Formulating and testing a method for perturbing precipitation time series to reflect anticipated climatic changes

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Abstract. Urban water infrastructure has very long planning horizons, and planning is thus very dependent on reliable estimates of the impacts of climate change. Many urban water systems are designed using time series with a high temporal resolution. To assess the impact of climate change on these systems, similarly high-resolution precipitation time series for future climate are necessary. Climate models cannot at their current resolutions provide these time series at the relevant scales. Known methods for stochastic downscaling of climate change to urban hydrological scales have known shortcomings in constructing realistic climate-changed precipitation time series at the sub-hourly scale. In the present study we present a deterministic methodology to perturb historical precipitation time series at the minute scale to reflect non-linear expectations to climate change. The methodology shows good skill in meeting the expectations to climate change in extremes at the event scale when evaluated at different timescales from the minute to the daily scale. The methodology also shows good skill with respect to representing expected changes of seasonal precipitation. The methodology is very robust against the actual magnitude of the expected changes as well as the direction of the changes (increase or decrease), even for situations where the extremes are increasing for seasons that in general should have a decreasing trend in precipitation. The methodology can provide planners with valuable time series representing future climate that can be used as input to urban hydrological models and give better estimates of climate change impacts on these systems.

1 Introduction

Climate change impacts water management worldwide as the water cycle is an essential part of the climate system. The planning horizon for water infrastructure is often very long, making reliable predictions of future climate crucial (Arnbjerg-Nielsen et al., 2015b). In the design of water infrastructure, precipitation data are needed. Especially for urban infrastructure the time resolution of precipitation data needed for design and planning is much finer than what is provided by climate models (Berndtsson and Niemczynowicz, 1988; Schilling, 1991). Hence a lot of effort is put into giving reliable estimates of what the expected change in precipitation will be at these fine scales (Fowler et al., 2007; Kendon et al., 2014; Mayer et al., 2015). Expected changes in precipitation, however, do not translate directly into changes in floods or overflows from structures. To determine these changes, urban hydrological models have to be run, driven by the changed precipitation (Olsson et al., 2009; Willems et al., 2012). By definition, fine-resolution precipitation time series for future climates are not observable, and hence a multitude of statistical approaches have been developed to enable generation of time series with properties that for a large range of metrics have the same characteristics as the expected future precipitation (Willems, 1999; Olsson and Burlando, 2002; Cowpertwait, 2006; Molnar and Burlando, 2008; Burton et al., 2010; Willems et al., 2012; Sørup et al., 2016a).

Expectations to precipitation at event level under climate change are often non-linear with the anticipation that changes in occurrence and size of extreme events will be higher than...
changes in seasonal or yearly precipitation (Boberg et al., 2010). This is a problem often solved by weather generators or other similar downscaling techniques (Fowler et al., 2007; Burton et al., 2010), but these often have difficulty in presenting realistic time series at the sub-hourly to hourly timescales relevant for urban infrastructure (Segond et al., 2006; Verhoeve et al., 2010; Sørup et al., 2016a). Several studies have tested the applicability of Markov models for simulation of high-resolution precipitation series (Srikantan and McMahon, 1983; Thyregod et al., 1998; Ailliot et al., 2009; Gelati et al., 2010; Sørup et al., 2012). The approach has the advantage that realistic chronology is created in the output. However, for very high resolutions the sensing method of the gauge may have an impact on the signal, giving an upper bound to the temporal resolution of the model, as has been shown for e.g. tipping bucket gauges (Thyregod et al., 1998; Sørup et al., 2012).

In the present study, we develop and demonstrate a novel non-linear methodology that perturbs existing precipitation time series to reflect complex expectations to precipitation in a changed future climate. The method incorporates regional historical knowledge about precipitation through the use of Intensity-Frequency-Duration (IDF) relationships (WMO, 2009) and knowledge about the expected changes in these due to climate change. Thus, the method generates time series for a changed climate which are chronologically identical to the observations used as input, but perturbed to reflect climate change. These series can be used as input for hydraulic or hydrologic models where the climate change effect has to be assessed for all possible rain conditions.

