

Improving the Xin'anjiang hydrological model based on mass-energy balance

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Abstract. Conceptual hydrological models are preferable for real-time flood forecasting, among which the Xin'anjiang (XAJ) model has been widely applied in humid and semihumid regions of China. Although the relatively simple mass balance scheme ensures a good performance of runoff simulation during flood events, the model still has some defects. Previous studies have confirmed the importance of evapotranspiration (ET) and soil moisture content (SMC) in runoff simulation. In order to add more constraints to the original XAJ model, an energy balance scheme suitable for the XAJ model was developed and coupled with the original mass balance scheme of the XAJ model. The detailed parameterizations of the improved model, XAJ-EB, are presented in the first part of this paper. XAJ-EB employs various meteorological forcing and remote sensing data as input, simulating ET and runoff yield using a more physically based mass-energy balance scheme. In particular, the energy balance is solved by determining the representative equilibrium temperature (RET), which is comparable to land surface temperature (LST). The XAJ-EB was evaluated in the Lushui catchment situated in the middle reach of the Yangtze River basin for the period between 2004 and 2007. Validation using ground-measured runoff data proves that the XAJ-EB is capable of reproducing runoff comparable to the original XAJ model. Additionally, RET simulated by XAJ-EB agreed well with moderate resolution imaging spectroradiometer (MODIS)-retrieved LST, which further confirms that the model is able to simulate the mass–energy balance since LST reflects the interactions among various processes. The validation results prove that the XAJ-EB model has superior performance compared with the XAJ model and also extends its applicability.

1 Introduction

Hydrological models are widely used for real-time flood forecasting due to their abilities to predict hydrological fluxes (e.g., runoff) and states (e.g., soil moisture) with various leading time (Chen et al., 2016). These models can be grouped as physically based models, which are mainly based on partial differential equations (Richards equation, de St. Venant equation, etc.) or conceptual models, which usually employ a number of mathematical functions or distribution curves to reproduce hydrological processes (Kampf and Burges, 2007; Niu et al., 2014). Conceptual models are preferred for flood forecasting with consideration of the data and computational conditions (Blöschl et al., 2008; Hapuarachchi et al., 2011). Examples are the Sacramento soil moisture accounting (SAC-SMA) model (Burnash et al., 1973) implemented by the US National Weather Service (NWS) (Smith et al., 2003), a spatially distributed flash flood model used in northern Austria (Blöschl et al., 2008), the HBV model (Bergström and Singh, 1995; Zhang and Lindström, 1997) adopted for the forecasting of Savinja catchment (Kobold and Brilly, 2006) and the Xin'anjiang (XAJ) model (Zhao, 1995) applied in the Huaihe River basin, China (Lu et al., 2008). These operational practices have proved the accuracy of stream discharge predicted by conceptual models, which is usually the major concern of real-time flood forecasting.

In China, the XAJ model is the most widely used model for flood forecasting in humid and semi-humid regions (Liu et al., 2009; Yao et al., 2009; Zhao, 1992). The XAJ model employs a spatial probability distribution curve to represent the variability of tension water capacity in the catchment and calculates runoff generation based on the conception of mass balance (Zhao, 1995). With respect to the evapotranspiration (ET), the XAJ model uses pan evaporation as its input, and then computes actual ET using an empirical relationship, taking only the soil moisture content (SMC) into account. Such a generalized scheme successfully strikes a balance between model complexity and computational accuracy, providing a reasonable runoff prediction during flood events after proper calibration against runoff observations.

At present, however, the traditional calibration approach is becoming more challenging for the XAJ model. This is partly due to the fact that the model parameters have become distributed to take account of the heterogeneities of the catchment (Xia and Zhang, 2009; Yao et al., 2012), which theoretically requires more constraints to calibrate and validate these spatially distributed parameters.

Moreover, although precipitation and runoff can be measured by traditional approaches, accurate catchment-average ET and SMC are difficult to obtain at the catchment scale. Therefore, the bias of simulations is more likely to be accumulated in SMC when only mass balance is considered. The significance of SMC to real-time flood forecasting has gradually been recognized. Studies showed that the bias in predicting flood peaks is related to unrealistic antecedent SMC estimation (Huza et al., 2014), and therefore the performance of real-time flood forecasting can be improved by setting or assimilating initial SMC (Brocca et al., 2009; Berthet et al., 2009; Komma et al., 2008; Tramblay et al., 2010; Wanders et al., 2014). The accuracy of SMC estimation before flood events largely depends on ET estimation. In addition, considering the abilities to extend the leading time and quantify predictability, ensemble flood forecasting techniques are more attractive today (Cloke and Pappenberger, 2009), and the estimation of SMC and ET is even more important in ensemble flood forecasting time.

For the aforementioned reasons, it is therefore necessary to introduce more constraints to the XAJ model, and the energy balance can serve this purpose well since the hydrological processes are governed by both mass and energy balance. One feasible way to introduce the energy balance to the XAJ model is through ET. As is discussed before, the simple and empirical ET routine of the XAJ model is based on mass balance only, and the major defects of the ET routine are (1) the input pan evaporation is measured only at few specific locations, reflecting daily evaporation from open water, which means that the potential ET (PET) over a large area is assumed to be the same; such an assumption dose not always hold under heterogeneous meteorology or underlying surface conditions (Xu et al., 2006; Yuan et al., 2008); (2) calibration of K_c (see Sect. 2.1 for details), a sensitive parameter of the XAJ model controlling water balance, is needed to convert pan evaporation to PET, which is impossible for ungauged catchments where observed runoff is unavailable; and (3) the empirical relationship linking PET with actual ET only takes water balance into account, neglecting other factors (e.g., meteorological conditions) that control ET processes (Wang and Dickinson, 2012).

It should be noted that the energy balance-based ET schemes have been intensively studied in the land surface modeling community (Overgaard et al., 2006). Land surface models (LSMs) are developed to provide various fluxes and states connecting the atmosphere and land surface (Overgaard et al., 2006; Niu et al., 2011). Most LSMs have an energy balance component for ET estimation, but the way these models solve the energy balance differs. According to Su (2002) and Kalma et al. (2008), generally three different approaches are employed by LSMs for ET estimation: (1) calculate all energy balance components except latent heat flux, which is obtained as the residual of the energy budget; (2) compute all components involved in energy balance by closing the balance equation; latent heat is solved at the same time when energy budget is closed; and (3) an empirical approach using water stress to derive ET. However, these approaches are rarely applied in hydrological models, especially for real-time flood forecasting, because their structures are complex and generally require considerable data and parameters to drive the model.

