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Trends and abrupt changes in 104 years of ice cover and water temperature in a dimictic lake in response to air temperature, wind speed, and water clarity drivers

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Abstract. The one-dimensional hydrodynamic ice model, DYRESM-WQ-I, was modified to simulate ice cover and thermal structure of dimictic Lake Mendota, Wisconsin, USA, over a continuous 104-year period (1911-2014). The model results were then used to examine the drivers of changes in ice cover and water temperature, focusing on the responses to shifts in air temperature, wind speed, and water clarity at multiyear timescales. Observations of the drivers include a change in the trend of warming air temperatures from 0.081 °C per decade before 1981 to 0.334 °C per decade thereafter, as well as a shift in mean wind speed from $4.44 \,\mathrm{m\,s^{-1}}$ before 1994 to $3.74 \,\mathrm{m\,s^{-1}}$ thereafter. Observations show that Lake Mendota has experienced significant changes in ice cover: later ice-on date(9.0 days later per century), earlier ice-off date (12.3 days per century), decreasing ice cover duration (21.3 days per century), while model simulations indicate a change in maximum ice thickness (12.7 cm decrease per century). Model simulations also show changes in the lake thermal regime of earlier stratification onset (12.3 days per century), later fall turnover (14.6 days per century), longer stratification duration (26.8 days per century), and decreasing summer hypolimnetic temperatures (-1.4 °C per century). Correlation analysis of lake variables and driving variables revealed ice cover variables, stratification onset, epilimnetic temperature, and hypolimnetic temperature were most closely correlated with air temperature, whereas freeze-over water temperature, hypolimnetic heating, and fall turnover date were more closely correlated with wind speed.

Each lake variable (i.e., ice-on and ice-off dates, ice cover duration, maximum ice thickness, freeze-over water temperature, stratification onset, fall turnover date, stratification duration, epilimnion temperature, hypolimnion temperature, and hypolimnetic heating) was averaged for the three periods (1911-1980, 1981-1993, and 1994-2014) delineated by abrupt changes in air temperature and wind speed. Average summer hypolimnetic temperature and fall turnover date exhibit significant differences between the third period and the first two periods. Changes in ice cover (ice-on and iceoff dates, ice cover duration, and maximum ice thickness) exhibit an abrupt change after 1994, which was related in part to the warm El Niño winter of 1997-1998. Under-ice water temperature, freeze-over water temperature, hypolimnetic temperature, fall turnover date, and stratification duration demonstrate a significant difference in the third period (1994–2014), when air temperature was warmest and wind speeds decreased rather abruptly. The trends in ice cover and water temperature demonstrate responses to both long-term and abrupt changes in meteorological conditions that can be complemented with numerical modeling to better understand how these variables will respond in a future climate.

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1 Introduction

Many studies have shown that lake temperatures and ice cover can strongly affect water chemistry, individual organism physiology, population abundance, community structure, and food-web dynamics (King et al., 1997; Schindler et al., 1990). Air temperature (Findlay et al., 2001; Lynch et al., 2015), wind speed (Brown et al., 1993; Lynch et al., 2015), and water clarity (Arhonditsis et al., 2004b; Lathrop et al., 1996) are important factors driving these lake ecosystem properties. Understanding how lakes respond to changes in these drivers is of great interest to predict how lakes may change in the future (Fang and Stefan, 2009; Magnuson et al., 1997; Robertson, 1989). The response of lake ice and water temperature to long-term changes in air temperature and wind speed is integral to assess potential impacts of climate change on lake ecology.

Over the past 100 years, climate has been changing and will continue to change (IPCC, 2013). Globally averaged combined land and ocean surface temperature data show a linear warming trend of 0.85 °C from 1880–2012 (IPCC, 2013). This warming was most pronounced from 1979– 2012, greater than 0.25 °C per decade (Hartmann et al., 2013). Increases in air temperature alter the ice cover of lakes (Butcher et al., 2015; Magnuson et al., 2000; Robertson et al., 1992) and affect their thermal structures (Robertson and Ragotzkie, 1990), evidenced by increasing epilimnetic temperatures (Arhonditsis et al., 2004a; Dobiesz and Lester, 2009; Schindler et al., 1990), warming of the lake surface temperature (Schneider and Hook, 2010; Shimoda et al., 2011), increasing temperature gradient across the thermocline (Robertson and Ragotzkie, 1990; Wilhelm and Adrian, 2008), changing thermocline depth (King et al., 1997; Schindler et al., 1990), advancing the onset of summer stratification (Austin and Colman, 2007), delaying fall turnover (King et al., 1997), increasing the strength of thermal stratification (Rempfer et al., 2010), and prolonging the stratified period (Robertson and Ragotzkie, 1990; Wilhelm and Adrian, 2008).

Trends in wind speed over the last 30-50 years have been reported in several studies that have analyzed historical wind speed records across the globe (Jiang et al., 2009; Wan et al., 2010). Klink (2002) examined 22- to 35-year records (ranging between 1959 and 1995) of wind speed at seven stations in and around Minnesota and found decreasing annual wind speeds at five of the seven stations. Pryor et al. (2009) reported that the 50th and 90th percentile annual wind speeds over the period 1973-2005 across most of the US have also decreased. Decreased wind speeds increase thermal stratification and can reduce whole-lake average temperature (Tanentzap et al., 2008). Interestingly, an opposing trend (increasing wind speed) has been observed in Lake Superior, North America, where the lake surface temperatures have been warming faster than air temperatures (Austin and Colman, 2007). Desai et al. (2009) suggest that the larger increase in water temperatures than air temperatures reduced the air—water temperature gradient and destabilized the atmospheric surface layer above Lake Superior, which resulted in increasing wind speed at a rate of nearly 5% per decade. Differences in wind-driven mixing may explain different temperature responses of hypolimnetic waters in large and small lakes (Winslow et al., 2015). While the importance of wind in lake heat transfer (Fu et al., 2009; Read et al., 2012), mixing, and thermal structure (Desai et al., 2009; Schindler et al., 1990) has been recognized, studies on the effects of wind speed alterations on seasonal ice cover and thermal structure of lakes are still rare.

Water clarity, which controls the amount of solar radiation penetrating into a lake, plays an important role in heat budgets in lakes. Increased water clarity can result in warmer deep waters (Stefan et al., 1996), while reduced light penetration can result in decreased mixing depth and cooler deep waters (Hocking and Straškraba, 1999; Tanentzap et al., 2008). Previous studies have also shown that increased water clarity was correlated with deeper mixed-layer depth (Fee et al., 1996; Mazumder and Taylor, 1994; Schindler et al., 1996) and increased hypolimnetic heating rate (Yan, 1983). Water clarity has important consequences for photosynthesis and vertical distribution of biota. Accompanied by a warming climate, increased evaporation and changes in precipitation patterns can alter the inputs of nutrients and dissolved organic carbon (DOC) into lakes, resulting in changes in water clarity (Schindler et al., 1990, 1996).

Abrupt shifts, rather than linear changes, can occur in both climate and lake variables over long timescales. In the past, the majority of referenced studies used some form of linear regression analysis to look for changes, which assumes that lakes undergo monotonic changes over time (Van Cleave et al., 2014). This assumption can mask the occurrence of step changes (Liu et al., 2013; North et al., 2013) and can hide the underlying mechanisms that are responsible for the changes (North et al., 2014). As noted in other studies (Mueller et al., 2009; Van Cleave et al., 2014), long-term changes in lake thermodynamic variables can be associated with a pronounced, nonlinear step change that indicates a rapid switch between stable states or regimes (North et al., 2013; Rodionov, 2004; Scheffer et al., 2001). Identifying this type of abrupt change in climate drivers and corresponding abrupt or gradual change in lake variables may shed light on the role of changing climate on the corresponding ecosystem.

The purpose of this study is to investigate how long-term changes in air temperature, wind speed, and water clarity affect the ice cover and thermal structure of a dimictic Lake Mendota, Wisconsin, USA during the past century using a long-term 104-year simulation model. We hypothesize that changes in lake ice cover (ice-on and ice-off dates, ice cover duration, and maximum ice thickness) and thermal structure (stratification onset, fall turnover date, stratification duration, water temperatures, and hypolimnetic heating) variables may be characterized by periods of abrupt change rather than

gradual trends, based on observations of rapid change in the climate drivers of air temperature and wind speed. To address this, a one-dimensional hydrodynamic model with ice cover is employed to simulate long-term (1911–2014) ice cover and water temperature in the lake. With the knowledge of lake responses to these past conditions, we aim to reveal how lakes might respond to future changes in air temperature, wind speed, and water clarity.

2 Methods

2.1 Hydrodynamic model

An ice and snow model was added to the DYRESM-WQ model (Hamilton and Schladow, 1997), a physically based one-dimensional hydrodynamic model for simulating vertical mixing and advective transport in lakes and reservoirs. The resulting model, DYRESM-WQ-I (Hsieh, 2012), is used to simulate daily changes in the vertical distribution of water temperature and ice cover in Lake Mendota from 1911-2014. In this model, the lake is represented by a series of Lagrangian horizontal layers with uniform properties that may change in elevation and thickness in response to inflows/outflows and surface mass fluxes (evaporation and precipitation). Layer thickness is updated using an algorithm to give appropriate vertical density resolution at each time step. Mixing in the model is represented by merging the layers when the sum of available turbulent kinetic energy (TKE) produced by wind stirring, convective turnover, and shear stress exceeds the potential energy required to mix the adjacent layer below. Hypolimnetic mixing is modeled with an eddy diffusivity coefficient, which is a function of the dissipation of TKE and strength of stratification. More detailed descriptions of the simulation of water temperature and mixing are provided by Imberger and Patterson (1981).