The presented methodology is based on the assumption that precipitation can be scaled according to identified expectations to climate changes. In its simplest form, this assumption is identified as the Delta Change (DC) method (Fowler et al., 2007). The basic assumption is that relative changes in output from climate models might represent expectations to climate change well even though the output itself could be wrongly scaled in absolute values. A more elaborate use of this assumption is provided by Distribution Based Scaling (DBS) presented by Yang et al. (2010). In this approach parameters are derived from regional climate model data to estimate present and future distribution functions for rainfall intensities. The relative change in the distribution parameters is applied to a similar distribution function based on observational data. Thus, perturbation of rainfall intensities due to climate change relies on the rarity of the individual events and changes markedly from average to extreme events with a high impact on hydrological responses of simulation models (van Roosmalen et al., 2011). Unlike the study by Yang et al. (2010), the expected changes in this study are not calculated directly using the DC method on Regional Climate Model output; they are derived from comprehensive state-of-the-art studies where all available data are used to determine realistic expectations to changes to precipitation due to climate change (e.g. Giorgi, 2006; Kendon et al., 2008; Christensen et al., 2015).

2 Methodology

In urban water management, the relevant time frame to consider is most often that of the rain event (Willems, 1999). The determination of robust IDF relationships for present climate at the relevant timescales is a prerequisite. For developed countries where high-resolution precipitation is generally available, these two prerequisites are very often met (Arnbjerg-Nielsen et al., 2015a), making the methodology generally relevant. The general flow of the methodology is presented in Fig. 1, and how to proceed with each step is presented in the following sections (2.1–2.5).

2.1 Modelling framework

Let us consider a system $S$ that describes precipitation over a time period. The original data are expressed as a time series of precipitation intensity over fixed time steps. This time series alternates between a dry period (no precipitation) and a rainy one. A given event is characterised as dry, extreme or non-extreme with respect to the amount of precipitation during the event.

We denote by $E$ the state space of the system $S$, with at least three states, i.e. $|E| \geq 3$. Also let $D_0$, $D_1$ and $D_2$ be the non-empty sets of states of dry periods, non-extreme and extreme events, respectively, with $|D_0| = 1$, $|D_1| = d_1 \geq 1$ and $|D_2| = d_2 \geq 1$, i.e. there exists exactly one state for dry periods, $D_0 = D^{dry}$, but a different number of extreme and non-extreme states ($d_1$ and $d_2$, respectively) can be defined for both the non-extreme and extreme events. An extreme event can be further categorised according to the severity of the phenomenon, expressed in terms of the return period of the measured intensity. Non-extreme events can be categorised according to the season in which they appear. Hence, the state space $E$ is partitioned into three disjoint subsets as follows:

$$ E = D_0 \cup D_1 \cup D_2, $$ (1)

where $D_i \cap D_j = \emptyset, i \neq j, ij \in \{0, 1, 2\}$. We link the non-extreme events to the seasonality of the phenomenon and thus $D_1 = \{D^{winter}, D^{spring}, D^{summer}, D^{autumn}\}$, that is $d_1 = 4$. $D_2$ can likewise be partitioned into one or several states appropriate for describing extreme precipitation which may have different return periods or different hydro-climatic origins. In this study, we use a partition based on return periods with $D_2 = \{D^{2}, D^{10}, D^{100}\}$, referring to states that classify the extremes as either 2-, 10- or 100-year events based on return level.

By definition there is always a dry period between two events, and we assume that there is no dependence between consecutive events. We define the following processes that describe the evolution of a semi-Markov system (Barbu and Limnios, 2008):
Define relevant system states

- \( J := (J_n)_{n \in \mathbb{N}} \) is a Markov chain with state space \( E \), where \( J_n \) is the state of the system at the \( n \)th event;

- \( U := (U_n)_{n \in \mathbb{N}} \) is the sequence of jump times between states with state space \( \mathbb{N} \) and \( U_0 = 0 \); and

- \( Z := (Z_k)_{k \in \mathbb{N}} \) is a discrete-time process with states on \( E \), with \( Z_k \) to be the state of the system at a time step \( k \).

The processes \( J \) and \( Z \) are related through the formula

\[
Z_k = J_N(k), k \in \mathbb{N}, \tag{2}
\]

where \( N(k) \) is the discrete-time counting process of events in \([1, k] \subset \mathbb{N} \), i.e.

\[
N(k) := \max \{ n \in \mathbb{N} : U_n \leq k \}. \tag{3}
\]

The corresponding transition matrix of the chain \( J \) is very simple. Figure 2b illustrates the evolution of the stochastic system described above.