Benefiting from remote sensing and data assimilation techniques, more meteorological and land surface data are available now. The scientific community has been working to improve the ET scheme of hydrological models (e.g., Corbari et al., 2011; Niu et al., 2014; Spies et al., 2015; Yan et al., 2012). In particular, some efforts have been made to improve the ET simulation of the XAJ model. Methodologies reported can be summarized as two approaches. The first approach was to introduce a physically based formula to simulate PET based on meteorological measurements, aiming to provide more accurate PET input while the XAJ model structure remained unchanged (Yuan et al., 2008). The second approach involved replacing the ET routine by a more sophisticated scheme, typically the Penman-Monteith (PM) equation, which simulates actual ET by meteorological variables, remote sensing data and modeled SMC (Li et al., 2009; Zhou et al., 2013). These studies have demonstrated the feasibility of improving the ET scheme of the XAJ model. In these previous works, however, the mass balance and energy balance are either isolated or one-way linked, neglecting the interactions between them. Additionally, the PM equation employed tends to neglect evaporation due to the "big leaf" assumption (Yan et al., 2012). A more scientific way to simulate ET is by coupling both the mass and energy. For example, as reported by Corbari et al. (2011), a water balance model FEST (Rabuffetti et al., 2008) was augmented by coupling a energy balance scheme and various case studies have confirmed its applicability under different conditions (Masseroni et al., 2011; Corbari et al., 2013; Corbari and Mancini, 2014).

The overall goal of this paper is to develop an energy balance scheme suitable for the XAJ model, with which the mass-balance-based runoff yield scheme of the original XAJ model can be fully coupled. The improved model employs a physically based mass-energy balance component to simulate ET and runoff yield, imposing more constrains on the XAJ model. The remainder of the paper is organized as follows: Sect. 2 presents the basic theory we adopted to develop the mass-energy balance scheme for the XAJ model, Sect. 3 reports the calibration and validation of the improved model against various observations, Sect. 4 further discusses the advantages of the improved model and Sect. 5 summarizes the study.

2 Improving the XAJ model

2.1 The XAJ Model and its mass balance scheme

The XAJ model was developed by Zhao (1977, 1995) based on the concept of runoff formation with respect to repletion of storage, which means that for each location in the catchment, there is no runoff yielded until the soil water deficit is replenished. Therefore, the XAJ model is the most suitable for humid and semi-humid regions where saturation-excess runoff is more likely to occur. A statistical tension water ca-



Figure 1. Flow chart of the XAJ model. The red box denotes the model input consisting of precipitation (P) and pan evaporation (EW); the yellow boxes denote the model-simulated fluxes including evapotranspiration (ET) and discharge (TQ); the green box denotes the discharge after routing simulation (usually using the Muskingum method). Symbols outside the boxes are model parameters.

pacity curve was introduced to represent the spatial distribution of tension water capacity (maximum soil water deficit, i.e., the difference between field capacity and wilting point), which is regarded as the essence of the XAJ model. The flow chart of the XAJ model is shown in Fig. 1. All symbols outside the blocks are parameters, whose physical meanings are shown in Table 1. The inputs to the model are areal mean rainfall (P) and measured pan evaporation (EW) while the outputs are the discharge at the outlet of the basin (TQ) and the actual ET.

The basic computational unit of the XAJ model is the element area, which, in principal, is a small natural catchment that has relatively homogeneous underlying surface characteristics (terrain, soil and vegetation, etc.). Simulation of outflow from each element area consists of four major components (Li et al., 2011; Qu et al., 2011). Here we only present a simple description; for mote details, refer to Zhao (1992):

- 1. evapotranspiration, which is simulated by a three-layer soil (i.e., upper, lower, and deep layer) model based on pan evaporation and soil moisture;
- 2. runoff yield, which, based on the tension water capacity curve, simulates the runoff yield according to the rainfall and soil storage deficit;

Parameter	Definition	Calibrated value for the LS catchment
IMP	Ratio of impermeable area to the total area in the catchment	0.01
KC	Ratio of potential evapotranspiration to pan evaporation	0.95
В	Exponential of the distribution of tension water capacity	0.50
WM	Elementary area mean tension water capacity	Vary
WUM	Tension water capacity of upper layer	Vary
WLM	Tension water capacity of lower layer	Vary
С	Deeper evapotranspiration coefficient	0.10
SM	Elementary area mean free water capacity	45.00
EX	Exponential of the distribution of free water capacity	1.50
KG	Outflow coefficient of free water storage to the ground flow	0.40
KI	Outflow coefficient of free water storage to the sub-flow	0.40
CI	Recession constant of sub-flow storage	0.63
CG	Recession constant of groundwater storage	0.99
CS	Recession constant during stream routing in the elementary area	0.55
LAG	Lag time step during stream routing in the elementary area	0

Table 1. Parameter symbols and corresponding definitions in the XAJ model. Also shown the parameters calibrated for the Lushui(LS) catchment during year 2004 and 2005.

- runoff separation, which separates the abovementioned runoff into three components, i.e., surface, subsurface and groundwater;
- 4. flow routing, which transfers the local runoff to the outlet of each basin forming the outflow. Several approaches including a unit hydrograph, linear reservoir, and lag and route can be adopted.

The mass balance of the XAJ model is expressed as

$$\Delta W = P - R - \text{ET},\tag{1}$$

where ΔW is the soil water content storage term (mm); *P* is precipitation (mm); and *R* is runoff yield (mm).

The mass balance solution depends on the nonlinear relationship between W and R represented by a tension water capacity curve (Fig. 2), for a given time step when P is larger than ET, R is calculated as

$$R = P - \text{ET} - (\text{WM} - W_0) + \text{WM} \left(1 - \frac{P - \text{ET} + A}{\text{WMM}}\right)^{1+B}$$
$$(P - \text{ET} + A < \text{WMM})$$
(2)

$$R = P - \text{ET} - (\text{WM} - W_0)$$

(P - ET + A \ge WMM), (3)

where W_0 is the initial soil water (mm), A is the value of Y axis of the tension water capacity curve corresponding to W_0 (mm), WMM is the maximum tension water capacity over the catchment (mm) and WM and B are parameters of the XAJ model as listed in Table 1.