The ice model is based upon the MLI model of Rogers et al. (1995) with alterations to two-way coupling of the watercolumn dynamics to the ice model and the addition of timedependent sediment heat flux for all horizontal layers. Ice growth in the model is based upon a quasi-steady state assumption that the timescale for heat conduction through the ice is short relative to the timescale of meteorological forcing (Patterson and Hamblin, 1988; Rogers et al., 1995). This assumption is valid under a Stefan number < 0.1 (Hill and Kucera, 1983). The ice module is applied when the simulated surface water temperature first drops below 0 °C; the initial ice thickness is set to a value of 5 cm to address effects of partial ice cover (Patterson and Hamblin, 1988; Vavrus et al., 1996). Upward conductive heat flux between ice/snow cover and the atmosphere, q_0 , is determined by numerically solving the quasi-steady state heat conduction equations (Rogers et al., 1995) and assigning appropriate boundary conditions to the water, ice, and atmospheric interfaces. At the ice (or snow) surface, a heat flux balance provides the condition for surface melting, and accretion or ablation of ice is determined through the heat flux at the ice—water interface. Imbalance between heat conduction through ice and the heat flux from the water to the ice gives the rate of change of ice thickness at the ice—water interface. Snow conductivity is estimated from its density using an empirical equation (Ashton, 1986), and snow compaction is based on an exponential decay formula (McKay, 1968), with snow compaction parameters based on air temperature and snowfall/rainfall (Rogers et al., 1995). Snow (white) ice is generated in response to flooding, when the mass of snow that can be supported by the ice cover is exceeded. The uppermost solid layer of ice or snow is adjusted in thickness at the end of each 1 h model time step according to the balance of the heat budget. When ice thickness decreases to less than 5 cm, open water conditions are restored.

Sediment heat flux, the main external source of heat after freezing, is important to water temperatures beneath ice cover (Ellis et al., 1991). Sediment heat flux (Fang and Stefan, 1996a) is included as a source/sink term for each Lagrangian layer to closely simulate under-ice water temperatures. A simple diffusion relation (Rogers et al., 1995) is used to estimate heat transfer from the sediments to the water column, q_{sed} :

$$q_{\text{sed}} = K_{\text{sed}} \frac{\mathrm{d}T}{\mathrm{d}z},\tag{1}$$

where K_{sed} is the sediment conductivity (= 1.2 W m⁻¹ °C⁻¹). dT/dz, the temperature gradient across the sediment–water interface, is estimated as

$$\frac{\mathrm{d}T}{\mathrm{d}z} \approx \frac{T_{\mathrm{s}} - T_{\mathrm{w}}}{z_{\mathrm{sed}}},\tag{2}$$

where $T_{\rm s}$ is the sediment temperature, $T_{\rm w}$ is the water temperature adjacent to the sediment surface, which varies hourly and with depth, and $z_{\rm sed}$ is the distance beneath the water–sediment interface at which the sediment temperature becomes largely invariant. From data collected at four locations on Lake Mendota (Birge et al., 1927), it was found that sediment temperatures varied little at 5 m depth below the sediment–water interface, so $z_{\rm sed}$ is set to be 5 m. In addition, data from Birge et al. (1927) are used to fit a curve to describe the seasonal variation of $T_{\rm s}$

$$T_{\rm s} = 9.7 + 2.7 \sin \left[\frac{2\pi (D - 151)}{\rm TD} \right],$$
 (3)

where *D* is the number of days from the start of the year and TD is the total number of days for the year of interest (365 or 366). The vertical transfer of heat in the water column beneath the ice is regulated by an assigned thermal diffusion coefficient. The formulation is the same as that originally used in DYRESM-WQ (Hamilton and Schladow, 1997) to simulate heat transfer throughout the open water period. This

produced diffusivities that were within the range of measurements by Ellis et al. (1991) of 1–3 times greater than molecular values.

Input for the model includes lake morphometry (lake volume and surface area as a function of elevation), initial vertical profiles for water temperature and salinity, Secchi depth, meteorological variables, and inflows/outflows. The model calculates the surface heat fluxes using meteorological variables: total daily shortwave radiation, daily cloud cover, air vapor pressure, daily average wind speed, air temperature, and precipitation. During the simulation, all parameters/coefficients in the model are kept constant. The time step in the model for calculating water temperature, water budget, and ice thickness was set to 1 h. Snow ice compaction, and snowfall and rainfall components are updated at a daily time step, corresponding to the frequency of meteorological data input. Cloud cover, air pressure, wind speed, and air temperature are assumed to be constant throughout the day, and precipitation is assumed uniformly distributed. Shortwave radiation distribution throughout the day is computed based on the lake latitude and the day or year. The DYRESM-WQ-I model is calibrated using measured lake variables including water level, temperature profiles, ice thickness, and ice-on and iceoff dates. The overall simulation period was 104 years, starting with an isothermal (measured) water column temperature of 3.1 °C on 7 April 1911 and ending on 31 October 2014.

2.2 Model calibration

The model was calibrated for the period 1995-2014 by varying the minimum layer thickness over values ranging from 0.05 to 0.5 m at 0.025 m intervals. Layer thickness values were evaluated for the least amount of deviation between predicted and observed temperature values for Lake Mendota over the period. Based on this analysis, a minimum layer thickness of 0.125 m was chosen as the best setting to predict water temperature at all depths. Other parameter values in the hydrodynamic and ice cover models were obtained from literature values (Table 1). To evaluate the performance of the model, root mean square error (RMSE) was used to compare simulated and observed ice cover and water temperature values for the full model period (1911–2014; see Sect. 4.2). Simulated and observed values are compared directly, with the exception of aggregation of water temperature measurements to daily intervals where subdaily intervals were available.

2.3 Piecewise regression algorithm

Breakpoints in the air temperature trend over the study period were determined using a piecewise linear regression (PLR) method (Tomé and Miranda, 2004; Toms and Lesperance, 2003; Ying et al., 2015) that assumes continuity in the trendlines across the breakpoint. The piecewise linear regression model finds the breakpoint, B, that minimizes the residual

Table 1. Values of DYRESM-ICE parameters and model simulation specifications for both hydrodynamic and ice cover portions of the model.

Parameter	Value				
Hydrodynamic model parameters					
Albedo Bulk aerodynamic momentum transport coefficient Critical wind speed (m s ⁻¹) Effective surface area coefficient (m ²) Emissivity of water surface Potential energy mixing efficiency Shear production efficiency Vertical mixing coefficient Wind stirring efficiency Minimum layer thickness	$0.08^{i,ii}$ 0.00139^{ii} 4.3^{ii} $1 \times 10^{7 iii}$ 0.96^{iv} $0.2^{i,ii}$ $0.06^{i,ii,iii}$ 200^{iii} 0.8^{ii}				
Maximum layer thickness Vertical light attenuation coefficient	0.6 ⁱⁱ variable ^v				
Ice model parameters					
Waveband 1, snow ice light extinction (m ⁻¹) Waveband 2, snow ice light extinction (m ⁻¹) Waveband 1, blue ice light extinction (m ⁻¹) Waveband 2, blue ice light extinction (m ⁻¹) Waveband 1, snow light extinction (m ⁻¹) Waveband 2, snow light extinction (m ⁻¹) Distance of heat transfer, ice—water (m) Density, snow ice (kg m ⁻³) Density, blue ice (kg m ⁻³) Density, snow (kg m ⁻³) Compaction coefficient Thermal conductivity, snow ice (W m ⁻¹ °C ⁻¹)	3.8 ^{vi} 20 ^{vi} ,vii 1.5 ^{vi} ,vii 20 ^{vi} ,vii 6 ^{vi} ,vii 20 ^{vi} ,=vii 0.039 ^{viii} 890 ^{vi} 917 ^{vi} ,vii variable ^{ix} variable ^{vi} 2.0 ^{vi}				
Thermal conductivity, show the (W m ⁻¹ $^{\circ}$ C ⁻¹) Thermal conductivity, snow (W m ⁻¹ $^{\circ}$ C ⁻¹) Thermal conductivity, sediment (W m ⁻¹ $^{\circ}$ C ⁻¹) Thermal conductivity, water (W m ⁻¹ $^{\circ}$ C ⁻¹)	2.3 ^{vi} ,vii variable ^x 1.2 ^{vi} 0.57 ^{vi} ,vii				

Sources: ⁱ Antenucci and Imerito (2003); ⁱⁱ Tanentzap et al. (2007); ⁱⁱⁱ Yeates and Imberger (2003); ^{iv} Imberger and Patterson (1981); ^v Williams et al. (1980); ^{vi} Rogers et al. (1995); ^{vii} Patterson and Hamblin (1988); ^{viii} Vavrus et al. (1996); ^{ix} McKay (1968); ^x Ashton (1986).

sum of squares (RSS_{PLR}) of the model between the two phases (Ying et al., 2015)

$$RSS_{PLR} = \sum_{i=1}^{n} [y_i - \alpha - k_1 x_i - (k_2 - k_1) \max(x_i - B, 0)]^2,$$
(4)

where x_i and y_i are the time and air temperature data corresponding to the *i*th data point, respectively, and k_1 and k_2 are the slopes of the linear fit to data before and after the breakpoint B. The parameter α is the intercept of the linear fit to data below the estimated breakpoint B, and n is the series length.