2.2 Framework for determining state of individual events

There is no unique way to assign a state to an extreme event. In the literature some studies apply hydro-climatic regimes for this classification (Gelati et al., 2010; Svoboda et al., 2016), while others apply event statistics (Madsen et al., 2009; Sørup et al., 2016a). For any given application, the most appropriate classification depends on the data available. In this paper, various methods based on the maximum mean intensities are used to define the event state. For all investigated methods the changes to extremes are evaluated by calculation of IDF curves based on return levels, \( z_I \), at event level for a selection of return periods, \( I \) (WMO, 2009). The return period \( T \) of individual events across all intensities is determined using the median plotting position (Rosbjerg, 1988):

\[
T_{\text{median}} = \frac{T_{\text{total}} + 0.4}{\text{rank} - 0.3}, \tag{4}
\]

where \( T_{\text{total}} \) is the length of the time series and rank is the rank number of the individual event.

Using data with observations every minute and a minimum dry weather separation between events of 60 min, the mean maximum intensities over 5, 10, 30, 60, 180, 360 and 720 min are calculated for each event. At shorter time frames, e.g. 1 min, the variability of the observed extremes is expected to be very large due to the inherent sampling error (Fankhauser, 1998), and at very long time frames, e.g. 1 day (i.e. 1440 min), the extremes often consist of several events following one another and a different event definition would be necessary to ensure that the real extremes are identified (Madsen et al., 2009). A representative return period for the event is derived based on a mathematical comparison to regional IDF estimates (Fig. 3). This return period is then in turn used to define the state of the event. We test four different selection criteria which define the state of extreme events as either \( D^2 \), \( D^{10} \) or \( D^{100} \). The selection criteria are listed in Sect. 3.3.

Figure 1. Flow diagram showing the general process involved in the presented methodology.

Figure 2. (a) Illustration of the magnitude of perturbation of events for non-extreme summer and winter events as well as 2- and 100-year extreme events, with summer events being perturbed with a factor below 1 and factors for the winter and the extremes being above 1. Factors for extremes are higher than for the winter events, and factors for the very extreme are higher than for the more moderate extreme. (b) Illustration of the states associated with the different events if they were to happen in the shown chronology; the dry state, \( D^{100} \), is present between all wet states.
2.3 Perturbation and change factor

With each event of a time series classified according to a state, the time series can be perturbed using the following methodology linking the time series to the states of the individual events.

Let \( R_k, k \in N \), be the precipitation intensity at time step \( k \) and \( R := (R_k)_{k \in N} \) the corresponding process describing these intensities. The process of perturbed precipitation in each time step \( k \) is denoted by \( R^* := (R^*_k)_{k \in N} \).

Similarly to the state space \( E \), we introduce the state space of the change factors, denoted by \( E_{CF} \), \( |E_{CF}| = |E| \). We can then write

\[
E_{CF} = C_0 \cup C_1 \cup C_2, \tag{5}
\]

with \( |C_0| = 1 \), \( |C_1| = d_1 \) and \( |C_2| = d_2 \).

We consider the process \( CF := (CF_n)_{n \in N} \) with state space \( E_{CF} \), where \( CF_n \) is the change factor at the \( n \)th event. Let \( W := (W_k)_{k \in N} \) be the chain, with state space \( E_{CF} \), of change factors in time steps \( k \in N \), that is

\[
W_k = CF_{N(k)} \tag{6}
\]

with \( N(k) \) to be the counting process defined in (Eq. 3). Under the above notation, the original and perturbed sequences of precipitation, \( R_k \) and \( R^*_k \), are written as

\[
R^*_k = W_k R_k. \tag{7}
\]

This means that, for a sequence of events, some events will be perturbed more than others, and for extreme cases some might be reduced while others are increased, depending on the local expectations to climate change. Figure 2a shows an example where a non-extreme summer event is perturbed to a lesser volume than the original while a winter non-extreme is increased marginally and both 2- and 100-year extremes are increased considerably more (both in absolute numbers as well as in relative percentages). Figure 2b shows how the state space changes if these four events were to happen chronologically in time with the state jump times marked on the \( x \) axis.