Figure 2. Tension water capacity curve of the XAJ model, which describes the tension water capacity distribution over the catchment. Each point on the curve represents a tension water capacity (*Y* axis, ranging from 0 to WMM) and the proportion of the area that has a tension water capacity no larger than that value (*X* axis). The mass balance calculation procedures of the XAJ model are presented: for a given time step when precipitation (*P*) is larger than evapotranspiration (ET), the difference between *P* and ET is partitioned into runoff (*R*, green shaded area) and soil water (ΔW , blue shaded area) based on the tension water capacity curve and initial soil water (W_0 , yellow shaded area).

2.2 Energy balance scheme developed for the XAJ model

The energy balance of land surface is expressed as

$$\Delta S = R_{\rm n} - G - H - \rm LE, \tag{4}$$

where ΔS is the energy storage term (W m⁻²), R_n is net radiation (W m⁻²), G is ground heat flux (W m⁻²), H is sensible heat flux (W m⁻²) and LE is latent heat flux (W m⁻²).

In this paper, a "patch approach" was adopted to distinguish the energy fluxes between bare soil and the canopy (Lhomme and Chehbouni, 1999; Lu et al., 2014), assuming both bare soil and the canopy receive the same radiation loading, and the total sensible and latent heat fluxes are weighted by the canopy fraction f_v derived from leaf area index (LAI):

$$f_v = 1 - e^{-0.52 \text{LAI}} \tag{5}$$

1. Net radiation (R_n)

 R_n is the arithmetic difference between downward and upward short- and long-wave radiation:

$$R_{\rm n} = R_{\rm ds}(1-\alpha) + R_{\rm dl} - \zeta \sigma ({\rm RET}^4), \qquad (6)$$

where $R_{\rm ds}$ and $R_{\rm dl}$ are downward short- and longwave radiation (W m⁻²), respectively; α is land surface albedo (–); ζ is land surface emissivity (–); σ is the Stefan–Boltzmann constant (W m⁻² K⁻⁴); and representative equilibrium temperature (RET) is representative equilibrium temperature (K).

2. Ground heat flux (G)

G is the flux that is transferred between the land surface and the subsurface via soil thermal conduction:

$$G = (k_{\rm s}/{\rm d}z)({\rm RET} - T_{\rm soil}), \tag{7}$$

where k_s is soil thermal conductivity (W m⁻¹ K⁻¹), which is related to soil conditions (Corbari et al., 2011; McCumber and Pielke, 1981); dz is the soil depth for calculating ground heat flux (m); and T_{soil} is soil temperature at depth dz (K).

Equation (7) can be solved numerically together with the heat diffusion equation as implemented by many LSMs; however, such an approach requires detailed thermal and hydrological information on different soil layers, which is not available in the XAJ model. In addition to the numerical solution, there are also other parameterizations that derive G from more easily available data, e.g., net radiation (Idso et al., 1975; Santanello and Friedl, 2003; Su, 2002), sensible heat flux (Cellier et al., 1996) or surface temperature (Bhumralkar, 1975; Deardorff, 1978; Wang and Bras, 1999). Liebethal and Foken (2007) and Venegas et al. (2013) evaluated different approaches and found these alternatives can also reproduce reasonable G after calibration. In order to accommodate the energy balance scheme, we adopted force restore model proposed by Bhumralkar (1975) and Blackadar (1976) to estimate G from RET, the original force restore equation to estimate soil temperature can be rearranged as

$$G = \frac{1}{C_T} \left[\frac{(\text{RET} - \text{RET}_0)}{\Delta t} + \frac{2\pi}{\tau} (\text{RET} - \overline{T}) \right], \qquad (8)$$

where RET₀ is the representative equilibrium temperature of the previous time step (K); Δt is time step (s); $\frac{2\pi}{\tau}$ is the angular frequency for diurnal forcing (radians s⁻¹); \overline{T} is the mean surface temperature (K); and C_T is the coefficient weighted by the volumetric heat capacity of soil and canopy:

$$C_T = 1 / \left(\frac{1 - f_v}{C_g} + \frac{f_v}{C_v} \right),\tag{9}$$

where C_g is the soil heat capacity (MJ m⁻³ K⁻¹) and C_v is the canopy heat capacity (MJ m⁻³ K⁻¹).

3. Sensible heat flux (H)

H represents heat energy transferred between the surface and air when their temperatures are different, which is the weighted average of the sensible heat flux of bare soil and the canopy:

$$H = (1 - f_v)H_s + f_vH_c,$$
 (10)

where H_s and H_c are the sensible heat flux of bare soil and the canopy (W m⁻²), respectively, which are parameterized as

$$H_{\rm s} = \frac{\rho_{\rm ac_p}}{r_{\rm abs}} ({\rm RET} - T_{\rm a}), \tag{11}$$

$$H_{\rm c} = \frac{\rho_{\rm ac_p}}{r_{\rm a}} ({\rm RET} - T_{\rm a}), \qquad (12)$$

where ρ_a is air density (kg m⁻³); c_p is the specific heat capacity of air (MJ kg⁻¹ K⁻¹); T_a is air temperature (K); r_{abs} and r_a are the aerodynamic resistances for bare soil and canopy (s m⁻¹), respectively.

The aerodynamic resistance determines the transfer of heat and water vapor from evapotranspiration surface into the air at reference height. For the canopy component, r_a is evaluated according to Thom (1972) as

$$r_{\rm a} = \frac{\left[\ln\left(\frac{z_{\rm m}-d}{z_{\rm om}}\right) - \Psi_{\rm m}\left(\frac{z_{\rm m}-d}{L}\right)\right] \left[\ln\left(\frac{z_{\rm h}-d}{z_{\rm oh}}\right) - \Psi_{\rm h}\left(\frac{z_{\rm h}-d}{L}\right)\right]}{k^2 u}, \quad (13)$$

where z_m and z_h are the reference heights where wind and humidity are measured (m); *d* is the zero plane displacement height (m); z_{om} and z_{oh} are the roughness length governing the transfer of momentum and heat, respectively (m); Ψ_m and Ψ_h are atmospheric stability correction factors for momentum and heat (–), respectively; *L* is the Obukhov length (m); *k* is the Von Karman constant; and *u* is wind speed (m s⁻¹).

