECgenerated DSI for Kingston P. Station for different durations

Table S22.2 Ratio and percentage changes between updated stationary versus EC-generated DSI for Kingston P. Station for different durations

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	0.97	0.97	0.97	0.96	0.95	0.95
	[-2.8%]	[-2.7%]	[-3.1%]	[-4.0%]	[-4.8%]	[-5.7%]
30-min	0.98	0.97	0.96	0.95	0.93	0.92
	[-2.5%]	[-3.2%]	[-4.1%]	[-5.7%]	[-7.1%]	[-8.5%]
1-hour	0.99	0.96	0.93	0.90	0.87	0.85
	[-1.5%]	[-4.5%]	[-7.3%]	[-11.4%]	[-14.7%]	[-18.1%]
2-hour	0.97	0.95	0.95	0.96	0.97	0.98
	[-3.3%]	[-5.1%]	[-4.9%]	[-4.1%]	[-3.0%]	[-1.8%]
6-hour	0.99	0.98	0.99	1.01	1.03	1.06
	[-1.2%]	[-2.2%]	[-1.4%]	[0.8%]	[2.9%]	[5.3%]
12-hour	1.0	0.98	0.99	1.01	1.04	1.07
	[0.3%]	[-1.5%]	[-0.8%]	[1.4%]	[3.9%]	[6.5%]
24-hour	0.99	1.0	1.01	1.02	1.04	1.06
	[-0.5%]	[-0.4%]	[0.7%]	[2.3%]	[3.9%]	[5.6%]

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	0.92	0.96	1.0	1.08	1.1	1.21
	[-9.2%]	[-4.3%]	[0.45%]	[7.1%]	[ <i>12.3%</i> ]	[17.4%]
30-min	0.92	0.89	0.90	0.92	0.94	0.97
	[-9.3%]	[-12.3%]	[-11.7%]	[-9.2%]	[-6.4%]	[-3.3%]
1-hour	0.88	0.88	0.91	0.98	1.05	1.12
	[-13.3%]	[-13.3%]	[-9.3%]	[-1.9%]	[4.3%]	[ <i>10.8%</i> ]
2-hour	0.92	0.93	0.95	0.98	1.0	1.03
	[-8.9%]	[-7.8%]	[-5.8%]	[-2.5%]	[0.12%]	[2.9%]
6-hour	0.93	0.92	0.92	0.92	0.93	0.94
	[-7.2%]	[-9.0%]	[-9.1%]	[-8.4%]	[-7.5%]	[-6.3%]
12-hour	0.95	0.97	0.98	1.01	1.03	1.05
	[-5.6%]	[-3.4%]	[-1.8%]	[0.5%]	[2.5%]	[4.3%]
24-hour	0.92	0.94	0.94	0.94	0.94	0.93
	[-9.3%]	[-6.2%]	[-5.9%]	[-5.9%]	[-6.7%]	[-7.6%]

Table S23.1 Ratio and percentage changes between updated nonstationary versus ECgenerated DSI for London International Airport for different durations

Table S23.2 Ratio and percentage changes between updated stationary versus EC-generated DSI for London International Airport for different durations

Duration	2-year	5-year	10-year	25-year	50-year	100-year
	2	· ·	•	•	•	•
15-min	0.92	0.94	0.95	0.97	0.98	1.0
	[-8.9%]	[-6.8%]	[-5.2%]	[-3.2%]	[-1.7%]	[-0.1%]
30-min	0.93	0.94	0.97	1.02	1.07	1.13
	[-7.6%]	[-6.2%]	[-3.1%]	[2.2%]	[6.6%]	[11.2%]
1-hour	0.88	0.87	0.89	0.92	0.95	0.99
	[-13.1%]	[-14.8%]	[-12.9%]	[-8.9%]	[-5.1%]	[-1.05%]
2-hour	0.92	0.92	0.93	0.94	0.95	0.97
	[-8.4%]	[-8.3%]	[-7.5%]	[-5.9%]	[-4.8%]	[-3.4%]
6-hour	0.94	0.94	0.96	0.98	1.0	1.02
	[-6.4%]	[-5.8%]	[-4.4%]	[-2.1%]	[0.08%]	[2.3%]
12-hour	0.95	0.96	0.96	0.96	0.96	0.96
	[-5.3%]	[-4.6%]	[-4.3%]	[-4.1%]	[-3.8%]	[-3.8%]
24-hour	0.92	0.96	0.96	0.97	0.96	0.96
	[-8.7%]	[-4.5%]	[-3.9%]	[-3.3%]	[-3.8%]	[-4.4%]