2.4 Volume correction based on seasonal dependence of extremes

The extreme part of precipitation is only expected to constitute a smaller fraction of the total precipitation volume on an annual basis (Sørup et al., 2016b), but as extreme precipitation is often associated with a particular season (see e.g. Sørup et al., 2012), the volumetric part of the extremes might be higher for sub-annual considerations. This implies that situations where the expectations for changes to the extremes are very different from the expectations to changes to seasonal precipitation have to be handled through volumetric corrections in order to accommodate the fact that both expectations to changes in extremes and overall seasonal changes are correct. How to do this best will be very much dependent on the local conditions. In our case this is described in Sect. 3.4.

2.5 Evaluation of perturbed time series

The evaluation of the perturbed time series is done against the original time series and against the expected changes.

The average percent-wise difference between the perturbed return levels, \( z^*_i,j,m \), of the modelled time series, \( R^*_k \), perturbed with the time-dependent change factors, \( W_k \), against the same return levels, \( z_{i,j,m} \), of the original time series, \( R_k \), multiplied by the target change factor, \( CF'_e \), can be defined as

\[
\Phi_{i,j,m} = \left(1 - \frac{z^*_i,j,m}{z_{i,j,m} CF'_e}\right) \times 100 \%, \tag{8}
\]

across all IDF points, \( i \), all extremity levels and seasonality, \( j \), and all perturbed time series, \( m \). A combined skill score, \( \Phi \), across all considered metrics that describe the average deviation from the expectations, can then be defined as

\[
\Phi = \sum_{i \in I} \sum_{j \in J} \sum_{m \in M} \left|1 - \Phi_{i,j,m}\right|/|I|/|J|/|M|, \tag{9}
\]

with \( |I|/|J|/|M| \) being the product of the total number of IDF points, \( I \), the total number of extreme levels considered plus seasonality, \( J \), and the total number of time series perturbed, \( M \), as a normalization factor.

2.6 Sensitivity analysis

The robustness of the methodology is tested by evaluating its sensitivity to the actual magnitude of the target parameters for both extreme and seasonal changes. Low (L), mean (M) and high (H) scenarios are constructed and paired in all possible combinations to assess both the individual and combined influence of these (Table 1). As this increases the number of scenarios with which the precipitation time series substantially are perturbed, this is not done until after an initial evaluation of the state selection criteria.
Table 1. Tested combinations of extreme and seasonal changes.

<table>
<thead>
<tr>
<th>Seasonality</th>
<th>Low expected change</th>
<th>Mean expected change</th>
<th>High expected change</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low expected change</td>
<td>LL</td>
<td>ML</td>
<td>HL</td>
</tr>
<tr>
<td>Mean expected change</td>
<td>LM</td>
<td>MM</td>
<td>HM</td>
</tr>
<tr>
<td>High expected change</td>
<td>LH</td>
<td>MH</td>
<td>HH</td>
</tr>
</tbody>
</table>

3 Case study: Denmark

To showcase the methodology, it is applied to Danish conditions where the situation is that complex non-linear changes are expected with respect to precipitation in a changed climate.

3.1 Data

3.1.1 Observational data

Precipitation data from the Danish SVK rain gauge network are used in this study (Mikkelsen et al., 1998; Madsen et al., 2002). For this study 10 time series from different parts of Denmark with lengths of approximately 33 years between 1979 and 2012 are used. To distinguish individual events, a dry weather period between individual events of at least 60 min is applied.

3.1.2 IDF curves

For present climate IDF curves are extracted from a regional model for extremes originally developed by Madsen et al. (1998) and updated by Madsen et al. (2009) and Madsen et al. (2017). The IDF curves vary across Denmark, but a single mean regional curve is chosen for this study independently of the location of the gauge considered. Table 2 summarises the IDF values used.

3.1.3 Expectations to climate change

The official recommendations regarding climate change for urban infrastructure in Denmark was determined by Gregersen et al. (2014) on the basis of the ENSEMBLES data set (van der Linden and Mitchell, 2009), with the addition of a few simulations using high-end scenarios. The data set indicates that in general precipitation amounts and intensities will increase and that extremes will increase more than the expected mean increases for Denmark. Furthermore, the results show that it is very likely that increases will be more pronounced for the very rare extremes compared to the more frequent extremes. Table 3 sums up these official expectations for the three return periods that has to be assessed in Danish urban hydrological contexts.