In this paper, we estimated d, z_{om} and z_{oh} by empirical functions based on canopy height h (m) (Allen et al.,

1998):

$$d = 0.666 h,$$
 (14)

$$z_{\rm om} = 0.123 \, h,$$
 (15)

$$z_{\rm oh} = 0.1 \, z_{\rm om}.$$
 (16)

The aerodynamic resistance for bare soil r_{abs} can be determined in the same way as r_a using Eq. (13), but with different roughness length for bare soil. In this paper, we assumed 0.01 and 0.001 m for z_{om} and z_{oh} , respectively.

4. Latent heat flux (LE)

LE is the energy used for the phase change of water, which is directly related to ET. It is also the weighted average of the latent heat flux of bare soil and the canopy:

$$LE = (1 - f_v)LE_s + f_vLE_c,$$
(17)

where LE_s and LE_c are the latent heat fluxes of bare soil and the canopy (W m⁻²), respectively, which are parameterized following Corbari et al. (2011) as

$$LE_{s} = \frac{\rho_{ac_{p}}}{\gamma(r_{abs} + r_{s})}(e^{*} - e_{a}), \qquad (18)$$

$$LE_{c} = \frac{\rho_{ac_{p}}}{\gamma(r_{a} + r_{c})} (e^{*} - e_{a}),$$
(19)

where γ is the psychometric constant (Pa °C⁻¹); r_s and r_c are resistances for bare soil and the canopy (s m⁻¹), respectively; e^* is the saturated vapor pressure of the evapotranspiration surface (Pa); and e_a is the vapor pressure of air (Pa). In particular, e^* is also related to RET:

$$e^* = 6.11 \times 10^{\frac{7.5\text{RET}_c}{237.3 + \text{RET}_c}},$$
(20)

where RET_c is RET expressed in degree Celsius ($^{\circ}$ C).

In this paper, we parameterized r_s and r_c following the work of Corbari et al. (2011) and Yan et al. (2012), owing to the similar soil water routines of the XAJ model and models reported by these authors.

$$r_{\rm s} = 3.5 \left(\frac{\theta_{\rm sat}}{\theta}\right)^{2.3} + 33.5,\tag{21}$$

$$r_{\rm c} = \frac{1}{R_{\rm h}} \frac{r_{\rm s\ min}}{\rm LAI} \frac{\theta_{\rm fc} - \theta_{\rm wp}}{\theta - \theta_{\rm wp}},\tag{22}$$

where θ_s is saturated soil moisture (–); θ is soil moisture (–); $r_{s \min}$ is minimum stomatal resistance of canopy (s m⁻¹); R_h is relative humidity (–); and θ_{fc} and θ_{wp} are field capacity and wilting point (–), respectively.

As is summarized in Sect. 1, there are several approaches to derive latent heat flux from the energy balance. In this paper, we adopted the approach proposed by Corbari et al.

Y.-H. Fang et al.: Improving the Xin'anjiang model

(2011) where the energy balance is solved by determining RET, which is theoretically the land surface temperature (LST) that closes the balance. Given that the energy storage term (ΔS) is often negligible at the basin scale (Corbari et al., 2011) and the remaining energy budget components in Eq. (4) are all related to RET, we employed Newton–Raphson iterative method to solve RET that can close the energy balance. As reported by Corbari et al. (2011), the Newton–Raphson method is an efficient way to solve the energy balance under different hydro-meteorological conditions. The actual LE is then solved based on the resulting RET using Eq. (17) through Eq. (22).

2.2.1 XAJ-EB: the XAJ model improved by coupling mass-energy balance

The mass (Eq. 1) and energy balance (Eq. 4) is coupled through ET and W. ET is derived from LE in the energy balance as

$$ET = \frac{LE}{\lambda \rho_w},$$
(23)

where λ is the latent heat of vaporization (MJ kg⁻¹) and ρ_w is the density of water (kg m⁻³).

Different from many models that simply link the mass and energy balance, an iterative algorithm is employed here to ensure the full coupling between mass and energy balance. More specifically, for a given time step, based on W of the previous time step, the energy balance calculates ET and transfers it to the mass balance to update W. The updated Wis transferred back to the energy balance to calculate ET until the coupled mass–energy balance is achieved, i.e., difference in W from the last two iterations is below a pre-defined threshold (0.01 in this paper).

In order to couple the energy balance to the XAJ model, we changed the basic computational unit for runoff yield, from an elementary area to a grid cell. The computational unit of the energy balance scheme is grid because all inputs to it are grid-based, which is different from that of the XAJ model. We adopted the "Grid-XAJ" concept that also employs the grid as a computational unit (Li et al., 2007; Yao et al., 2009). Here, we used a grid to compute runoff yield only, rather than all processes, because runoff separation and routing are isolated from runoff yield and do not affect the mass balance of the grid.

The improved XAJ model, i.e., XAJ-EB introduces atmospheric forcing and remote sensing data as input and calculates runoff, evapotranspiration and soil water simultaneously using a grid cell based on the mass–energy balance. Runoff yield calculated for grid cells are aggregated to an elementary area for routing simulation.

By coupling the energy balance scheme, XAJ-EB is able to calculate ET based on meteorological and remote sensing data, providing ET estimation at high spatial and temporal resolution, which successfully overcomes the defects of orig-

inal ET scheme of the XAJ model. More importantly, as a key variable of the energy balance solution, RET represents the equilibrium temperature of the land surface that controls the entire mass-energy balance. RET is comparable to LST retrieved from remotely sensed imagines (Corbari et al., 2011), which serves as a new constraint of the XAJ model besides runoff.

3 Evaluation of the XAJ-EB model

3.1 Study Area

We selected a gauged catchment, namely the LuShui River catchment (LS) to test the XAJ-EB model. It is situated in the middle reaches of Yangtze River (Chang Jiang) basin and is controlled by the ChongYang hydrological site (Fig. 3). LS covers an area of 2250 km², ranging from 29.08 to 29.83° N and 113.67 to 114.17° E. Annual precipitation, pan evaporation and runoff depth of LS are 1550, 1200 and 753.3 mm, respectively (Cheng et al., 2013). The study area is mainly characterized by mountainous and hilly terrain, which covers more than 90 % the total area, with a mean elevation of 258 m. According to MODIS-based land cover climatology data (Broxton et al., 2014), the major land cover types of this area are cropland and mixed forests. There are eight precipitation sites and one hydrological site within the catchment, operated by the Bureau of Hydrology, Yangtze River Water Resources Commission.