An F test was used to compare the residual sum of squares of an ordinary linear regression model with the piecewise lin-

ear regression model with a level of $\alpha = 0.05$ used to indicate significance, and the breakpoint year was determined to pass with p = 0.0016.

2.4 Sequential t test analysis of abrupt changes

Abrupt changes in mean annual wind speeds and lake ice cover and temperature variables were detected using the sequential t test STARS (Rodionov, 2004), which can automatically detect multiple change points. A shift occurs when a statistically significant difference exists between the mean value of the variable before and after a certain point based on the t test. The variables were tested using a threshold significance level p = 0.05, a Huber weight parameter, h = 1 (North et al., 2013; Rodionov, 2006), and a cut-off length L = 15 years (North et al., 2013).

3 Model input data

3.1 Bathymetry

Lake Mendota (43°40′ N, 89°24′ W) has a surface area of 39.4 km² and maximum fetch of 9.8 km (Kitchell, 1992). The mean depth is 12.7 m, and maximum depth is 25.3 m. For detailed bathymetry refer to Kamarainen et al. (2009).

3.2 Meteorological variables

Daily meteorological data required to run the DYRESM-WQ-I model include solar radiation, air temperature, vapor pressure, wind speed, cloud cover, rainfall, and snowfall. Daily air temperatures are computed as the average of daily maximum and minimum temperatures. Vapor pressure, wind speed, and cloud cover are also entered as daily average values while solar radiation, rainfall, and snowfall are daily accumulation values.

Meteorological data for the Madison area have been continuously recorded since 1869, however, the station and techniques have changed several times. Robertson (1989) constructed a continuous, homogeneous daily meteorological data set from 1884 to 1988 by adjusting for changes in site location and observation time, and resultant changes in the surface roughness (e.g., height of surrounding trees and buildings). These data were appended with data from the most recent weather station of the National Climate Data Center (NCDC, NOAA) located in Madison (MSN) Dane County Regional Airport (Truax Field), approximately 4.5 km east from the simulation location, the same site as that used in 1988. All data except solar radiation can be obtained for MSN from http://www.ncdc.noaa.gov/, except solar radiation which can be obtained from http://www.sws. uiuc.edu/warm/weather/ (approximately 150 km southeast of Lake Mendota). Since Robertson (1989) adjusted all historical data to that collected in 1988, no adjustments are applied to the recent data except for wind. In 1996, a discontinuity in the wind record was caused by change in observational techniques and sensor locations (McKee et al., 2000). To address the nonclimatic changes in wind speed, data from MSN are carefully compared with those collected from the tower of the Atmospheric and Oceanic Science Building at the University of Wisconsin-Madison (http://ginsea. aos.wisc.edu/labs/mendota/index.htm), approximately 4 km south of simulation location. Hourly data from both sites ($U_{MSN,hourly}$ and $U_{AOS,hourly}$) during 2003–2010 were used to form a 4×12 (four components of wind direction \times 12 months) matrix ($K_{4,12}$) of wind correction factors, yielding $U_{AOS,daily} = K_{i,j} \times U_{MSN,daily}$. A comparison of results indicated that the MSN weather station measured a higher magnitude in winds out of the east by 5 % and lower magnitude in winds out of the west and south by 30 and 10 %, respectively. The adjusted wind data (= $K_{i,j} \times U_{\text{MSN,daily}}$) are used in the model simulation. Overall the adjusted wind data show a decline in mean wind velocities of 16% from 1988-1993 to 1994-2014) compared to 7% at a nearby weather station with no known observational changes (St. Charles, Illinois; 150 km southeast of Lake Mendota).

3.3 Light extinction

Seasonal Secchi depths can be used to determine the light extinction coefficient for DYRESM-WQ-I. Lathrop et al. (1996) compiled Secchi depth data for Lake Mendota between 1900 and 1993 (1701 daily Secchi depth readings from 70 calendar years), and summarized the data for 6 seasonal periods: winter (ice-on to ice-off date), spring turnover (ice-off date to 10 May), early stratification (11 May to 29 June), summer (30 June to 2 September), destratification (3 September to 12 October), and fall turnover (13 October to ice-on date). After 1993, Secchi depths were obtained from the North Temperate Lakes - Long Term Ecological Research (NTL-LTER) (https://portal.lternet.edu/nis/home. isp#). For years with no Secchi data, the long-term mean seasonal Secchi depth was used to estimate light extinction. Light extinction coefficients are calculated as a function of Secchi depth using the equation, $k = 1.1/z_s^{0.73}$ (Williams et al., 1980), where k is the light extinction coefficient and z_s is the measured Secchi depth, in meters.

3.4 River inflow and outflow

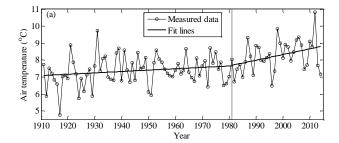
Daily inflow measurements have been made on selected Lake Mendota tributaries since 1974, and daily outflow from the lake has been measured since 1975. Streamflow for the tributaries were obtained from http://waterdata.usgs.gov/wi/nwis/sw/. Daily outflow from 1975 to 1997 were calculated from gate/lock/bypass pipe USGS ratings and local governmental daily operational records. Daily outflow from 1998 to 2003 were estimated from monthly outflow estimates from downstream Lake Waubesa and Mendota outlet data from earlier years. Daily outflow from 2003 to the present, were ob-

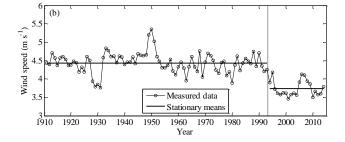
tained from http://waterdata.usgs.gov/wi/nwis/uv/?site no= 05428000. These measurements were used to calculate total daily inflow and outflow. Total daily inflow and outflow from 1930 to 1974 were estimated from measurements made at the gauging station downstream of the lake using the drainage-area ratio method (Maidment, 1993). Prior to 1930, total inflow and outflow were calculated using a water budget approach, i.e., the balance of inflow/outflow, precipitation, evaporation, and lake level changes. The inflow/outflow is the residual unknown term of the water balance where other terms include evaporation, rainfall, and water level. The calculation is performed at the interval of water level measurements and the residual term is then distributed evenly across the number of days between water level measurements. Water level of Lake Mendota has been recorded since 1916 at the Yahara River inlet in the north of the lake (http://waterdata.usgs.gov/wi/nwis/dv). Prior to 1916, the long-term mean lake level was assumed in water budget calculations. River water temperature has been recorded at the Yahara River inlet since 2002 (US Geological Survey, http://waterdata.usgs.gov/nwis). To estimate daily river temperatures prior to 2002, river temperatures were estimated from air temperatures (Hsieh, 2012). A linear regression was used to correlate river temperatures and weekly average air temperature data during 2002–2009 for air temperatures above the freezing temperature ($r^2 = 0.86$), and a separate polynomial regression analysis was performed for air temperatures below the freezing temperature ($r^2 = 0.68$).

3.5 Lake ice cover and water temperature

Observed ice cover data from 1911-2014 (available at NTL-LTER website: https://portal.lternet.edu/nis/home. jsp#), showed that Lake Mendota, on average, freezes on 22 December (ice-on date), breaks up on 31 March (iceoff date), and has an ice duration of 98 days. Ice thickness and snow depth during the study period were compiled from various sources: 1911-1916 (unpublished data from E. Birge, University of Wisconsin); daily ice thickness during 1961-1962, 1962-1963, and for part of the winter 1963-1964 (Stewart, 1965); 1975-1995 (unpublished data, D. Lathrop, Wisconsin Department of Natural Resources); after 1995, ice thickness and snow depth were sampled once or twice every winter by the NTL-LTER Program (https: //portal.lternet.edu/nis/home.jsp#). In addition, during winters of 2008-2009 and 2009-2010, blue ice, snow ice, total ice (blue ice + snow ice), and snow cover depth were measured weekly at multiple locations on the lake (Hsieh, 2012). In total, there are 251 measurements of total ice, 21 for blue ice, 21 for snow ice, and 49 for snow depth during 1911 to 2014.

Long-term water temperature records were obtained from Robertson (1989) and the NTL-LTER data set (https://portal.lternet.edu/nis/home.jsp#). The frequency of water temperature data varied widely from only one or two profiles per year





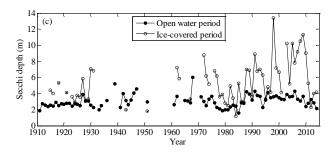


Figure 1. Historical record of annual average (a) air temperature and (b) wind speed in Madison, WI, USA, and (c) Secchi depth in Lake Mendota.

to several profiles for a given day, while there were no data collected in some years between 1931 and 1970. The vertical resolution of the water profiles varied from 0.5 to 2 m and sometimes 5 m when the water column was weakly stratified.