In addition, the Danish Meteorological Institute has published expectations regarding climate change on a seasonal basis (Olesen et al., 2014). The analysis is performed for a range of climate variables and focuses on utilizing the data available in the best possible way to create realistic uncertainty intervals for the expected changes. The estimated change factors for precipitation are based on analysis of the RCP2.6 and RCP8.5 scenarios (Moss et al., 2010), hence a low-end emission scenario and a high-end emission scenario, respectively. Table 4 lists these expectations as well as a simple mean average of the two to represent the mean expected change. To match the change factors for extreme precipitation in Gregersen et al. (2014), which primarily is based on the more average emission A1B scenario (Nakicenovic et al., 2000), simple scaling of the seasonal expectations to a midpoint is applied, as scalability has been shown to be a valid assumption across most scales and most indices (Christensen et al., 2015). The A1B scenario does not lie exactly in the middle between the RCP2.6 and RCP8.5 scenarios, but definitely somewhere between these, and the original estimates from Olesen et al. (2014) are kept as low and high expected changes for the sensitivity analysis.

3.2 Defining states

For Denmark the state space (Eq. 1) is defined with a total of eight states based on the expectations to climate change listed in Tables 3 and 4 with four seasonal states defined for the non-extreme events and three states for the different extreme event levels:

$$E = \{D^\text{dry}, D^\text{winter}, D^\text{spring}, D^\text{summer}, D^\text{autumn}, D^2, D^{10}, D^{100}\}.$$  (10)

Correspondingly the change factors used to perturb the time series are, as a starting point, determined based on the mean expectations listed in Tables 3 and 4.

3.3 Determining state of individual events

For the determination of the state of the individual extreme events four different selection criteria are investigated, with the purpose of defining a representative return period for each event. All points mentioned refer to the return periods of the events intensity points, $T = \{T_5, T_{10}, T_{30}, T_{60}, T_{180}, T_{360}, T_{720}\}$, shown in a situation as depicted in Fig. 3:

Criterion A The maximum return period is used to define the return period of the whole event (based on one point):

$$T_\text{event} = T_1 = \max T.$$  (11)

Criterion B The mean of the three largest return periods is used to define the events (based on three points),
Table 2. IDF intensities (µm s^{−1}) for various return periods for Denmark extracted from the model presented by Madsen et al. (2017).

<table>
<thead>
<tr>
<th>Return period (years)</th>
<th>Duration (min)</th>
<th>5</th>
<th>10</th>
<th>30</th>
<th>60</th>
<th>180</th>
<th>360</th>
<th>720</th>
</tr>
</thead>
<tbody>
<tr>
<td>100</td>
<td>43.67</td>
<td>34.80</td>
<td>20.63</td>
<td>12.47</td>
<td>5.21</td>
<td>3.11</td>
<td>1.72</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>28.62</td>
<td>21.43</td>
<td>11.37</td>
<td>6.95</td>
<td>3.09</td>
<td>1.86</td>
<td>1.09</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>19.54</td>
<td>14.08</td>
<td>7.08</td>
<td>4.38</td>
<td>2.04</td>
<td>1.25</td>
<td>0.75</td>
<td></td>
</tr>
<tr>
<td>0.5</td>
<td>12.40</td>
<td>8.73</td>
<td>4.33</td>
<td>2.75</td>
<td>1.33</td>
<td>0.84</td>
<td>0.51</td>
<td></td>
</tr>
</tbody>
</table>

Table 3. Expected changes in extreme precipitation for Denmark. All values from Table 1 of Gregersen et al. (2014).

<table>
<thead>
<tr>
<th>Change factor for extreme precipitation (−)</th>
<th>2-year event (CF^{2})</th>
<th>10-year event (CF^{10})</th>
<th>100-year event (CF^{100})</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low expected change</td>
<td>1.0</td>
<td>1.0</td>
<td>1.0</td>
</tr>
<tr>
<td>Mean expected change</td>
<td>1.2</td>
<td>1.3</td>
<td>1.4</td>
</tr>
<tr>
<td>High expected change</td>
<td>1.45</td>
<td>1.7</td>
<td>2.0</td>
</tr>
</tbody>
</table>

\[ T_{\text{event}} = \frac{1}{3} \sum_{i=1}^{3} T_{i}^{*}, \]  \hspace{1cm} (12)

where \( T_{2}^{*} \) and \( T_{3}^{*} \) are the second and third maxima, respectively, i.e. \( T_{2}^{*} = \max\{T \setminus T_{1}^{*}\} \) and \( T_{3}^{*} = \max\{T \setminus (T_{1}^{*} \cap T_{2}^{*})\} \).