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	0.99	0.99	1.01	1.07	1.13	1.19
	[-0.67%]	[-1.11%]	[1.45%]	[6.56%]	[ <i>11.13</i> %]	[ <i>16.0</i> %]
30-min	0.99	0.99	1.01	1.04	1.07	1.10
	[-1.32%]	[-0.54%]	[1.11%]	[3.9%]	[6.3%]	[ <b>8.88</b> %]
1-hour	0.97	0.94	0.96	1.0	1.04	1.09
	[-3.2%]	[-5.93%]	[-4.23%]	[0%]	[4.0%]	[8.5%]
2-hour	0.99	0.95	0.95	0.96	0.97	0.99
	[-1.5%]	[-5.29%]	[-5.54%]	[-4.3%]	[-2.8%]	[-0.9%]
6-hour	0.99	1.00	1.03	1.08	1.12	1.18
	[-0.53%]	[0.13%]	[2.6%]	[7.1%]	[11.1%]	[ <b>15.3</b> %]
12-hour	1.00	1.02	1.03	1.06	1.09	1.12
	[0%]	[1.5%]	[3.3%]	[6.04%]	[8.5%]	[ <i>10.9</i> %]
24-hour	1.02	1.03	1.03	1.03	1.03	1.03
	[1.93%]	[3.05%]	[3.02%]	[2.9%]	[2.9%]	[2.5%]

Table S24.1 Ratio and percentage changes between updated nonstationary versus ECgenerated DSI for Trenton Airport for different durations

Table S24.2 Ratio and percentage changes between updated stationary versus EC-generated DSI for Trenton Airport for different durations

	•	_	10			100
Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	1.01	1.03	1.07	1.16	1.25	1.35
	[1.38%]	[2.78%]	[6.8%]	[ <i>13.9%</i> ]	[ <i>19.9%</i> ]	[ <b>26.06</b> %]
30-min	0.98	1.01	1.04	1.09	1.13	1.18
	[-1.63%]	[0.8%]	[3.7%]	[8.1%]	[ <i>11.7%</i> ]	[15.4%]
1-hour	0.95	0.91	0.91	0.94	0.97	1.01
	[-4.8%]	[-9.8%]	[-9.4%]	[-6.4%]	[-3.1%]	[0.7%]
2-hour	0.96	0.94	0.96	1.0	1.05	1.10
	[-3.7%]	[-5.95%]	[-4.1%]	[0.45%]	[4.6%]	[9.1%]
6-hour	0.98	0.98	0.99	1.03	1.06	1.11
	[-1.97%]	[-2.3%]	[-0.82%]	[2.69%]	[6.0%]	[9.5%]
12-hour	1.0	1.05	1.09	1.15	1.21	1.27
	[-0.3%]	[4.41%]	[8.1%]	[ <i>13.04%</i> ]	[17.1%]	[21.1%]
24-hour	1.03	1.05	1.05	1.05	1.04	1.04
	[2.87%]	[4.51%]	[4.6%]	[4.3%]	[4.2%]	[3.6%]