3.2 Data

3.2.1 Digital elevation model (DEM)

We mainly relied on digital elevation model (DEM) to delineate the sub-catchments and elementary areas (the basic computational unit of the XAJ model; see Sect. 2.1 for details). The DEM dataset employed in this paper was ASTER (Advanced Spaceborne Thermal Emission and Reflection Radiometer) DEM version 2, released in October 2011 by the US National Aeronautics and Space Administration (NASA) and Japan's Ministry of Economy, Trade, and Industry (METI). The spatial resolution of ASTER DEM is 1" (approximately 30 m in the study area). DEM data were downloaded from http://dx.doi.org/10.5067/ASTER/ ASTGTM.002 and extracted based on the boundary of LS. To match the spatial scale of the model (see Sect. 3.3 for details), we further resampled the DEM to the spatial resolution of 1 km using majority resampling technique.

3.2.2 Land cover and soil data

Land cover and soil data were used to determine several land cover or soil-dependent parameters (e.g., minimal stomatal resistance and soil tension water capacity) of the model. The land cover dataset we chose was 0.5 km MODISbased Global Land Cover Climatology developed by Broxton et al. (2014) based on 10 years (2001–2010) of the MODIS land cover (MCD12Q1, Collection 5.1) product. The dataset classified the land surface into 17 different land cover types, avoiding the unrealistic land cover change as observed by the original MCD12Q1 product. The land cover dataset is available online at http://landcover.usgs.gov/global_climatology. php. Similar to the DEM data, we resampled the land cover data into 1 km spatial resolution using majority resampling technique.

We mainly used two types of soil data properties for this study, i.e., soil physical properties (e.g., field capacity), which were obtained from a dataset developed by Dai et al. (2013), and soil thickness obtained from a dataset developed by Pelletier et al. (2015). The former dataset, namely the "China dataset of soil properties", was developed mainly for land surface modeling and includes various soil hydraulic parameters derived from soil physical and chemical properties using pedotransfer functions (Dai et al., 2013). The spatial resolution of this dataset is 30" (approximately 1 km in the study area) and the vertical variation of the soil properties is documented for seven layers to a depth of 1.38 m. The soil property data were retrieved from http://globalchange.bnu. edu.cn/research/soil3. The latter dataset, namely the "gridded global dataset of soil, immobile regolith and sedimentary deposit thicknesses", documents the estimation of the thickness of the permeable layers above the bedrock (Pelletier et al., 2015), which can be regarded as soil depth defined by the XAJ model. This dataset was retrieved from http://dx.doi.org/10.3334/ORNLDAAC/1304, and it has the same spatial resolution as the China dataset of soil properties at 30".

3.2.3 Remote sensing data

Variables retrieved from remote sensing data were used to drive (e.g., LAI and albedo) or validate the model (e.g., LST). We adopted various moderate resolution imaging spectroradiometer (MODIS) products to provide spatial estimations of LAI, albedo and LST; detailed information on these variables, including product name and spatial and temporal resolution, can be found in Table 2. All remote sensing data were download from http://reverb.echo.nasa.gov/ for the period between year 2004 and 2007. The albedo dataset was resampled to a 1 km spatial resolution.

3.2.4 Meteorological and hydrological data

The meteorological forcing data we employed included precipitation, downward shortwave radiation, downward longwave radiation, wind speed, air temperature, air pressure and specific humidity from 2004 to 2007. Precipitation data from eight rain gauges were collected by the Bureau of Hydrology, Yangtze River Water Resources Commission. All other forc-



Figure 3. Lushui (LS) catchment. The red triangle is the ChongYang hydrological site that observes precipitation, pan evaporation and runoff; the green dots are precipitation sites set up to measure precipitation only; the blue line is the LS stream. The elementary areas are also shown, which are the computation unit of the XAJ models (see Sect. 2.1 for details).

Table 2. Variable, MODIS product name, and spatial and temporal resolution of the remote sensing data used in this paper

Remote sensing variable	MODIS product name	Spatial resolution	Temporal resolution
LAI	MCD15A3	1 km	4-day
Albedo	MCD43A1	500 m	16-day
LST	MOD11A1	1 km	Daily
ET	MOD16A2	1 km	8-day

ing data were retrieved from the China Meteorological Forcing Dataset (CMFD) (He and Yang, 2011), which was produced by merging a variety of data sources (Chen et al., 2011; Leng et al., 2015). The spatial and temporal resolutions of this dataset are 0.1° (approximately 10 km in the study area) and 3 h, respectively. The dataset was downloaded from http: //westdc.westgis.ac.cn/. Runoff and pan evaporation data of the ChongYang hydrological station for the same period were also collected by the Bureau of Hydrology.

3.3 Model setup

In consideration of the catchment characteristics as well as data availability, we defined the dimension of the computational grid as $1 \text{ km} \times 1 \text{ km}$, resulting in 72 columns $\times 60$ rows that covered the study area. All other datasets were resampled to $1 \text{ km} \times 1 \text{ km}$ resolution. The temporal resolution of the model is 3 h, the same as the meteorological forcing data.

The estimation of areal mean precipitation in the computational grid is crucial for the accurate hydrological modeling. Several approaches existed for spatially interpolating the precipitation from gauges; however, their performances and uncertainties depend on certain conditions including the pattern of precipitation, the characteristic of catchment and the locations of gauges (Ball and Luk, 1998; Di Piazza et al., 2011; Zhang and Srinivasan, 2009). It is difficult to evaluate the performance of different interpolation approaches in LS since the true areal precipitation is theoretically not available. In this paper, the conventional Thiessen polygon approach, the one intensively used in the XAJ model, was employed to derive the spatially distributed precipitation from eight gauges. To make the precipitation inputs of XAJ-EB comparable to those of XAJ, the precipitation of gauges are interpolated to grids by the following steps:

- Thiessen polygons were generated according to the geographic locations of gauges.
- 2. Thiessen polygons were overlaid with element areas, and the precipitation of *i*th element area (P_i) was weighted by Thiessen polygons that intersected with it (the precipitation of green-filled element area in Fig. 4 was determined by Thiessen polygons 1, 3, 4 and 5, taking their area as weight).
- 3. Grids belonging to the same element area i were assigned the same precipitation P_i .



Figure 4. Sketch plot of precipitation calculation based on element areas and Thiessen polygons.

As seen from Eq. (4) through Eq. (22), a range of parameters/variables is needed for the energy balance scheme. Each grid was assigned a set of time-independent parameters including soil physical properties (e.g., θ_{fc}) and vegetation properties (e.g., $r_{s \min}$) based on soil and vegetation type. Other time-dependent variables were obtained either from remote sensing data (e.g., LAI) or model-simulated states (e.g., θ).