**Criterion C** The mean of all the return periods is used to define the events (based on all seven points):

\[ T_{\text{event}} = \bar{T}. \]  \hspace{1cm} (13)

**Criterion D** A customised step-wise threshold selection criterion is constructed where the event-specific IDF curve is compared to regional IDF levels.

Following these selection criteria, four different systems, \( S_i, i \in \{A, B, C, D\} \), are constructed and analysed.

Options \( S_A \) to \( S_C \) are straightforward based on Eqs. (11)–(13), but option \( S_D \) is determined specifically for the case study. Table 5 summarises the methodology for option \( S_D \) used in this study; specifically it is reflected that for very extreme events, fewer durations have to be extreme for the event as a whole to be considered extreme compared to the more moderate 2-year return level.

### 3.4 Volume correction based on seasonal dependence of extremes

In previous studies using the SVK data set, it has been shown that

1. the extreme events account for at most 25 % of the total rainwater volume on an annual basis (Sørup et al., 2016b), and
2. the extreme events occur mostly in the summer season (Sørup et al., 2012).

Furthermore, in the summer season the expected seasonal change (−10 %) differs mostly from the expected change in extremes (+20–40 %); see Tables 4 and 3, respectively. Based on this information the seasonal change factor for non-extreme summer events has to be adjusted to reach the overall change factors reported in Table 4. We estimate a partition between non-extreme and extreme events of \( \{f_{\text{non-extreme}}, f_{\text{extreme}}\} = \{0.8, 0.2\} \), and the change factor for 2-year events, \( \text{CF}^{2} \), is used to represent the extremes as the largest seasonal volume by far is for the more frequent extremes (Sørup et al., 2016b). In this way the change factor for summer, \( \text{CF}_{\text{summer}} \), can be adjusted from its value listed in Table 4 (0.9) as

\[ \text{CF}_{\text{summer adjusted}} = \frac{\text{CF}_{\text{summer}} - \text{CF}^{2} f_{\text{extreme}}}{f_{\text{non-extreme}}} = \frac{0.9 - 1.2 \cdot 0.2}{0.8} = 0.825. \]  \hspace{1cm} (14)

In other words the change factors for non-extreme summer events are modified from −10 to −17.5 % in order to compensate for the positive change of +20–40 % to the extremes occurring in the summer period. For the other seasons such an adjustment is not needed.

### 4 Results

#### 4.1 Evaluation of selection criteria

The 10 time series are perturbed using the four different state selection criteria (\( S_A - S_D \)) and the evaluation metric is calculated using Eq. (9) with the extreme events having return periods closest to 2, 10 and 100 years (Table 6). Overall, state
Table 4. Expected seasonal changes to precipitation in Denmark based on data from Table 5 of Olesen et al. (2014) and linearly scaled midpoint values.

<table>
<thead>
<tr>
<th>Change factor for seasonal precipitation (–)</th>
<th>Winter (CFwinter)</th>
<th>Spring (CFspring)</th>
<th>Summer (CFsummer)</th>
<th>Autumn (CFautumn)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low expected change (RCP2.6)</td>
<td>1.0</td>
<td>1.0</td>
<td>1.0</td>
<td>1.0</td>
</tr>
<tr>
<td>Mean expected change</td>
<td>1.1</td>
<td>1.05</td>
<td>0.9</td>
<td>1.05</td>
</tr>
<tr>
<td>High expected change (RCP8.5)</td>
<td>1.2</td>
<td>1.1</td>
<td>0.8</td>
<td>1.1</td>
</tr>
</tbody>
</table>

Table 5. Selection criterion \( S_D \) for choosing \( T_{\text{events}} \) at event level.

<table>
<thead>
<tr>
<th>( T_{\text{event}} )</th>
<th>Selection criterion</th>
</tr>
</thead>
<tbody>
<tr>
<td>2-year event</td>
<td>At least four points from the event have a return period above 0.5 years</td>
</tr>
<tr>
<td>10-year event</td>
<td>At least three points from the event have a return period above 2 years</td>
</tr>
<tr>
<td>100-year event</td>
<td>At least three points from the event have a return period above 10 years</td>
</tr>
<tr>
<td>non-extreme event</td>
<td>None of the above criteria are met</td>
</tr>
</tbody>
</table>

Table 6. Calculated skill scores, \( \Phi \), for the four selection criteria A–D calculated using Eq. (10).