<u>Sellerated I</u>			or annorone e	uluions		
Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	1.05	1.08	1.06	1.02	0.99	0.96
	[5.03%]	[7.02%]	[5.6%]	[2.4%]	[-0.76%]	[-4.35%]
30-min	0.96	1.00	1.07	1.19	1.31	1.45
	[-3.99%]	[0.33%]	[6.6%]	[16.2%]	[23.72%]	[ <b>31.2</b> %]
1-hour	0.90	0.94	1.03	1.19	1.36	1.57
	[-10.9%]	[-6.1%]	[2.6%]	[16.2%]	[ <b>26.5</b> %]	[ <b>36.4</b> %]
2-hour	0.97	0.98	1.06	1.21	1.37	1.56
	[-3.3%]	[-1.9%]	[5.3%]	[17.4%]	[26.8%]	[36.04%]
6-hour	0.89	0.84	0.86	0.93	1.01	1.11
	[-12.3%]	[-19.4%]	[-16.1%]	[-7.2%]	[ <b>1.09</b> %]	[ <b>9.8%</b> ]
12-hour	0.90	0.83	0.84	0.90	0.97	1.06
	[-11.5%]	[-20.7%]	[-18.9%]	[-	[-2.9%]	[5.9%]
				11.04%]		
24-hour	0.84	0.79	0.80	0.87	0.94	1.03
	[-19.02%]	[-27.2%]	[-24.3%]	[-15.6%]	[-6.8%]	[2.6%]

Table S25.1 Ratio and percentage changes between updated nonstationary versus ECgenerated DSI for Stratford WWTP for different durations

Table S25.2 Ratio and percentage changes between updated stationary versus EC-generated DSI for Stratford WWTP for different durations

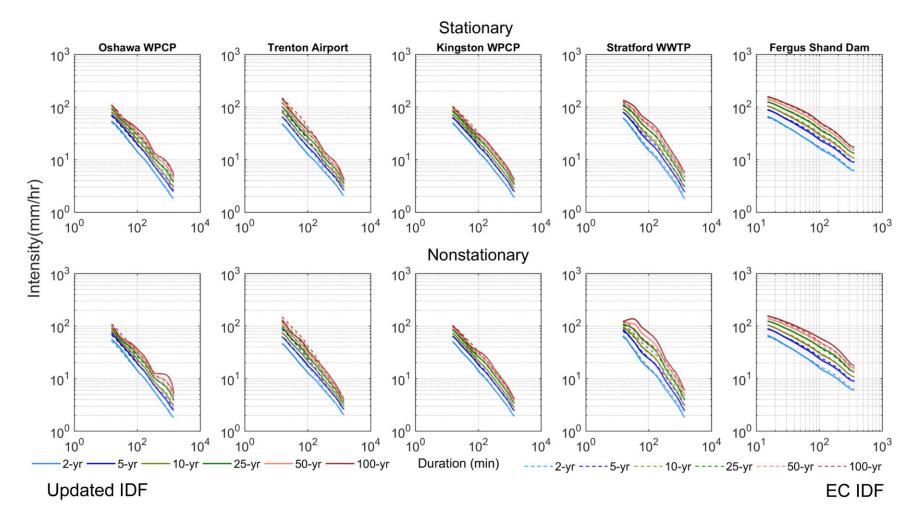
Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	1.0	1.01	1.03	1.04	1.05	1.07
	[-0.1%]	[1.4%]	[2.47%]	[3.97%]	[5.1%]	[6.3%]
30-min	0.95	0.96	0.99	1.04	1.09	1.15
	[-5.25%]	[-4.5%]	[-1.45%]	[3.89%]	[8.5%]	[ <i>13.2%</i> ]
1-hour	0.92	0.91	0.94	1.0	1.06	1.14
	[-8.7%]	[-10.03%]	[-6.7%]	[-0.06%]	[5.8%]	[ <i>12.05</i> %]
2-hour	0.92	0.88	0.91	0.98	1.05	1.15
	[-8.7%]	[-13.6%]	[-10.2%]	[-2.18%]	[5.1%]	[ <i>12.7</i> %]
6-hour	0.89	0.82	0.84	0.88	0.94	1.01
	[-12.3%]	[-21.3%]	[-19.7%]	[-13.1%]	[-6.45%]	[0.8%]
12-hour	0.89	0.81	0.82	0.86	0.92	0.99
	[-12.4%]	[-22.7%]	[-21.9%]	[-15.7%]	[-8.86%]	[-1.3%]
24-hour	0.84	0.79	0.80	0.84	0.90	0.97
	[-19.02%]	[-27.2%]	[-25.5%]	[-18.5%]	[-11.4%]	[-3.1%]