4 Results

4.1 Shifts in air temperature, wind speed, and water clarity

Annual air temperature (Fig. 1a) had a relatively small increase from 1910 until 1980, but has increased dramatically since 1981. Based on a piecewise linear regression algorithm, there was a small warming trend of $0.081\,^{\circ}\text{C}$ per decade during 1911–1980, followed by a dramatic change (a warming trend of 334 $^{\circ}\text{C}$ per decade) from 1981–2014. Figure 1b shows that mean annual wind speed was $4.44\,\text{m s}^{-1}$ until 1994, when a significant shift occurred to $3.74\,\text{m s}^{-1}$ (15% reduction) based on the sequential t test STARS method (Rodionov, 2004). Figure 1c shows Secchi depth for Lake Men-

dota; however, no statistical trend was obtained due to the incompleteness of the data.

Combining the statistically significant breakpoint in air temperature trend that occurred in 1981 and the shift in wind speed in 1994, the Madison climate may be broken into three different periods. The first, from 1911–1980, was a relatively cool period and had an average wind speed of $4.44\,\mathrm{m\,s^{-1}}$. The second period (1981–1993) occurred after the breakpoint in the air temperature trend and had a warmer air temperature and a wind speed of $4.44\,\mathrm{m\,s^{-1}}$. The third period (1994–2014) occurred after the shift in wind speed from $4.44\,\mathrm{to}\,3.74\,\mathrm{m\,s^{-1}}$ and had even warmer air temperatures.

4.2 Model validation and long-term simulations

Here, we provide results of model validity comparisons followed by results of long-term changes in both observed (where available) and simulated conditions for snow and ice thickness, ice-on and ice-off dates, lake water temperature, summer stratification, and thermocline depth.

4.2.1 Ice and snow thickness

Figure 2 shows the comparison of the long-term (from 1911 to 2014) simulation and measured data for blue ice, white ice, and total ice thickness and snow depth. Mean absolute differences between simulated and measured thickness of total ice, blue ice, snow ice, and snow cover are 7.8 cm (n = 251; RMSE = 7.9 cm), 5.5 cm (n = 21; RMSE = 3.3 cm), 1.9 cm (n = 21; RMSE = 2.3 cm), 4.1 cm (n = 49; RMSE = 3.7 cm),respectively. Some discrepancy between the model results and measurements may be due to the 1-D structure of the model. The DYRESM-WQ-I model provides only the lakewide average ice and snow depths, hence no horizontal variation. For a medium-to-large lake, such as Lake Mendota, spatial variations in ice and snow depths should be expected (Bengtsson, 1986). In the winters of 2008–2009 and 2009–2010, ice measurements were made at multiple locations on Lake Mendota (Hsieh, 2012). Data in 2008-2009 showed variations in ice thickness. Total ice thickness in the middle of the lake was approximately 12 cm greater than that at a littoral location (water depth $= 2 \,\mathrm{m}$) in late winter. In 2009-2010, ice cover was fairly spatially uniform through the entire sampling period. Consequently, discrepancy between model results and measurements is expected in those years when ice thickness varied spatially. The accuracy of predictions from DYRESM-WQ-I was compared with other models: MINLAKE (Fang and Stefan, 1996b) produced standard errors of 11 cm for total ice thickness and 6 cm for snow cover for Thrush Lake, Minnesota, and 12 cm for total ice and 7 cm for snow cover for the north basin of Little Rock Lake, Wisconsin. In comparison, similar discrepancies between modeled and observed ice thickness and snow cover were produced from other models including LIMNOS (Vavrus et al., 1996) on Lake Mendota, Wisconsin with dis-

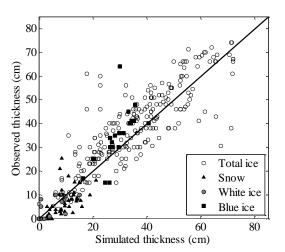


Figure 2. Comparison between observations and simulated total ice, snow cover, white ice, and blue ice.

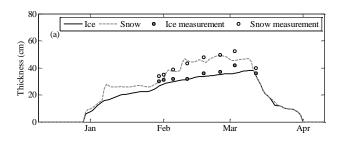
crepancies of 4–9 cm for ice cover; MLI (Rogers et al., 1995) on Harmon Lake, British Columbia, which had up to 6 cm error for ice cover and 4 cm error for snow cover; and CLIMo (Duguay et al., 2003) on lakes in Barrow, Alaska (differences of 5-6 cm for ice thickness); Poker Flat, Alaska (mean absolute error of 2 cm for ice cover and underestimation of snowice thickness of 7 cm); and Churchill, Manitoba (ice thickness observations were within model values for the snow-free and 100% snow-covered scenarios). Duguay et al. (2003) found that variability in snow density and snow accumulation play a significant role in ice thickness, which may account for discrepancies between simulated and observed ice cover thicknesses in our study. In general, DYRESM-WQ-I predicts the ice and snow depths fairly accurately. Figure 3a shows the evolution of simulated ice and snow thickness with multiple ice and snow thickness measurements taken during the winter of 2009–2010. Once ice develops, water beneath the ice continues to freeze, adding to the ice thickness, as heat is conducted from water to the air. In this winter period, lake ice grew fast initially and then slowed substantially. Eventually, the ice reaches its maximum thickness and stops growing (Ashton, 1986). Once air temperatures begin to warm up, ice quickly thins until the ice-off date. Overall, the model is able to capture the growing ice cover as well as the temporally variable snow cover found on the lake.

Figure 3b shows the long-term (1911–2014) simulated annual maximum ice thickness during each winter. The annual maximum thickness varied widely from 20.1 cm (1997–1998) to 72.0 cm (1911–1912) during the 1911–2014 period. The timing when ice reached its maximum thickness also varied considerably, from 17 January (1973) to 7 April (1923). In 73 out of 103 winters, ice reached its maximum thickness in March. Linear regression analysis on simulated annual maximum ice thicknesses indicates that it has decreased at a rate of 12.7 cm per century during 1911–

Table 2. Mean values of climate drivers and lake variables of three hypothesized periods during 1911–2014.

Driver/variable	Unit	Period			Difference in mean		
		(1) 1911– 1980	(2) 1981– 1993	(3) 1994– 2014	(1) and (2)	(2) and (3)	(1) and (3)
Lake driver							
Air temperature (slope)	°C decade ⁻¹	0.081	0.334	0.334			
Wind speed	$\mathrm{m}\mathrm{s}^{-1}$	4.44	4.44	3.74			
Lake variables							
Maximum ice thickness	cm	49.8	44.9	40.7	-4.9	-4.2	-9.1*
Ice-on date (model)	Date	21 Dec	23 Dec	29 Dec	2 days	6 days	8 days*
(observation)	Date	21 Dec	24 Dec	29 Dec	3 days	5 days	8 days*
Ice-off date (model)	Date	9 Apr	2 Apr	30 Mar	−7 days	-3 days	$-10 \mathrm{days}^*$
(observation)	Date	3 Apr	27 Mar	26 Mar	−7 days	-1 days	-8 days*
Ice duration (model)	Days	108.7	99.5	91.1	-9.2*	-8.4*	-17.6*
(observation)	Days	103.2	92.9	85.6	-10.3*	-7.3*	-17.6*
Under-ice water temperature	°C	1.74	1.81	2.08	0.07	0.27	0.34*
Freeze-over water temperature	°C	1.03	1.14	1.66	0.11	0.52	0.63*
Stratification onset date	Date	24 May	17 May	18 May	−7 days	-1 days	−6 days
Midsummer epilimnetic temperature	°C	23.0	23.2	23.4	0.2	0.2	0.4
Midsummer hypolimnetic temperature	°C	12.0	11.8	10.9	-0.2	-0.9*	-1.1*
Epilimnion–hypolimnion temp. difference	°C	10.9	11.4	12.5	0.5	1.1	1.6*
Hypolimnetic heating (1 July–31 August)	°C	0.699	0.688	0.583	-0.011	-0.105	-0.116
Turnover date	Date	20 Sept	21 Sept	3 Oct	1 day	12 days*	13 days*
Stratification duration	Days	119.4	127.4	138.6	8.0	11.2	19.2*

Asterisks (*) mark significant differences between two period (p < 0.05).



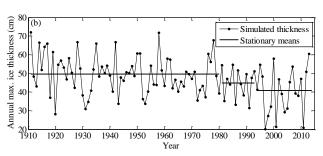


Figure 3. (a) Simulated ice and snow with measured values for the winter 2009–2010 and (b) simulated annual maximum total ice thickness.

2014. These results are much smaller than those for European lakes of similar latitudes (Choiński et al., 2010, 2013; Marszelewski and Skowron, 2006; Skowron, 2009), with changes ranges from 0.20 to 0.60 cm yr⁻¹, almost double that of Lake Mendota if the current change per year is extended to change per century. A t test of the mean values shows a statistically significant (p < 0.05) difference in the mean annual maximum ice thickness between period 1 (1911–1980) and period 3 (1994–2014). Period 2 was not statistically different from either of the other two periods (Table 2).