3.4 Calibration and validation of the XAJ model

As listed in Table 1, several parameters have to be estimated before applying the XAJ model, among which tension water capacity WM has the physical definition that can be estimated from the soil proprieties for each grid:

$$WM = (\theta_{fc} - \theta_{wp}) \times SD, \qquad (24)$$

where SD is soil depth (mm). All three soil proprieties can be retrieved from soil dataset described above.

For parameters other than WM, 2 years of data (2004 and 2005) were chosen to perform a calibration against observed runoff data using the original XAJ model, which calculates ET using measured pan evaporation.

We first introduced a model-independent parameter estimation tool, namely PEST (Doherty et al., 1994) to provide an optimized combination of parameters. PEST is based on the Gauss–Marquardt–Levenberg (GML) algorithm (Marquardt, 1963) and has been widely applied in calibrating hydrological models. The initial values as well as the optimization limits of the parameters were set according to Zhao (1984). After the automatic calibration, we used the traditional trial and error method to adjust some parameters based on our experience in calibrating the XAJ model. This is because the algorithm implemented by PEST tries to fit the complete time series of runoff observations, regardless of high flows or low flows, while the flood events are the major concerns of real-time flood forecasting. Therefore, the trial and error method was applied to improve the simulations of high flows based on parameters optimized by PEST.

The metrics adopted to evaluate the model performance are the root mean square error (RMSE), Nash–Sutcliffe model efficiency coefficient (NSE) and relative error of total runoff volume (bias):

RMSE =
$$\sqrt{\frac{1}{n} \sum_{i=1}^{n} (Q_{\text{obs},i} - Q_{\text{sim},i})^2}$$
, (25)

$$NSE = 1 - \frac{\sum_{i=1}^{n} (Q_{obs,i} - Q_{sim,i})^2}{\sum_{i=1}^{n} (Q_{obs,i} - \overline{Q}_{obs})^2},$$
 (26)

N

$$bias = \frac{V_{sim} - V_{obs}}{V_{obs}},$$
(27)

$$V_{\rm sim} = \sum_{i=1}^{n-1} \left(\frac{Q_{\rm sim,1} + Q_{\rm sim,i+1}}{2} \right) \Delta t_i, \tag{28}$$

$$V_{\rm obs} = \sum_{i=1}^{n-1} \left(\frac{Q_{\rm obs,1} + Q_{\rm obs,i+1}}{2} \right) \Delta t_i,$$
(29)

where $Q_{\text{obs},i}$ and $Q_{\text{sim},i}$ are observed and modeled discharge (m³ s⁻¹) at time step *i*, respectively; *n* is total time step; and Δt_i is the interval between time step *i* and *i* + 1 (s).

Table 1 summaries the optimized parameter values while Fig. 5a shows comparison between XAJ-modeled and observed runoff during the calibration period. The XAJ model reproduced both the variation and amplitude of flood events with RMSE, NSE and bias values of $37.96 \text{ m}^3 \text{ s}^{-1}$, 0.70 and -0.09 %, respectively, which indicates the good performance of the model and the efficiency of our calibration strategy. One important objective of the calibration process was to control the overall water balance (-0.09 %) by adjusting KC based on pan evaporation, because the model performance is sensitive to the accuracy and representativeness of the pan evaporation observations.

To validate the model, we ran the model for another 2 years (2006 and 2007) with these calibrated parameters. Figure 5b presents the validation results, which shows the good agreement between XAJ-modeled and observed runoff. Although the XAJ model slightly overestimated the total runoff volume by 2.18 %, the RMSE and NSE were even better than the values obtained during the calibration period, further confirming the fitness and robustness of the parameters we calibrated.

3.5 Validation of XAJ-EB against runoff

Given that the mass balance of the XAJ model remained unchanged, we used the calibrated parameters directly to run



Figure 5. Comparison between observed and XAJ-modeled daily runoff for the ChongYang hydrological site for the calibration (**a**; 1 January 2004–31 December 2005) and validation (**b**; 1 January 2006–31 December 2007) period. Also shown the evaluation metrics including RMSE, NSE, and bias.



Figure 6. Comparison between observed and XAJ-EB-modeled daily runoff for tue Chong Yang hydrological site for period between 1 January 2004–31 December 2007. Also shown the evaluation metrics including RMSE, NSE, and bias.

the XAJ-EB model for the whole period between 2004 and 2007. For this simulation using XAJ-EB, the coefficient KC was eliminated since the ET was simulated directly using the mass–energy balance scheme. Figure 6 shows the comparison between XAJ-EB-modeled and observed runoff. The overall RMSE, NSE and bias were $26.09 \text{ m}^3 \text{ s}^{-1}$, 0.77 and -0.53 %, respectively. The overall performance of the runoff simulation by XAJ-EB is comparable to that of the original XAJ model.

3.6 Validation of XAJ-EB against MODIS LST

The RET simulated by XAJ-EB is theoretically the LST that closes the energy balance, which is comparable to the LST retrieved from remote sensing data, providing another variable for model calibration and validation. Among various



Figure 7. Scatter plot of MODIS-retrieved and XAJ-EB-modeled land surface temperature (LST), (a): catchment-average LST and (b): grid LST.

LST products released, the MODIS LST products have been widely used owing to high accuracy (Corbari et al., 2011, 2014b; Wan et al., 2004). The dataset we used in this paper is the MOD11A1 daytime LST product. Although it is available daily at a 1 km spatial resolution, some images are affected by cloud, resulting in a high number of missing values. In order to better validate the LST simulation, we examined each image for the whole simulation period and chose 107 images with a maximum of 30 % missing values.

We first performed grid-by-grid comparison using the sampling XAJ-EB-modeled LST according to MODIS LST data availability, the fitness was evaluated by coefficient of determination (R^2):

$$R^{2} =$$

$$\left[\frac{n\left(\sum_{i=1}^{n} \text{LST}_{\text{sim},i} \text{LST}_{\text{obs},i}\right) - \sum_{i=1}^{n} \text{LST}_{\text{sim},i} \sum_{i=1}^{n} \text{LST}_{\text{obs},i}}{\sqrt{\left[n\left(\sum_{i=1}^{n} \text{LST}_{\text{sim},i}\right) - \left(\sum_{i=1}^{n} \text{LST}_{\text{sim},i}\right)^{2}\right]\left[n\left(\sum_{i=1}^{n} \text{LST}_{\text{obs},i}\right) - \left(\sum_{i=1}^{n} \text{LST}_{\text{obs},i}\right)^{2}\right]}\right]^{2},$$
(30)

where LST_{sim_i} and LST_{obs_i} are XAJ-EB-modeled and MODIS-retrieved LST (K), respectively, at time step *i*; and *n* is the total LST data to be evaluated.