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	1.05	1.02	1.01	1.01	1.01	1.02
	[4.5%]	[1.8%]	[1.21%]	[1.1%]	[1.3%]	[1.75%]
30-min	1.02	0.98	0.98	1.0	1.02	1.05
	[2.1%]	[-2.05%]	[-1.89%]	[0.06%]	[2.3%]	[ <b>4.8</b> %]
1-hour	0.99	0.94	0.95	0.99	1.03	1.08
	[-0.8%]	[-6.5%]	[-5.4%]	[-1.4%]	[2.8%]	[7.4%]
2-hour	0.91	0.92	0.96	1.05	1.13	1.23
	[-10.4%]	[-9.0%]	[-3.9%]	[4.7%]	[ <i>11.6%</i> ]	[18.7%]
6-hour	0.94	0.97	0.99	1.02	1.05	1.07
	[-6.2%]	[-3.0%]	[-0.7%]	[2.2%]	[4.3%]	<b>[6.6</b> %]

Table S26.1 Ratio and percentage changes between updated nonstationary versus ECgenerated DSI for Fergus Shand dam for different durations

Table S26.2 Ratio and percentage changes between updated stationary versus EC-generated DSI for Fergus Shand dam for different durations

Duration	2-year	5-year	10-year	25-year	50-year	100-year
15-min	1.05	1.02	1.02	1.02	1.02	1.03
	[4.5%]	[2.2%]	[1.73%]	[1.86%]	[2.27%]	[2.86%]
30-min	1.03	0.97	0.97	0.98	1.00	1.03
	[2.4%]	[-2.74%]	[-3.1%]	[-1.60%]	[0.36%]	[3.76%]
1-hour	0.99	0.93	0.94	0.97	1.01	1.05
	[-1.03%]	[-7.1%]	[-6.48%]	[-3.02%]	[0.67%]	[4.86%]
2-hour	0.94	0.92	0.94	0.97	1.0	1.03
	[-6.3%]	[-8.44%]	[-6.95%]	[-3.47%]	[-0.31%]	[3.19%]
6-hour	0.96	0.97	0.99	1.01	1.03	1.05
	[-4.36%]	[-2.7%]	[-1.1%]	[1.12%]	[ <b>2.79</b> %]	[4.53%]



**Figure S15.** Estimated nonstationary versus EC-generated IDFs for return periods T = 2, 5, 10, 25, 50 and 100-year for the urbanized and moderately locations in Southern Ontario. The updated and EC IDFs are shown using solid and dotted lines respectively.

## SI 5 Statistical Significance of Nonstationary versus Stationary DSI

The (statistically) significant differences in DSI is computed using the statistical test for the difference between two means or the standardized z-statistics, which is given by (Madsen et al., 2009; Mikkelsen et al., 2005)

$$z = \frac{\hat{z}_T^{NonSta} - \hat{z}_T^{Sta}}{\sqrt{0.5(var\{\hat{z}_T^{NonSta}\} + var\{\hat{z}_T^{Sta}\})}}$$
(5.1)

Where  $\hat{z}_T^{NonSta}$  is the *T*-year DSI obtained from the best selected nonstationary model,  $\hat{z}_T^{Sta}$  describes the same but with the best stationary model. The denominator indicates predictive uncertainty;  $var{\hat{z}_T^{NonSta}}$  and  $var{\hat{z}_T^{Sta}}$  are the estimated variance obtained from the *T*-year event estimates and corresponding 95% credible interval. The z-statistic can be interpreted as statistically equivalent to quantiles of standard normal distribution, *i.e.*,  $z = \pm 1.64$  correspond to 10% significance levels. The null hypothesis of the test assumes the *T*-year event estimate obtained using the best fitted nonstationary model is significantly different from its best fitted stationary counterpart.