<table>
<thead>
<tr>
<th>Selection criterion</th>
<th>( S_A )</th>
<th>( S_B )</th>
<th>( S_C )</th>
<th>( S_D )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \Phi )</td>
<td>9.3 %</td>
<td>8.5 %</td>
<td>12 %</td>
<td>6.4 %</td>
</tr>
</tbody>
</table>

Figure 4. Performance of the different selection criteria, \( S_A – S_D \), in producing (a) 2-year extremes, (b) 10-year extremes, (c) 100-year extremes and (d) seasonal changes according to the perturbation schemes listed in Tables 3 and 4.

The selection criterion \( S_D \) outperforms the other alternatives even though all selection criteria seem reasonable, as all estimated deviations are below 13 % of the expected changes.

In order to study the performance for each state, we construct the skill score variable of Eq. (8) and plot it against the duration for the individual extremes and against months for seasonal precipitation (Fig. 4). Plotted this way 100 % represents a perfect fit, 0 % represents no change and everything positive represents a change in the right direction. For the 2-year return levels both state selection criteria \( S_B \) and \( S_D \) perform similarly and with a relative change close to 100 %. State selection criterion \( S_A \) overestimates the 2-year return level by approximately 10 % on average and state selection criterion \( S_C \) underestimates it with a similar magnitude, which still corresponds to a positive change for the events (Fig. 4a). For the 10-year return level, all state selection criteria perform similarly very well (Fig. 4b). When the 100-year return level is evaluated, the reason for criterion \( S_D \)'s better overall performance becomes clear: it is the only criterion that does not systematically underestimate this return level (Fig. 4c). Even so, all criteria produce results where the direction of change is correct. Given the inherent uncertainty in estimating the actual levels of such events, obtaining close to 85 % of the expected change is considered good. With respect to the seasonal behaviour, all state selection criteria have approximately the same performance at a level close to 100 % (Fig. 4d).
(5–720 min). At the minute scale, this is of minor importance, but at 2 days (2880 min) the tendency is very robust across different state selection criteria and extremity levels. This is most likely because these average extreme events are caused by several events with dry periods in between. Hence the individual events are each assessed to be non-extreme and they are adjusted towards lower volumes, even though combined they are rather extreme.

4.2 Sensitivity analysis with selection criterion D

The sensitivity analysis is carried out for the best state selection criterion only, i.e. criterion $S_D$. The resulting skill scores for the nine individual sensitivity scenarios are listed in Table 7. The highest sensitivity is found when changing between the different extreme precipitation scenarios, with a large increase in the metric when moving from low to mean scenarios and also a notable increase when moving from mean to high scenarios. As such the performance of the methodology drops with the magnitude of the expected changes to extremes, but even for the high extremes the performance is similar to the performance of state selection criteria $S_A$ to $S_D$ in Table 6. The methodology, on the other hand, shows very little sensitivity to the variation in expectations to seasonal changes, not even for the combination where the difference between expectations to seasonal summer precipitation ($-20\%$) and the extremes become very high.

For all extreme ($+45–100\%$) indices (Fig. 5a–c), the sensitivity of the expected change in extremes is notable and, especially for the 100-year return level, it is clear that performance drops with increased magnitude of the expected changes to extremes (Fig. 5c), but only to levels comparable to that of the state selection criteria $S_A$ to $S_C$ as shown in Fig. 4. Again, the performance for 2-day events (2880 min) is worse than average, as also seen in Fig. 4. For seasonality (Fig. 5d), the general picture is that the sensitivities of both expectations to seasonality and extremes are of less importance and at a similar level, which in general is a lower level than the one observed for the three extreme indices.

<table>
<thead>
<tr>
<th>Seasonality</th>
<th>Low</th>
<th>Mean</th>
<th>High</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low</td>
<td>0.0%</td>
<td>6.0%</td>
<td>8.6%</td>
</tr>
<tr>
<td>Mean</td>
<td>1.0%</td>
<td>6.4%</td>
<td>8.8%</td>
</tr>
<tr>
<td>High</td>
<td>1.2%</td>
<td>6.3%</td>
<td>8.8%</td>
</tr>
</tbody>
</table>

Table 7. Calculated skill scores, $\Phi$, for selection criterion $S_D$ for the nine different sensitivity scenarios listed in Table 1 calculated using Eq. (9).