4.2.2 Ice-on and ice-off dates

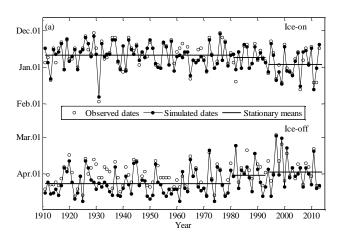
Figure 4 shows measured and simulated ice-on date, ice-off date, and ice duration on the lake. The measured ice-on date is defined as the first day when the lake becomes fully covered in ice, and the ice-off date is the last day of the ice breakup before the open water season. Simulated results and observations are in good agreement, with a mean absolute difference of 2.3 days (RMSE = 2.4 days) for ice-on date and 5.7 days (RMSE = 4.8 days) for ice-off date. It is noted that both the mean error and RMSE are much smaller than the interannual variability in the observed ice-on dates (standard deviation (SD) = 11.2 days) and ice-off dates (SD = 10.6 days). Interannual variations in ice cover on Lake Mendota were large in the past century. Observed ice-on

dates ranged from 3 December (1929) to 30 January (1931) with a range of 58 days. Ice-off dates ranged from 27 February (1998) to 20 April (1923) with a range of 51 days. The model successfully captures the interannual variations of iceon and ice-off dates. For example, it reproduces the unusual late ice-on date in 1930-1931 and several noticeable early ice breakups associated with intense El Niño-Southern Oscillation (ENSO) events, i.e., 1965, 1972, 1982, and 1997 (Anderson et al., 1996; Magnuson et al., 2000; Robertson et al., 2002). Figure 4b shows the ice duration, defined as the period between ice-on and ice-off dates. The mean absolute difference in ice duration between the model results and observations is 6.6 days (RMSE = 6.1 days), compared to the observed SD of 17.9 days. Overall, we consider the model performs well in simulating ice-on and ice-off dates and ice cover duration.

Long-term trends in ice formation are examined by applying linear regression to the model results and observed data. Figure 4 clearly shows progressively later freezing, earlier breakup, and shorter duration in Lake Mendota from 1911 to 2014. Based on model results, ice-on dates exhibit a trend toward later dates by 9.0 days per century, ice-off dates exhibit a trend toward earlier dates of 12.3 days per century, and ice duration exhibits a trend of shorter duration by 21.3 days per century. Model results are in good agreement with those obtained from the observed data (7.4 days later ice-on dates, 9.3 days earlier for ice-off dates, and 18.0 days shorter duration per century). All linear trends from the observed and simulated data are statistically significant (p < 0.05). Similar tendencies have been observed at other lakes, which show decreasing ice cover duration from later ice-on dates and earlier ice-off dates (Choiński et al., 2010, 2013; Marszelewski and Skowron, 2006; Skowron, 2009). However, lakes in near the Great Lakes, North America, and Poland have shown larger rates of change over periods of less than a century. For example, Jensen et al. (2007) observed average ice duration decreases of 5.3 days decade⁻¹ from 1975–2004 in the Great Lakes region, and Polish lakes had observed changes as large as 0.8 to 0.9 days yr⁻¹ for the period 1961-2000(Marszelewski and Skowron, 2006) and 0.5 to 0.6 days yr⁻¹ from 1956-2005 (Skowron, 2009). Mean values of ice-on date, ice-off date, and ice duration for the three selected periods, i.e., 1911-1980, 1981-1993, and 1994-2010, (see Table 2 and Fig. 4) show a statistically significant (p < 0.05, based on t test) difference between period 1 (1911–1980) and period 3 (1994–2014) for all ice cover variables and a statistically significant (p < 0.05) difference between period 1 and period 2 (1981–1993) for ice cover duration.

4.2.3 Water temperature

The performance of the model in simulating water temperatures in the lake is presented in Figs. 5 and 6. For temperatures at the near-surface water, we use the simulated volume-weighted mean water temperatures between depths of 0 and



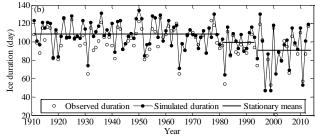


Figure 4. Observed and simulated (a) ice-on and ice-off dates and (b) ice cover duration. The annual ice cover was plotted in the first year of the winter, e.g., the winter 1911–1912 was plotted in the year 1911. Stationary means for three selected periods are denoted by solid lines.

10 m. The simulated epilimnetic temperatures compare well with those estimated from the measured data; the annual mean absolute error is $0.69 \,^{\circ}$ C (n = 3239; RMSE = $0.30 \,^{\circ}$ C), demonstrating the ability of the model to simulate the heat budget in the upper mixed layer of the lake. Near-surface temperatures range from about 0 °C in winter to 26.1 °C in summer, and strongly respond to the net surface heat flux, as illustrated by the 2-3 °C variations that occur in both simulated and measured data, e.g., in the summer of 1921, 1960, 1994, and 2009 (Fig. 5). Overall the model captures interannual variations in epilimnetic temperatures even during extreme years; for example, the relatively high maximum epilimnetic temperatures (> 25 °C) in the summers of 1949, 1955, 1963, 1987, 1988, and 1999, and relatively cold annual maximum epilimnetic temperatures (~ 22 °C) in the summers of 1915, 1924, and 1942.

Figure 6 shows the comparison between the simulated volume-weighted near-bottom (within the hypolimnion) temperatures over the depths between 20–25 m and those estimated from the measured data. The mean absolute error is $1.04\,^{\circ}\text{C}$ (n=3239; RMSE= $0.53\,^{\circ}\text{C}$). Near-bottom temperatures range from $0.2\,^{\circ}\text{C}$ in winter to $19.1\,^{\circ}\text{C}$ in autumn, which is approximately $10\,^{\circ}\text{C}$ less than the variation in near-surface temperatures. Near-bottom temperatures are lowest

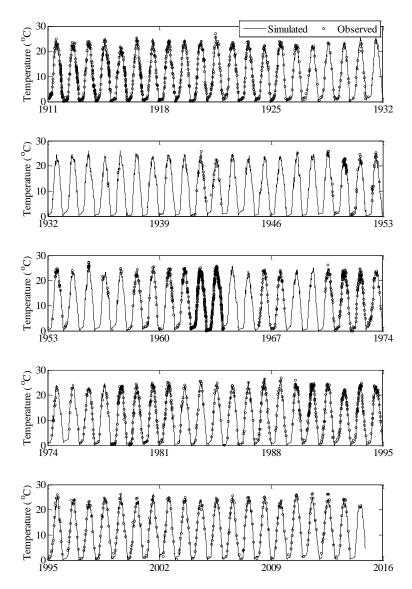


Figure 5. Time series of the simulated and observed volume-weighted near-surface (epilimnetic) temperature (0-10 m) from 1911-2014.

when the lake first freezes, and then slowly increase because of heat released from the bottom sediment. However, we cannot discount that cold inflows could also penetrate into the lake and affect temperature at the selected depths (20–25 m). After ice breakup and just prior to seasonal stratification, temperature in near-bottom waters is usually identical to surface waters and the whole water column undergoes a period of sustained increase in temperature. Hypolimnetic temperatures then stay relatively constant during the stratified period with limited heat exchange associated with strong temperature gradients across the thermocline.

To further examine the model's capability of simulating the extreme differences in temperature, we compare measured and modeled temperatures under years with cold (1924) and warm (1963) epilimnion temperatures and cold (1972) and warm (1926) hypolimnion temperatures.

Figure 7 shows that the model accurately captures the extreme conditions in those 4 years. For plotting, measurement values are assumed to remain constant for the duration of time between measurements. Measurements are generally taken at 1 m intervals over the depth of the water column, but in instances with irregular measurement intervals, temperatures are interpolated at intervals of 1 m for the depth of the lake. Slight variation in temperatures at each depth may be attributed to differences between the averaged seasonal Secchi depth values used to drive the model and the observed Secchi depth values. To demonstrate the model's ability to simulate changes in ice conditions and water temperature under the ice, measured and simulated conditions for these extreme years are presented in Fig. 8. In this figure, the time frame and temperature scales are adjusted to highlight the subtle changes in winter and ice conditions and

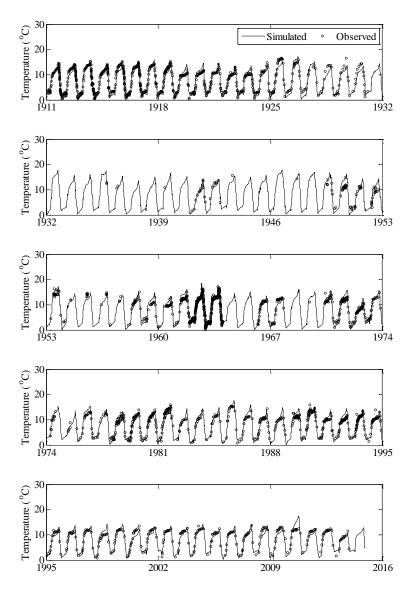


Figure 6. Time series of the simulated and observed volume-weighted near-bottom (hypolimnetic) temperatures (20–25 m) from 1911–2014.

modeled ice and snow thickness are added to the top of the plots. While some discrepancies in temperature are recognized in the model comparison, the model generally captures the inverse stratification under the ice cover. Updated measurements of sediment temperature during winter may provide a better estimate of the sediment heat flux during ice cover conditions, and improve under-ice temperature predictions. Overall, the model can reliably simulate water temperature in open water and ice seasons for extreme cold and warm years.