Figure 7a shows the scatter plot between the XAJ-EBmodeled and MODIS-retrieved grid LST for all 107 MODIS images we chose; the resulting R^2 value reached reaches 0.91, indicating the good agreement between the two variables. We also plotted the catchment-average LST (Fig. 7b), from which we can clearly see that most LST points are distributed along the 1 : 1 line with small deviation. Figure 7 indicates that XAJ-EB is capable of accurately simulating LST under various hydro-meteorological and underlying surface conditions.

We also plotted the time series of XAJ-EB-modeled catchment-average LST against MODIS-retrieved catchment-average LST (Fig. 8), and calculated the corresponding RMSE and NSE values as 2.25 K and 0.89, respectively. The results are acceptable since the overall accuracy of the MODIS LST product is reported to be ± 1 K





Figure 8. Time series of modeled catchment-average land surface temperature for the period between 1 January 2004–31 December 2007. The MODIS-retrieved catchment-average land surface temperature (LST) is also shown when the data availability exceeded the threshold (see Sect. 3 for details).

(Kalma et al., 2008), which further confirm the fit between XAJ-EB-modeled and MODIS-retrieved LST.

3.7 Validation of XAJ-EB against MODIS ET

There were no direct ET measurements in the LS catchment due to the lack of eddy flux towers. Consequently, to evaluate the ET simulation from XAJ-EB, we adopted the MODIS ET(MOD16A2) product as the reference. Different from the MODIS LST product, MODIS ET is based on the PM equation using various MODIS products (Mu et al., 2007, 2011). Although many studies have confirmed the overall accuracy of the product, the specific accuracy over some regions cannot always be guaranteed due to the algorithm itself as well as land surface characteristics (Corbari et al., 2014b; Mu et al., 2007, 2011; Ramoelo et al., 2014; Roux et al., 2013).

Figure 9 shows the catchment average of XAJ-EBmodeled and MODIS-estimated 8-day ET; we also included the XAJ-modeled ET here for comparison. Total MODISestimated ET for this period is 3234.8 mm, higher than the 2655.7 mm from XAJ-EB and 2393.4 mm from XAJ. However, the cumulative observed precipitation and runoff values for the whole study period were 4609.0 and 2193.3 mm, respectively, from which we can roughly estimate the cumulative ET for the same period as 2416.7 mm if we assume total precipitation can be balanced by ET and runoff over such a



Figure 9. Comparison among MODIS-retrieved, XAJ and XAJ-EB-modeled 8-day catchment-average evapotranspiration (ET) for period between 1 January 2004–31 December 2007. The 8-day gauge-measured catchment-average precipitation is also shown for the same period.

long period. Corbari et al. (2014b) reported an overestimate of MODIS ET for the Yangtze River basin, which is in accordance with our results as shown in Fig. 9; i.e., MODIS ET is higher than ET from both models. Although there is bias in the total ET estimation, XAJ-EB-modeled ET had an R^2 value of 0.70, higher than that of the XAJ-modeled ET (0.50), which means the variation in ET from XAJ-EB was close to MODIS-estimated ET.

4 Discussion

4.1 Advantages of XAJ-EB over XAJ

In this paper, the original XAJ model was improved by coupling the mass-energy balance scheme. Validations using both ground-measured runoff and remotely sensed LST have proved the performance of XAJ-EB. Compared with the original XAJ model, there are some obvious advantages of the XAJ-EB model that overcome several defects as we reported in Sect. 1. First the model is capable of providing more reliable ET at high spatial and temporal resolution based on meteorological forcing and remotely sensed data, which may influence the soil moisture and further influence the runoff simulation. During 2007, we can see from Fig. 10b that the most significant difference occurred during the dry season when there was little precipitation, and the low SMC from XAJ-EB before the two largest flood events reduced the flood peak, which was closer to the observations (Fig. 10a).

Another advantage is that XAJ-EB is more suitable for use in ungauged basins, where either measured pan evaporation or runoff data are unavailable. This is because XAJ-EB simulates ET based on meteorological forgings and remotely sensed data, rather than measured pan evaporation used by XAJ. Moreover, LST is a crucial parameter controlling the mass-energy balance, which reflects the interactions among different processes (Wang et al., 2009). Moreover, LST is also an indicator of SMC variation (Corbari et al., 2011; Sandholt et al., 2002). Therefore, the model-



Figure 10. Comparison between XAJ and XAJ-EB-modeled daily runoff (a) and soil moisture (b) for the year 2007; soil moisture is expressed as equivalent water depth (soil depth * volumetric soil moisture) as defined by the XAJ model.

simulated LST provides an alternative way to calibrate and validate the spatially distributed parameters, especially when observed runoff data are unavailable. In fact, some efforts have been made to exploit the LST for hydrological modeling (Corbari and Mancini, 2014; Corbari et al., 2014a; Silvestro et al., 2013; Wang et al., 2009), and these studies have demonstrated the possibility of using LST as a supplement to traditional runoff data.

Finally, the XAJ model is not for flood forecasting only; it has been used for investigating the effects of climate (Peng and Xu, 2010) or land cover (Tian et al., 2013; Qu et al., 2011) change on streamflow, identifying the drought events (Duan and Mei, 2014) and examining the variability of SMC memory for wet and dry basins (Rahman et al., 2015). Such studies can benefit from reliable ET and SMC simulation. By explicitly taking into consideration meteorological forcing, land cover and vegetation characteristics, XAJ-EB is more suitable than XAJ for the study of hydrological responses under changing climate/land cover, which may help to extend the applications of original XAJ model.