Figure 5. Performance of selection criterion $S_D$ for different parameter values as specified in Table 1 for (a) 2-year extremes, (b) 10-year extremes, (c) 100-year extremes and (d) seasonal changes under climate change.

5 Discussion

The proposed framework is very flexible and the separation of dry, non-extreme and extreme weather makes it possible to very effectively perturb time series to reflect different changes in different categories. The presented case study uses eight states to distinguish between different levels of extremes and different seasons and is able to produce time series that satisfactorily represent the expected changes listed in Tables 3 and 4. For other places a different number of states could be relevant and the seasonal partition could be different depending on the local climate and expectation to climate change. The proposed modelling framework fully supports these spatial variations.

Four different state selection criteria over specified event durations are tested in the present study (see Sect. 2.2), as these covered realistic possibilities for the data set used in this study and the focus on urban hydrology. As such, different state selection criteria for different event durations could be relevant in different contexts and could, as illustrated by state selection criterion $S_D$, be specified as very subjective and case-specific criteria. In this study, the subjective state selection criterion $S_D$ outperforms the other criteria (see Table 6 and Fig. 2), but the superiority is mainly due to its ability to produce the largest changes for the very large, and very uncertain, extreme events. If this part of the evaluation is disregarded, criteria $S_B$ and $S_D$ have a very similar per-
formance, pointing to criterion $S_B$ as being a good onset for investigating data sets where no presumptions exist and no case-specific criterion can be constructed.

All state selection criteria showed a drop in performance for longer duration events than the ones used in the methodology; this is likely due to the used event definition with a minimum of 60 min of dry weather between individual events, which will mean that very long lasting extremes are likely split into several events and therefore not identified as extremes. A different event definition with a longer minimum dry period between events could probably partly solve this, but it would reduce the number of events markedly and increase the chance of small events close to extremes being seen as part of the extreme, with a somewhat false classification as a consequence.

The methodology is relatively sensitive to the magnitude of the perturbation factors (see Sect. 4.2), but the sensitivity is not very dominant and is only at the same size as the sensitivity of the different state selection criteria. Also, the methodology does not address the possibilities of changes to dry spells or changes to the occurrence rate of extremes in general. A future research direction could be to study how the state selection criteria along with the semi-Markov system applied here can be used to generate fully stochastic time series where both the inter-event time and the occurrence probability of the extreme states will be included as criteria that can be changed to meet the expectations to climate change.

6 Conclusions

The proposed methodology is a promising way of creating artificially perturbed precipitation time series, which can represent a changed climate and be used as input in hydrologic and hydraulic models. The methodology perturbs existing time series based on a semi-Markov system where precipitation time series are split into events characterised as dry, extreme or non-extreme. The wet events are divided into different states based on an Intensity-Duration-Frequency relationship based state selection criterion. Of the four tested state selection criteria, the case-specific ones show the best results, but the more general criteria too could be of use when less knowledge about the precipitation regime is available. The sensitivity of the methodology was tested against very different expectations to climate change, both with respect to seasonal changes and changes to extremes, and is generally very robust, also regarding seasons where the general change is negative while the expectation to extremes is positive. The produced time series satisfactorily reproduce changes across all seasons and across all levels of extremes relevant for urban hydrology.

7 Data availability

The data set used is a product of The Water Pollution Committee of The Society of Danish Engineers made freely available for research purposes. Access to data is governed by the Danish Meteorological Institute, and they should be contacted for enquiries regarding data access at https://www.dmi.dk/erhverv/anvendelse-af-vejrdata/spildevandskomiteens-regnmaalersystem/.

Competing interests. The authors declare that they have no conflict of interest.

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References


Fowler, H. J., Blenkinsop, S., and Tebaldi, C.: Review linking climate change modelling to impacts studies: recent advances in


Olesen, M., Madsen, K. S., Ludvigsen, C. A., Boberg, P., Christensen, T., Cappelen, J., Christensen, O. B., Andersen, K. K., and Christensen, J. H.: Fremtidige klimaforandringer i Danmark (Future climate changes in Denmark), Danmarks Klimacentrum rapport nr. 6 2014, Danish Meteorological Institute, Copenhagen, Denmark, https://www.dmi.dk/fileadmin/user_upload/Rapporter/DKClimatechange_rapport.pdf (last access: 21 December 2016), 2014 (in Danish).