Midsummer (averaged between 16 July and 15 August when the thermocline was well established) epilimnetic (0–10 m) and hypolimnetic (20–25 m) simulated temperatures from 1911 to 2014 are shown in Fig. 9a. Epilimnetic temperatures range from 19.7 to 24.8 °C. There is no statistically significant temporal trend in the midsummer epilim-

netic temperatures, which may be partly explained by the lack of a warming trend for the midsummer air temperature in the Madison area based on the measured meteorological data (Kucharik et al., 2010). In contrast, hypolimnetic temperatures range from 7.8 to 16.2 °C. The interannual variation in hypolimnetic temperatures (SD = 1.74 °C) is greater than that in epilimnetic temperatures (SD = $1.0 \,^{\circ}$ C). Simulated hypolimnetic temperatures show a decreasing trend of -1.4 °C per century (p < 0.05). Figure 9b shows that the decreased hypolimnetic temperatures resulted in the epilimnion-hypolimnion temperature difference increasing by $2.0\,^{\circ}$ C per century (p < 0.05). Midsummer hypolimnetic temperature and epilimnion (0-10 m)-hypolimnion (20–25 m) temperature difference both exhibit significant (p < 0.05) mean differences between period 1 (1911–1980) and period 3 (1994–2014), as shown in Table 2.

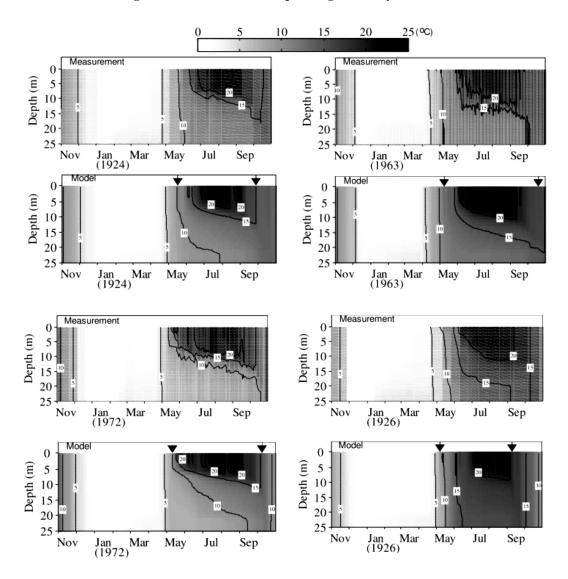


Figure 7. Comparison between the measured and simulated water temperatures as a function of time and depth under the cold epilimnetic year (1924), warm epilimnetic year (1963), cold hypolimnetic year (1972), and warm hypolimnetic year (1926) in Lake Mendota. Arrows mark the dates of onset of stratification and fall turnover.

Figure 10 shows the simulated long-term (104-year) mean under-ice water temperature (volume-weighted average of all depths) ranging from 0.78 to 3.07 °C (mean = 1.74 °C; SD = 0.54 °C). Based on model results, under-ice temperatures reveal a significant increasing trend (p < 0.05) of 0.48 °C per century during 1911–2014, suggesting that air temperature and wind speed may affect under-ice water temperature. For the selected periods, the under-ice (bold lines) and freeze-over (dashed lines; volume-weighted average of all depths) water temperatures exhibit interesting features. The difference between the water temperature over the entire ice-covered period and the freeze-over water temperature has decreased through time, indicating less heat gain during the winter, which may relate to a shorter time to transfer heat and a smaller gradient in temperatures between the

lake and the bottom sediments. The under-water ice temperatures and freeze-over water temperatures both show significant (p < 0.05) differences between period 1 (1911–1981) and period 3 (1994–2014), as shown in Table 2.

4.2.4 Summer stratification period and thermocline depth

We characterize summer stratification by the dates of the onset of stratification and fall turnover, and the total duration of stratification. Accurately describing these conditions requires high frequency observations, which is challenging for long-term data sets. As a result, we used modeled data to determine these variables. The dates of stratification onset/fall turnover are defined as the day when the surface-to-bottom temperature difference is greater/less than 2 °C

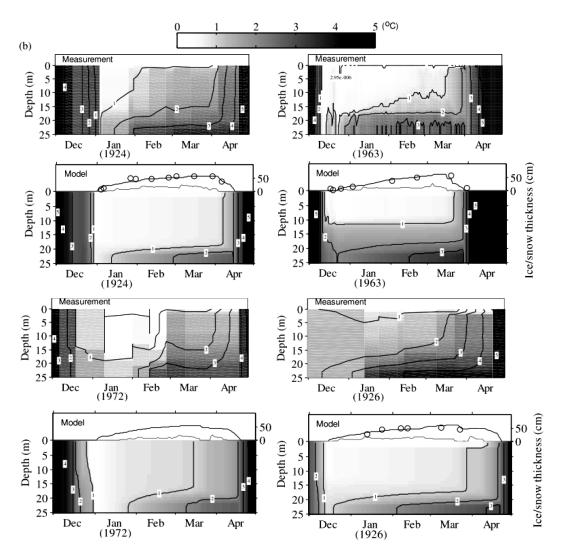


Figure 8. Comparison between the measured and simulated water temperatures and ice/snow thickness under the cold epilimnetic year (1924), warm epilimnetic year (1963), cold hypolimnetic year (1972), and warm hypolimnetic year (1926) in Lake Mendota during the ice-covered period. Time series are simulated ice and snow thickness (solid lines) with measurements (open circles).

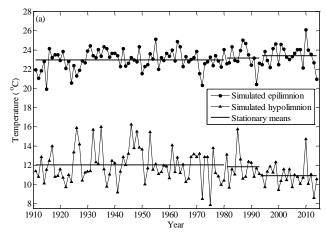
(Robertson and Ragotzkie, 1990). Figure 11 shows the dates of onset of stratification breakdown (fall turnover), and the total duration of stratification. The onset dates varied between 17 April (1977) and 30 June (1981), and the date of fall turnover varied from 2 August (1965) to 19 October (2013). Over a century (1911–2014), the onset of thermal stratification has become earlier by 12.3 days (p < 0.05), and fall turnover has become later by 14.6 days (p < 0.05), resulting in the stratification period increasing by 26.8 days (p < 0.05). Stratification onset date shows no significant difference among the three periods (see Table 2); however, the fall turnover date is significantly (p < 0.05) different between periods 2 and 3 and between periods 1 and 3, and the duration of stratification is significantly (p < 0.05) different between periods 1 and 3, as shown in Table 2.

The thermocline depth, defined as the depth of maximum temperature gradient, is determined from the model results (not shown in figure for brevity). During 1911–2014, the midsummer thermocline depth in Lake Mendota varied from 8.3 to 12.4 m (mean = 10.7 m; SD = 0.84 m) with no significant long-term change.

5 Discussion

5.1 Significance of lake drivers

Changes in long-term simulated ice cover and thermal variables in Lake Mendota from 1911–2014 appear to occur over short time frames within this period, synchronous with rapid changes in measured drivers (i.e., air temperature, wind speed, and water clarity). The variables examined included



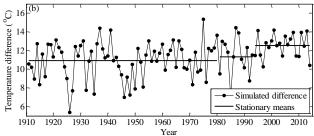


Figure 9. (a) Simulated midsummer (16 July–15 August) volume-averaged epilimnion and hypolimnion temperatures, and (b) epilimnion—hypolimnion temperature difference. Stationary means for three selected periods are denoted by solid lines.

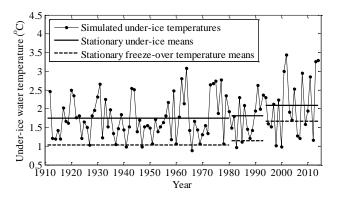


Figure 10. Simulated mean under-ice water temperatures (volume-weighted averages of all depths) during the ice-covered period between 1911 and 2014. The stationary means for three selected periods of under-ice water temperatures and freeze-over water temperatures are also plotted.

ice-on/ice-off dates, maximum ice thickness, freeze-over water temperature, midsummer epilimnetic and hypolimnetic temperatures, summer hypolimnetic heating, and dates of stratification onset and fall turnover. To identify the relationship between the drivers and each of these variables, we employed Pearson correlation analysis on the detrended driver

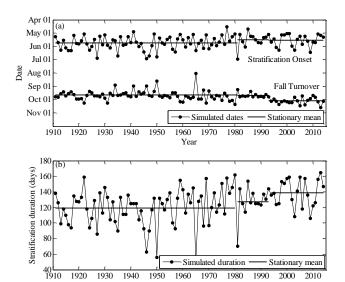


Figure 11. (a) Simulated date of stratification onset and fall turnover and **(b)** stratification duration. Stationary means for three selected periods are denoted by solid lines.

and simulation data. While using this method does not allow us to directly determine causality, we may identify possible related drivers to changes in lake variables and the relative importance of relationship of three drivers (i.e., air temperature, wind speed, and water clarity) to the lake variables. To calculate correlation coefficients, each lake driver was averaged over a fixed period (e.g., April-May or November-December) and then paired with each of the simulated lake variables from the same period. The averaging period for air temperature and wind speed was chosen based on the fixed period that yielded the best correlation. We chose to employ fixed periods because thorough testing indicated that using a dynamic period introduced seasonal meteorological variations into the analysis. For instance, the correlation coefficient between onset date and the mean air temperature averaged over the prior month is expected to be high simply due to the seasonal variations over the course of the year, i.e., the later in the spring, the warmer air temperature. Seasonal Secchi depths were compiled for six seasonal periods: winter, spring turnover, early stratification, summer, destratification, and fall turnover (Lathrop et al., 1996), and the period closest to the averaging period used for air temperature and wind speed was used for correlation analysis. The averaging periods used for calculating correlation coefficients of each pair of variables are listed in Table 3. We discuss below the correlations for each pair of variables, shown in Fig. 12.