4.2 Applicability of simplified energy balance of XAJ-EB

As we mentioned in Sect. 1, the energy balance scheme developed for the XAJ model is physically based with proper structures that are suitable for real-time flood forecasting operations. Consequently, we used certain generalizations and simplifications, especially for LST, we adopted a lumped RET to represent the integrated LST for the land surface. In contrast, some LSMs involve more sophisticated schemes;



Figure 11. Comparison between XAJ-EB and Noah-MP-modeled catchment-average latent heat flux (**a**) and land surface temperature (**b**). Panel (**c**) illustrates the comparison between catchment-average precipitation used by XAJ-EB and Noah-MP.

e.g., Noah-MP LSM (Niu et al., 2011) introduced three different LSTs: $T_{g,b}$ for temperature of bare ground fraction, $T_{g,v}$ for temperature of the vegetated fraction and T_v for canopy surface temperature.

To further investigate the applicability of XAJ-EB, we ran Noah-MP with the same dataset we used for XAJ-EB but excluded precipitation. Because Noah-MP requires grid precipitation input, we used the CMFD precipitation field rather than the gauge-measured value. Figure 11 presents the comparison of daily LST and latent heat flux from XAJ-EB with those from Noah-MP.

LST from Noah-MP was estimated using the simulated upward long-wave radiation, which represents the integration of different land surface components within the grid (see Niu et al., 2011, for details). Figure 11a shows a generally good agreement between the XAJ-EB and Noah-MP-simulated LST, with RMSE, NSE and bias values as 1.68 K, 0.97 and -0.20 %. Such good agreement indicates that, comparing with Noah-MP with multiple LSTs, the energy balance scheme of XAJ-EB is able to produce reliable LST with only one lumped temperature.

As for the latent heat flux, although the overall bias was small (-2.53%), low NSE (0.53) indicates there is an inconsistency in inconsistence of the ET time series. This is partly due to the different precipitation fields we used for the two models, which had an NSE of only 0.51 (Fig. 11c). By comparing Fig. 11b with Fig. 11c we found that a larger bias of ET generally corresponds to a larger bias in precipitation.

In addition to the simplification of the energy balance scheme, XAJ-EB also makes use of various remote sensing

products (LAI, albedo, etc.) to eliminate the processes that have little effects on flood forecasting (e.g., vegetation dynamics), only retaining the essential processes that related to ET and runoff simulation, which help to reduce both the complexity of the model and number of parameters need calibrated.

4.3 Calibration strategy of the model

Calibration is necessary for hydrological models, even for the physically based models (Singh and Bárdossy, 2012). There has been the concern regarding the selection of runoff observations for calibration. In general, runoff data including both dry and wet conditions is required to represent the various characteristics of the catchment, from which the stable and robust parameter values can be obtained (PERRIN et al., 2007; Razavi and Tolson, 2013; Singh and Bárdossy, 2012). However, considering the data availability, researchers have been studying the calibration strategies using runoff observations of short periods (e.g., Kim and Kaluarachchi, 2009; Sun et al., 2017; Wang et al., 2017). Although specific results differ depending on the catchments as well as the models adopted, they all found that high-flow periods exert greater influence on model calibration, which implies that the hydrological models can be calibrated against high flows, which are more important for real-time forecasting.

To validate the energy balance scheme as well as the XAJ-EB model developed in this paper, a two-step calibration of the XAJ model was applied (Sect. 3.4). The first step was to calibrate the parameters using PEST based on the complete time series of runoff observations. This is because the calibration of parameter KC requires complete runoff observations of several years to ensure that the accumulated simulated runoff was close to the corresponding observed value (Zhao, 1992), and the validation of LST and ET from XAJ-EB also requires accurate mass balance simulations all through the year, covering flood and non-flood periods, to better evaluate the performance of the model under various hydro-meteorological conditions. Then for the second step, the trial and error method was applied to adjust the resulting optimized parameters, mainly according to the high flows of flood events. Such straightforward but effective calibration strategy stroked a balance between the representativeness of the runoff data and the importance of large flood events, providing the reliable baseline to validate the XAJ-EB model in this study. However, a more rigorous quantification of the uncertainties in parameters calibration is need for the XAJ and XAJ-EB model in subsequent studies.

5 Conclusion

In this paper, an energy-balance-based scheme suitable for the XAJ model was developed by explicitly taking account of bare soil and the canopy using a "patch approach". Different energy fluxes for bare soil and the canopy respectively were parameterized. The energy balance was simulated by determining RET, which is theoretically the LST that closes the balance. The energy balance scheme was then fully coupled to the mass balance scheme of the XAJ model. In the improved model, XAJ-EB estimates the actual ET and runoff yield through a mass-energy balance approach using various meteorological and remotely sensed data.

Taking the LS catchment as the study area, we calibrated and validated the original XAJ model and used the same optimized parameters to evaluate the performance of the XAJ-EB model. With respect to the runoff simulation for the period between 2004 and 2007, the XAJ-EB model had RMSE, NSE and bias values of $26.09 \text{ m}^3 \text{ s}^{-1}$, 0.77 and -0.53 %, respectively. The results well matched the observed runoff, which was also comparable to the original XAJ model. In addition to runoff, XAJ-EB is also capable of simulating the dynamics of LST with R^2 , RMSE and NSE values of 0.93, 2.25 K and 0.89, respectively, compared with MODISretrieved catchment-average LST. The good match between modeled and remotely sensed LST implies that the XAJ-EB model is able to reproduce the mass-energy balance processes since LST reflects the interactions among various processes. Moreover, with LST as an output, XAJ-EB adds a new constraint and offers a potentially new approach for model calibration and validation, especially when runoff data are unavailable.

The mass-energy balance scheme developed in this paper is comparable to the sophisticated LSM Noah-MP model in terms of LST and latent heat flux modeling, which overcomes several defects of the original XAJ model that simulates actual ET using pan evaporation measurements. The inter-comparison between XAJ-EB and XAJ shows that the improvement of ET estimation helps to improve the runoff simulation, especially the runoff peak, which is the major concern of real-time flood forecasting. Moreover, by explicitly taking into consideration different atmospheric and underlying surface conditions, XAJ-EB is more suitable than XAJ for the study of hydrological responses under changing climate/land cover, which extend the applications of the original XAJ model.

Data availability. All data except hydrological data (i.e. precipitation, pan evaporation, runoff) can be accessed through URLs provided in Sect. 3.2. Those who need hydrological data can contact the corresponding author X. Zhang (zxn@hhu.edu.cn).

Author contributions. XZ and CC designed and supervised the study; Y-HF, CC, MM and G-YN developed the model and conducted simulations; WZ collected and processed the remote sensing and ground-measured data; all authors contributed to the preparation of this manuscript.

Competing interests. The authors declare that they have no conflict of interest.

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