				<u> </u>					
Duration	Toronto	Hamilton	Oshawa	Windsor	Kingston	London	Trenton	Stratford	Fergus Shand
15-min	-0.038	-0.362	0.251	-0.354	0.297	-0.032	-0.265	0.521	0.000
30-min	-0.050	-0.126	0.244	0.011	0.068	-0.158	0.030	0.118	-0.037
1-hour	-0.331	0.151	0.127	-0.288	0.158	-0.009	0.161	-0.168	0.016
2-hour	-0.170	0.041	-0.012	-0.153	-0.128	-0.041	0.246	0.371	-0.324
6-hour	0.389	-0.147	0.195	0.151	0.021	-0.088	0.183	0.000	-0.154
12-hour	0.214	-0.073	-0.031	0.088	-0.266	-0.038	0.032	-0.032	-
24-hour	0.000	-0.108	0.044	-0.116	-0.116	-0.049	-0.126	0.000	-

Table S27. Z-statistics\* between best selected nonstationary and stationary model for 2-year return period

\*The standardized Z-statistic is positive (negative) with an increasing (decreasing) trend, and statistically significant at 10% significance level when  $|z| > \pm 1.64$ .

Table S28. Z-statistics between best selected nonstationary and stationary model for 10-year return period

Duration	Toronto	Hamilton	Oshawa	Windsor	Kingston	London	Trenton	Stratford	Fergus Shand
15-min	0.373	-0.227	0.061	0.065	0.171	0.324	-0.281	0.196	-0.029
30-min	-0.201	0.001	-0.147	0.016	0.038	-0.295	-0.120	0.373	0.050
1-hour	-0.346	-0.007	-0.018	-0.068	0.075	0.151	0.224	0.348	0.046
2-hour	-0.324	0.309	-0.105	0.014	0.091	0.081	-0.070	0.397	0.129
6-hour	0.103	0.014	0.074	0.174	0.041	-0.277	0.212	0.140	0.017
12-hour	0.526	0.089	0.213	-0.043	-0.123	0.156	-0.264	0.201	-
24-hour	-0.039	0.061	0.000	-0.016	-0.071	-0.107	-0.104	0.047	-

Tuble 527.2 Sudstates between best beleeted nonsudohary and sudohary model for 56 year retain period									
Duration	Toronto	Hamilton	Oshawa	Windsor	Kingston	London	Trenton	Stratford	Fergus Shand
15-min	0.569	-0.144	-0.137	0.287	0.081	0.636	-0.287	-0.214	-0.032
30-min	-0.244	0.080	-0.230	0.077	0.035	-0.234	-0.160	0.499	0.050
1-hour	-0.497	-0.153	-0.054	0.120	0.039	0.273	0.195	0.564	0.059
2-hour	-0.498	0.465	-0.126	0.045	0.207	0.162	-0.205	0.349	0.372
6-hour	0.016	0.107	-0.049	0.142	0.077	-0.290	0.204	0.198	0.050
12-hour	0.635	0.138	0.328	-0.064	-0.037	0.273	-0.308	0.345	-
24-hour	-0.049	0.103	0.005	0.000	-0.024	-0.108	-0.052	0.111	-

Table S29. Z-statistics between best selected nonstationary and stationary model for 50-year return period

Table S30. Z-statistics between best selected nonstationary and stationary model for 100-year return period

Duration	Toronto	Hamilton	Oshawa	Windsor	Kingston	London	Trenton	Stratford	Fergus Shand
15-min	0.615	-0.120	-0.199	0.346	0.054	0.748	-0.284	-0.311	-0.032
30-min	-0.249	0.098	-0.239	0.092	0.035	-0.208	-0.166	0.529	0.046
1-hour	-0.531	-0.192	-0.059	0.175	0.031	0.309	0.182	0.613	0.062
2-hour	-0.534	0.510	-0.127	0.051	0.236	0.185	-0.231	0.327	0.441
6-hour	-0.002	0.130	-0.083	0.130	0.087	-0.280	0.200	0.209	0.058
12-hour	0.652	0.148	0.355	-0.067	-0.010	0.302	-0.311	0.390	-
24-hour	-0.052	0.110	0.007	0.000	-0.018	-0.104	-0.041	0.127	-

## References

Anderson, D. R., Burnham, K. P. and White, G. C.: AIC model selection in overdispersed capture-recapture data, Ecology, 75(6), 1780–1793, 1994.