5.1.1 Ice cover variables

Ice-on and ice-off dates have been shown to be sensitive to climate conditions (Livingstone, 1997; Magnuson et al., 2000; Robertson et al., 1992). For both air temperature and

Table 3. Averaging periods for lake drivers used for calculating correlation coefficients of each pair of variables.

Lake variables	Air temperature/ wind speed	Secchi depth*
Ice-on date	November-December	13 October – ice-on
Ice-off date	February-March	ice-on – ice-off
Max. ice thickness	January-March	ice-on – ice-off
Freeze-over water temperature	November-December	13 October – ice-on
Date of stratification onset	April–May	ice-off – 10 May
Summer epilimnetic temperature	16 July-15 August	30 June–2 September
Summer hypolimnetic temperature	May	ice-off – 30 June
Hypolimnetic heating	July-August	30 June-2 September
Date of fall turnover	September	3 September–12 October

^{*} Six seasonal periods defined in Lathrop et al. (1996).

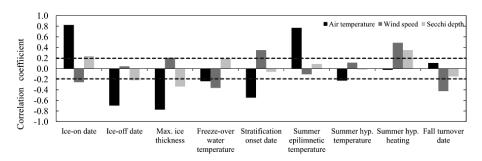


Figure 12. Correlation coefficients between lake variables and drivers. The critical value (dashed lines) for significant correlation (p < 0.05) is 0.193 (n = 104).

wind speed, the averages from 1 November to 31 December (N-D) give the highest correlation with ice-on date; in agreement with the results of Assel and Robertson (1995) and similar to Gao and Stefan (1999). Averaged air temperature and wind speed over the period from 1 February to 31 March (FM) provide the highest correlation with ice-off date, consistent with the study by Gao and Stefan (1999), who found that ice-off dates for 10 Minnesota lakes correlated significantly with February-April air temperatures. The strong positive correlation (r = 0.82) between ice-on date and N-D air temperature indicates a relationship between warmer N–D air temperatures and later freezing dates. Strong negative correlation between ice-off date and F-M air temperature (r = -0.70) indicates a relationship between earlier ice breakup and warmer F-M air temperatures. In contrast to air temperature, ice cover is only weakly related to the seasonal average wind speed. Nevertheless, the correlation between ice-on date and wind speed (r = -0.26) is significant, indicating a relationship between decreasing wind speed and earlier ice-on dates. Since large wind events prevent ice formation by breaking up skim ice, decreased wind speeds allow ice cover to form slightly earlier in the year. In the Madison area, the decreasing wind speeds may act to slightly mitigate the effects of increasing air temperature in later ice freezing. Correlation between ice dates and Secchi depths is low (r = 0.24 for ice-on dates and r = -0.22 for ice-off dates), indicating that water clarity has only a minor relationship with ice dates, in agreement with the simulation results of Fang and Stefan (1997). For both ice-on and ice-off dates, correlations with wind speed and Secchi depth are much less significant than with air temperature, indicating that air temperature has a more significant relationship with ice-on and ice-off dates and may be a more significant indicator of ice cover dates and ultimately ice cover duration.

Annual maximum ice thickness is negatively correlated with the 1 January–31 March (J–F–M) averaged air temperature (r = -0.77) and weakly correlated with J–F–M wind speed (r = 0.21), indicating a better relationship between annual maximum ice thickness and air temperature than for wind speed. The relationship of air temperatures on ice phenology is consistent with previous findings for lakes in northern Wisconsin, Canada, and Maine (Gao and Stefan, 2004).

The strong correlations between air temperature and ice cover variables agree with several earlier studies (Anderson et al., 1996; Gao and Stefan, 2004; Livingstone, 1997; Vavrus et al., 1996; Williams et al., 2004). Snowfall has also been shown to be related to ice-off date (Jensen et al., 2007) and ice thickness (Duguay et al., 2003; Vavrus et al., 1996) because snowfall changes surface albedo and isolates ice cover from the atmosphere. We found that simulated number of

snow days (number of days when the lake has snow cover) is strongly correlated with ice-off date (r = 0.70) and maximum ice thickness (r = 0.75), indicating snowfall is also significantly related to ice cover.

5.1.2 Water temperature and stratification

Figure 10 shows that the simulated water temperatures in Lake Mendota at the time of freezing have been increasing since 1911. The correlation between freeze-over water temperature and lake drivers during 1 November and 31 December (N–D) is significant but with low rvalues for wind speed (r=-0.37) and air temperature (r=-0.24) and insignificant for Secchi depth (r=0.18). This result indicates that wind mixing is related to cooling of the water column before Lake Mendota freezes.

The simulated onset dates of stratification are negatively correlated with April–May (A–M) air temperature (r=-0.55) and positively correlated with A–M wind speed (r=0.35). In Lake Mendota, the combination of increasing air temperatures and decreasing wind speeds are both related to earlier onset of stratification. Austin and Colman (2007) suggested that the declining ice cover combined with higher air temperatures cause the earlier onset of stratification in Lake Superior at a rate of 0.5 day yr $^{-1}$. However, no correlation between ice-off date and the onset of stratification was found for Lake Mendota in this study.

Midsummer (16 July-15 August) epilimnetic temperatures are most strongly correlated with the air temperature averaged over the corresponding period. Epilimnetic temperature is highly correlated with air temperature (r = 0.77) and not significantly correlated with wind speed averaged over the corresponding period (r = -0.11) and Secchi depth (r = 0.09). Midsummer hypolimnetic temperatures depend on the timing of stratification (how long the near-bottom water is heated before the onset of stratification) and the amount of heat mixed into hypolimnion before and during the stratification period. Hypolimnetic temperatures are weakly correlated with air temperatures (r = -0.23) and not significantly correlated with wind speed (r = 0.11) and Secchi depth (r = -0.02). Summer hypolimnetic heating (temperature change between 1 July and 31 August, J-A) is most strongly correlated with J-A wind speed (r = 0.49), moderately correlated with Secchi depth averaged over 30 June-2 September (r = 0.35), and not significantly correlated with J–A air temperature (r = -0.02). This indicates a relationship between stronger winds and clearer water and deeper heat mixing.

Fall turnover occurs when the lake water cools, driven largely by colder air temperature and wind-induced mixing. The date of fall turnover is significantly negatively correlated with September wind speed (r = -0.43) so that higher wind speed is related to earlier fall turnover. Air temperature (r = 0.11) and Secchi depth (r = -0.15) are not significantly correlated with the timing of fall mixing. Interestingly, the

midsummer epilimnion—hypolimnion temperature difference has a higher correlation with turnover date (r=0.62) than any of the three lake drivers. This finding suggests that the influences of spring conditions may be transmitted to the following summer and fall seasons. In other words, the cooler hypolimnion and the greater epilimnion—hypolimnion temperature difference after a warmer and less windy spring may be related to later fall turnover and a longer stratification period.

5.2 Abrupt changes in lake variables

To investigate the effects of abrupt changes in air temperature and wind speed on lake ice cover and water temperatures, we used the hydrodynamic model DYRESM-WQ-I to describe changes in several lake variables during 1911-2014. Simulation results were used to examine differences in mean values of these lake variables between specific periods (see Sect. 4.1). For each period of the selected periods, mean lake variables were calculated and the differences between periods were analyzed with t tests to determine if they were significantly different. Table 2 lists the mean values and differences for the nine lake variables during the three selected periods. Comparison of period 1 (1911–1980) to period 2 (1981-1993) of lake variables shows a shift to warmer air temperature, period 2 to period 3 (1994–2014) represents an abrupt change to lower wind speed, and period 1 to period 3 represents a shift to warmer air temperature combined with an abrupt change to lower wind speeds.

5.2.1 Ice cover

Three simulated ice cover variables (maximum ice thickness, ice-on date, and ice-off date) show no significant difference in means between periods 1 and 2. In other words, the abrupt change in air temperature trend does not result in a different ice period even though the ice cover variables are all highly correlated with air temperature (r > 0.70). This may be because the change in air temperatures was not of sufficient magnitude to cause a particularly large change in ice cover or it may signify that other drivers are contributing to changes in ice cover variables. Additionally, no significant difference is observed between period 2 and period 3 for the ice cover variables since the wind speed and ice cover variables are only weakly correlated. The ice variables do show a statistically significant difference in mean values between periods 1 and 3, indicating that a significant shift in these variables occurs only after a sufficiently large increase in air temperature and an abrupt shift in wind speed within the time between periods 1 and 3. In other words, air temperature needs to increase sufficiently to observe a statistically significant difference in ice cover. Ice cover duration, however, shows a significant difference in the mean between all periods (1-2, 2-3, 1)and 1-3), indicating that distinct differences in ice cover duration can be affected by both trends in air temperature (i.e., there was a large-enough change in air temperature between each period) and an abrupt shift in the wind speed. The combined effects of slightly later ice-on dates and earlier ice-off dates during each of the three periods resulted in statistically significant difference in mean ice cover duration values between each of the three periods.