- Bozdogan, H.: Akaike's information criterion and recent developments in information complexity, J. Math. Psychol., 44(1), 62–91, 2000.
- Burnham, K. P. and Anderson, D. R.: Model selection and multimodel inference: a practical information-theoretic approach, Springer Science & Business Media., 2003.
- Caroni, C. and Panagoulia, D.: Non-stationary modelling of extreme temperatures in a mountainous area of Greece, REVSTAT–Statistical J., 14(2), 217–228, 2016.
- Cheng, L., AghaKouchak, A., Gilleland, E. and Katz, R. W.: Non-stationary extreme value analysis in a changing climate, Clim. Change, 127(2), 353–369, 2014.
- Cheng, L. and AghaKouchak, A.: Nonstationary precipitation intensity-duration-frequency curves for infrastructure design in a changing climate, Sci. Rep., 4, doi: 10.1038/srep07093, 2014.
- Coles, S. G. and Tawn, J. A.: A Bayesian Analysis of Extreme Rainfall Data, J. R. Stat. Soc. Ser. C Appl. Stat., 45(4), 463–478, 1996.
- Dawson, C. W., Abrahart, R. J. and See, L. M.: HydroTest: A web-based toolbox of evaluation metrics for the standardised assessment of hydrological forecasts, Environ. Model. Softw., 22(7), 1034–1052, 2007.
- Gelman, A., Shirley, K. and others: Inference from simulations and monitoring convergence, Handb. Markov Chain Monte Carlo, 163–174, 2011.
- Gelman, A., Carlin, J. B., Stern, H. S. and Rubin, D. B.: Bayesian data analysis, Chapman & Hall/CRC Boca Raton, FL, USA. (2014).
- Gilleland, E. and Katz, R. W.: Extremes 2.0: an extreme value analysis package in r, J. Stat. Software, 2016.
- Gu, X., Zhang, Q., Singh, V. P., Xiao, M. and Cheng, J.: Nonstationarity-based evaluation of flood risk in the Pearl River basin: changing patterns, causes and implications, Hydrol. Sci. J., 62(2), 246–258, doi:10.1080/02626667.2016.1183774, 2017.
- Güntner, A., Olsson, J., Calver, A. and Gannon, B.: Cascade-based disaggregation of continuous rainfall time series: the influence of climate, Hydrol. Earth Syst. Sci. Discuss., 5(2), 145–164, 2001.
- Hirsch, R. M., Slack, J. R. and Smith, R. A.: Techniques of trend analysis for monthly water quality data, Water Resour. Res., 18(1), 107–121, 1982.
- Hu, S.: Akaike information criterion, Cent. Res. Sci. Comput., 93, Available from: http://www4.ncsu.edu/~shu3/Presentation/AIC\_2012.pdf, Accessed on June, 2017, 2007.
- Hurvich, C. M. and Tsai, C.-L.: Model selection for extended quasi-likelihood models in small samples, Biometrics, 1077–1084, 1995.
- Jebari, S., Berndtsson, R., Olsson, J. and Bahri, A.: Soil erosion estimation based on rainfall disaggregation, J. Hydrol., 436, 102–110, 2012.
- Karmakar, S. and Simonovic, S.: Flood Frequency Analysis Using Copula with Mixed Marginal Distributions, Water Resour. Res. Rep. Available from: http://ir.lib.uwo.ca/wrrr/19, 2007.
- Kass, R. E. and Raftery, A. E.: Bayes factors, J. Am. Stat. Assoc., 90(430), 773-795, 1995.
- Madsen, H., Arnbjerg-Nielsen, K. and Mikkelsen, P. S.: Update of regional intensity–duration–frequency curves in Denmark: tendency towards increased storm intensities, Atmospheric Res., 92(3), 343–349, 2009.
- Mandelbrot, B. B.: Intermittent turbulence in self-similar cascades: divergence of high moments and dimension of the carrier, in Multifractals and 1/*f* Noise, J. Fluid Mechanics, 62(2), 331-358, 1974.
- Mikkelsen, P. S., Madsen, H., Arnbjerg-Nielsen, K., Rosbjerg, D. and Harremoës, P.: Selection of regional historical rainfall time series as input to urban drainage simulations at ungauged locations, Atmospheric Res., 77(1–4), 4–17, 2005.
- Olsson, J.: Evaluation of a scaling cascade model for temporal rain-fall disaggregation, Hydrol. Earth Syst. Sci. Discuss., 2(1), 19–30, 1998.
- Olsson, J.: RANDOM CASCADE MODEL: documentation, Technical Report, Swedish Meteorological and Hydrological Institute, 2012.
- Panagoulia, D., Economou, P. and Caroni, C.: Stationary and nonstationary generalized extreme value modelling of extreme precipitation over a mountainous area under climate change, Environmetrics, 25(1), 29–43, 2014.

- Petrow, T. and Merz, B.: Trends in flood magnitude, frequency and seasonality in Germany in the period 1951–2002, J. Hydrol., 371(1), 129–141, 2009.
- Rana, A., Bengtsson, L., Olsson, J. and Jothiprakash, V.: Development of IDF-curves for tropical india by random cascade modeling, Hydrol. Earth Syst. Sci. Discuss., 10(4), 4709–4738, 2013.
- Renard, B., Sun, X. and Lang, M.: Bayesian methods for non-stationary extreme value analysis, in Extremes in a Changing Climate, pp. 39–95, Springer, 2013.
- Ross, G. J.: Detecting changes in high frequency data streams, with applications, Ph.D. thesis, Imperial College London, 2013.
- Ross, G. J., Tasoulis, D. K. and Adams, N. M.: Nonparametric Monitoring of Data Streams for Changes in Location and Scale, Technometrics, 53(4), 379–389, 2011.
- Sen, P. K.: Estimates of the regression coefficient based on Kendall's tau, J. Am. Stat. Assoc., 63(324), 1379–1389, 1968.
- Serinaldi, F. and Kilsby, C. G.: The importance of prewhitening in change point analysis under persistence, Stoch. Environ. Res. Risk Assess., 30(2), 763–777, 2016.
- Ter Braak, C. J.: A Markov Chain Monte Carlo version of the genetic algorithm Differential Evolution: easy Bayesian computing for real parameter spaces, Stat. Comput., 16(3), 239–249, 2006.
- Ter Braak, C. J. and Vrugt, J. A.: Differential evolution Markov chain with snooker updater and fewer chains, Stat. Comput., 18(4), 435–446, 2008.
- Wang, X., Huang, G., Liu, J., Li, Z. and Zhao, S.: Ensemble projections of regional climatic changes over Ontario, Canada, J. Clim., 28(18), 7327–7346, 2015.
- Willems, P.: Impacts of climate change on rainfall extremes and urban drainage systems, IWA Publishing, 2012.
- Xie, H., Li, D. and Xiong, L.: Exploring the ability of the Pettitt method for detecting change point by Monte Carlo simulation, Stoch. Environ. Res. Risk Assess., 28(7), 1643–1655, 2014.
- Yaglom, A. M.: The influence of fluctuations in energy dissipation on the shape of turbulence characteristics in the inertial interval, in Soviet Physics Doklady, vol. 11, p. 26, 1966.
- Yue, S.: A bivariate gamma distribution for use in multivariate flood frequency analysis, Hydrol. Process., 15(6), 1033–1045, 2001.