Analysis of simulated maximum ice thickness, ice-on date, ice-off date, and ice cover duration using the method of Rodionov (2004) shows that the most statistically significant timing of the shift in these ice cover variables occurs in the winter of 1997-1998, but a major shift in the air temperature or wind speed data was not observed at that time. The unusual winter of 1997-1998 strongly drove the statistically significant difference in mean values between periods 1 and 3 rather than the abrupt shift in wind speed in 1994. Interestingly, similar results have been reported in Lake Superior, where statistically significant step changes were found in winter ice duration and maximum wintertime ice extent; these step changes account for most of the long-term trends in ice cover for the lake (Van Cleave et al., 2014). The timing of this step change may be attributed to a combination of the longer term changes in meteorological conditions and the short-term annual change occurring in the warm El Niño winter of 1997-1998 (Van Cleave et al., 2014). Mueller et al. (2009) found that a similar climate shift between 1997 and 1998 initiated a change in lake ice phenology from infrequent to frequent summer loss in several high-Arctic lakes. Similarly, lakes in Poland show a considerable statistical relationship between ice cover and the North Atlantic Oscillation winter indexes (Skowron, 2009), indicating that ice cover may be driven by other large oscillations as well.

5.2.2 Water temperature and stratification

Means of five simulated lake variables (under-ice water temperature, freeze-over water temperature, epilimnionhypolimnion temperature difference (indicative of strength of stratification), and duration of stratification) over the three periods have significant (p < 0.05) differences only between period 1 and period 3. This change likely occurs because of the combined effects of large changes in air temperature and a change in wind speed. Both air temperature and wind speed are significantly correlated with these five lake variables. Each driver alone may not be strong enough to cause a major shift in the lake variables, but their combined effects may reinforce the drivers of abrupt change in ice and thermal phenology. Further work is required to examine how the major drivers may either reinforce or dampen lake ice and temperature responses, particularly in relation to directional shifts predicted under climate change.

Fall turnover date, highly correlated with wind speed, exhibits a significant (p < 0.05) shift in the mean value in 1994, corresponding with the abrupt shift in the wind speed. Interestingly, hypolimnetic water temperatures, which are not significantly correlated with wind speed, but are correlated

with air temperatures, also show a significant (p < 0.05) shift in the mean value in 1994. Hypolimnetic heating, significantly correlated with wind speed (r = 0.49), does not exhibit a significant breakpoint, nor are any of the mean differences among the three periods significant. Given the high correlation between wind speed and hypolimnetic heating, it is hypothesized that there should be a shift in hypolimnetic heating caused by the abrupt shift in wind speed in 1994. The lack of statistically significant step change may be explained by the simultaneous high correlation between Secchi depth and hypolimnetic heating (r = 0.35), indicating that water clarity may act to inhibit heating regardless of changes in wind speed, or it may be acting to filter or mitigate the effects of the wind speed shift. Finally, mean onset date of stratification and midsummer epilimnetic temperature exhibit no difference among the three periods. This may be due to two processes: (i) the climate signal is being filtered out by the lake or (ii) the external perturbation of the system is not yet strong enough to trigger a major shift in the system's internal dynamics.

5.3 Ecological significance of long-term changes in lake variables

Changes in lake ice cover and thermal structure are of great ecological significance. Summer stratification inhibits the vertical transport of oxygen and nutrients. The vertical temperature gradient in Lake Mendota increased (Fig. 9b), which should decrease the depth of vertical mixing and oxygen penetration and decrease the transport of nutrients from the hypolimnion to the epilimnion (Fee et al., 1994). Thus, increases in air temperature may increase the epilimnetichypolimnetic temperature gradient and decrease the extent of summer algal blooms in the Lake Mendota where internal loading of phosphorus has been shown to be significant to its summer phosphorus budget (Lathrop et al., 1998; Soranno et al., 1997). Additionally, phosphorus entrainment predominately occurs during periods of high wind (Kamarainen et al., 2009; Stauffer and Armstrong, 1986). Algal blooms have been associated with increases in epilimnetic phosphorus due to these high-wind episodes (Robarts et al., 1998; Soranno et al., 1997; Stauffer and Lee, 1973). Changes in the frequency of high-wind episodic events may further impact the growth of algal blooms within Lake Mendota (Kara et al., 2012). Elevated water temperatures can affect plankton community composition and abundance (Elliot et al., 2005; Findlay et al., 2001; Francis et al., 2014; Rice et al., 2015) and fish populations (Carpenter et al., 1992; De Stasio et al., 1996; Gunn, 2002; Magnuson et al., 1990). High water temperatures have been also shown to enhance the dominance of cyanobacteria (Huber et al., 2008; Jöhnk et al., 2008). Such changes in algal blooms, zooplankton populations, and fish populations may have drastic effects on the overall food web within Lake Mendota (Carpenter et al., 1998). Variations in ice cover conditions have impacts on ecosystems by dramatically changing habitat factors such as light and temperature (Adrian et al., 1999; Quayle et al., 2002). Such changes impact the distribution, behavior, community composition, reproduction, and evolutionary adaptations of organisms (Sala et al., 2000). Previous studies have shown that climate change will likely affect the biodiversity of freshwater ecosystems (Heino et al., 2009; Mantyka-Pringle et al., 2014; Wrona et al., 2006). Climate change can bring asynchronies in biotic communities that may result in a phenological decoupling of trophic relationships (Stenseth and Mysterud, 2002).

6 Conclusions

The one-dimensional hydrodynamic ice model, DYRESM-WQ-I, is developed and validated, then used to simulate the ice cover and thermal structure of Lake Mendota, WI from 1911–2014. The model reliably reproduces the interannual variations and long-term (104-year) changes in ice cover and thermal structure. To our knowledge, this study presents the first attempt to continuously model both ice cover and thermal structure of a lake over a period as long as a century. Simulated ice cover over this period has changed dramatically: freezing later (9.0 days per century), breaking up earlier (12.3 days per century), resulting in shorter ice duration (21.3 days per century), and thinner maximum ice thickness (12.7 cm per century). These results agree well with the observed data and previous studies. For lake thermal structure, results of the continuous model simulation indicate an earlier onset of thermal stratification (12.3 days per century), later fall turnover (14.6 days per century), and a longer stratification period (26.8 days per century) during this period. In addition, simulated midsummer hypolimnetic temperature decreased (-1.4°C per century), causing midsummer epilimnetic-hypolimnetic temperature differences (strength of stratification) to increase (2.0 °C per century). Interestingly, there is no significant trend in midsummer epilimnetic temperatures.

Correlations comparing simulated lake conditions with seasonally averaged meteorological conditions indicate that, among the three drivers, air temperature has the largest relationship with the ice cover variables (ice-on and ice-off dates, and maximum ice thickness) and with three stratification variables (date of the onset of stratification, epilimnetic temperatures, and hypolimnetic temperatures). Freeze-over water temperature, summer hypolimnetic heating, and date of fall turnover all have the largest correlation with wind speed. Both air temperature and wind speeds are highly correlated with the onset of stratification. Secchi depth does not appear to have a strong relationship with interannual variability of these variables for Lake Mendota, but in combination with wind speed may be related to hypolimnetic heating.

Changes in meteorological factors over the past 104 years were examined to determine if there have been abrupt shifts, rather than linear changes. Based on a change in the trend of air temperature increase occurring in 1981 and a major shift in wind speed in 1994, the Madison climate is divided into three distinct periods: 1911–1980, with relatively low air temperatures and mean wind speeds of $4.44 \,\mathrm{m\,s^{-1}}$; 1981– 1993, with higher air temperatures and mean wind speeds of 4.44 m s⁻¹; and 1994–2014 with still higher air temperatures and mean wind speed of 3.74 m s⁻¹. Ice cover duration exhibited a significant difference in the mean among all three periods, while ice-on date, ice-off date, and maximum ice thickness only show a significant difference between periods 1 and 3, indicating that only with a large change in air temperature and an abrupt shift in wind speeds are change in the ice cover variables statistically different. Midsummer hypolimnetic temperature and fall turnover date both reveal significant (p < 0.05) differences in the mean value in 1994, corresponding with the abrupt shift toward lower wind speeds. Some lake variables (under-ice water temperature, freeze-over water temperature, epilimnionhypolimnion temperature difference, and stratification duration) may not be driven by either the change in air temperature trend or the abrupt shift in wind speed alone, but a shift in the mean of the lake variables does occur in 1994 when both the air temperatures are warmest and the wind speed experienced an abrupt shift. The exact timing of shifts may be difficult to define because of extreme changes in weather in specific years and it may mask the longer term changes in meteorological conditions (i.e., abrupt shifts).

Linear trends from the extensive data collection may be misleading as they masks these sudden shifts in the air temperature and wind speed drivers and lake ice cover and thermal structure variables. Examining the mean differences in lake variables in response to shifts in air temperature and abrupt shifts in wind speeds provide a better understanding of how the southern Wisconsin climate has changed and what impact those changes have on shifts in the ice cover and water temperature of dimictic Lake Mendota. It is shown that air temperature and wind speed changes have occurred in stages and lake variables have responded in a nonlinear way to these changes.

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